

**Functions (F)**

Kindergarten	Grade 1	Grade 2	Grade 3	Grade 4	Grade 5	Grade 6	Grade 7	Grade 8	Grades 9-12
								<p><b>MA.8.F.1</b> Define, evaluate and compare functions.</p> <p><b>MA.8.F.1.1</b> Given a set of ordered pairs, a table, a graph or mapping diagram, determine whether the relationship is a function. Identify the domain and range of the relation.</p> <p><b>MA.8.F.1.2</b> Given a function defined by a graph or an equation, determine whether the function is a linear function. Given an input-output table, determine whether it could represent a linear function.</p> <p><b>MA.8.F.1.3</b> Analyze a real-world written description or graphical representation of a functional relationship between two quantities and identify where the function is increasing, decreasing or constant.</p>	<p><b>MA.912.F.1</b> Understand, compare and analyze properties of functions.</p> <p><b>MA.912.F.1.1</b> Given an equation or graph that defines a function, determine the function type. Given an input-output table, determine a function type that could represent it.</p> <p><b>MA.912.F.1.2</b> Given a function represented in function notation, evaluate the function for an input in its domain. For a real-world context, interpret the output.</p> <p><b>MA.912.F.1.3</b> Calculate and interpret the average rate of change of a real-world situation represented graphically, algebraically or in a table over a specified interval.</p> <p><b>MA.912.F.1.4</b> Write an algebraic expression that represents the difference quotient of a function. Calculate the numerical value of the difference quotient at a given pair of points.</p> <p><b>MA.912.F.1.5</b> Compare key features of linear functions each represented algebraically, graphically, in tables or written descriptions.</p> <p><b>MA.912.F.1.6</b> Compare key features of linear and nonlinear functions each represented algebraically, graphically, in tables or written descriptions.</p> <p><b>MA.912.F.1.7</b> Compare key features of two functions each represented algebraically, graphically, in tables or written descriptions.</p> <p><b>MA.912.F.1.8</b> Determine whether a linear, quadratic or exponential function best models a given real-world situation.</p> <p><b>MA.912.F.1.9</b> Determine whether a function is even, odd or neither when represented algebraically, graphically or in a table.</p>
									<p><b>MA.912.F.2</b> Identify and describe the effects of transformations on functions. Create new functions given transformations.</p> <p><b>MA.912.F.2.1</b> Identify the effect on the graph or table of a given function after replacing <math>f(x)</math> by <math>f(x)+k</math>, <math>kf(x)</math>, <math>f(kx)</math> and <math>f(x+k)</math> for specific values of <math>k</math>.</p> <p><b>MA.912.F.2.2</b> Identify the effect on the graph of a given function of two or more transformations defined by adding a real number to the <math>x</math>- or <math>y</math>-values or multiplying the <math>x</math>- or <math>y</math>-values by a real number.</p> <p><b>MA.912.F.2.3</b> Given the graph or table of <math>f(x)</math> and the graph or table of <math>f(x) + k</math>, <math>kf(x)</math>, <math>f(kx)</math> and <math>f(x+k)</math>, state the type of transformation and find the value of the real number <math>k</math>.</p> <p><b>MA.912.F.2.4</b> Given the graph or table of values of two or more transformations of a function, state the type of transformation and find the values of the real number that defines the transformation.</p> <p><b>MA.912.F.2.5</b> Given a table, equation or graph that represents a function, create a corresponding table, equation or graph of the transformed function defined by adding a real number to the <math>x</math>- or <math>y</math>-values or multiplying the <math>x</math>- or <math>y</math>-values by a real number.</p>

**MA.912.F.3**

**Create new functions from existing functions.**

**MA.912.F.3.1**

Given a mathematical or real-world context, combine two functions, limited to linear and quadratic, using arithmetic operations. When appropriate, include domain restrictions for the new function.

**MA.912.F.3.2**

Given a mathematical or real-world context, combine two or more functions, limited to linear, quadratic, exponential and polynomial, using arithmetic operations. When appropriate, include domain restrictions for the new function.

**MA.912.F.3.3**

Solve mathematical and real-world problems involving functions that have been combined using arithmetic operations.

**MA.912.F.3.4**

Represent the composition of two functions algebraically or in a table. Determine the domain and range of the composite function.

**MA.912.F.3.5**

Solve mathematical and real-world problems involving composite functions.

**MA.912.F.3.6**

Determine whether an inverse function exists by analyzing tables, graphs and equations.

**MA.912.F.3.7**

Represent the inverse of a function algebraically, graphically or in a table. Use composition of functions to verify that one function is the inverse of the other.

**MA.912.F.3.8**

Produce an invertible function from a non-invertible function by restricting the domain.

**MA.912.F.3.9**

Solve mathematical and real-world problems involving inverse functions.