

Grade 6 B.E.S.T. Instructional Guide for Mathematics

The B.E.S.T. Instructional Guide for Mathematics (B1G-M) is intended to assist educators with planning for student learning and instruction aligned to Florida's Benchmarks for Excellent Student Thinking (B.E.S.T.) Standards. This guide is designed to aid high-quality instruction through the identification of components that support the learning and teaching of the B.E.S.T. Mathematics Standards and Benchmarks. The B1G-M includes an analysis of information related to the B.E.S.T. Standards for Mathematics within this specific mathematics course, the instructional emphasis and aligned resources. This document is posted on the <u>B.E.S.T. Standards for Mathematics webpage</u> of the Florida Department of Education's website and will continue to undergo edits as needed.

Structural Framework and Intentional Design of the B.E.S.T. Standards for Mathematics

Florida's B.E.S.T. Standards for Mathematics were built on the following.

- The coding scheme for the standards and benchmarks was changed to be consistent with other content areas. The new coding scheme is structured as follows: Content.GradeLevel.Strand.Standard.Benchmark.
- Strands were streamlined to be more consistent throughout.
- The standards and benchmarks were written to be clear and concise to ensure that they are easily understood by all stakeholders.
- The benchmarks were written to allow teachers to meet students' individual skills, knowledge and ability.
- The benchmarks were written to allow students the flexibility to solve problems using a method or strategy that is accurate, generalizable and efficient depending on the content (i.e., the numbers, expressions or equations).
- The benchmarks were written to allow for student discovery (i.e., exploring) of strategies rather than the teaching, naming and assessing of each strategy individually.
- The benchmarks were written to support multiple pathways for success in career and college for students.
- The benchmarks should not be taught in isolation but should be combined purposefully.
- The benchmarks may be addressed at multiple points throughout the year, with the intention of gaining mastery by the end of the year.
- Appropriate progression of content within and across strands was developed for each grade level and across grade levels.
- There is an intentional balance of conceptual understanding and procedural fluency with the application of accurate real-world context intertwined within mathematical concepts for relevance.
- The use of other content areas, like science and the arts, within real-world problems should be accurate, relevant, authentic and reflect grade-level appropriateness.

Components of the B.E.S.T. Instructional Guide for Mathematics

The following table is an example of the layout for each benchmark and includes the defining attributes for each component. It is important to note that instruction should not be limited to the possible connecting benchmarks, related terms, strategies or examples provided. To do so would strip the intention of an educator meeting students' individual skills, knowledge and abilities.

Benchmark

focal point for instruction within lesson or task

This section includes the benchmark as identified in the <u>B.E.S.T. Standards for Mathematics</u>. The benchmark, also referred to as the Benchmark of Focus, is the focal point for student learning and instruction. The benchmark, and its related example(s) and clarification(s), can also be found in the course description. The 9-12 benchmarks may be included in multiple courses; select the example(s) or clarification(s) as appropriate for the identified course.

Terms from the K-12 Glossary
This section includes terms from
Appendix C: K-12 Glossary, found
within the B.E.S.T. Standards for
Mathematics document, which are
relevant to the identified Benchmark
of Focus. The terms included in this
section should not be viewed as a
comprehensive vocabulary list, but
instead should be considered during
instruction or act as a reference for
educators.

Vertical Alignment

across grade levels or courses

This section includes a list of related benchmarks that connect vertically to the Benchmark of Focus. Vertical alignment is the intentional progression of content from one year to the next, spanning across multiple grade levels. Benchmarks listed in this section make mathematical connections from prior grade levels or courses in future grade levels or courses within and across strands. If the Benchmark of Focus is a new concept or skill, it may not have any previous benchmarks listed. Likewise, if the Benchmark of Focus is a mathematical skill or concept that is finalized in learning and does not have any direct connection to future grade levels or courses, it may not have any future benchmarks listed. The information included in this section is not a comprehensive list, and educators are encouraged to find other benchmarks within a vertical progression.

Purpose and Instructional Strategies



This section includes further narrative for instruction of the benchmark and vertical alignment. Additionally, this section may also include the following:

- explanations and details for the benchmark;
- vocabulary not provided within Appendix C;
- possible instructional strategies and teaching methods; and
- strategies to embed potentially related Mathematical Thinking and Reasoning Standards (MTRs).

Common Misconceptions or Errors

This section will include common student misconceptions or errors and may include strategies to address the identified misconception or error. Recognition of these misconceptions and errors enables educators to identify them in the classroom and make efforts to correct the misconception or error. This corrective effort in the classroom can also be a form of formative assessment within instruction.

Strategies to Support Tiered Instruction

The instructional strategies in this section address the common misconceptions and errors listed within the above section that can be a barrier to successfully learning the benchmark. All instruction and intervention at Tiers 2 and 3 are intended to support students to be successful with Tier 1 instruction. Strategies that support tiered instruction are intended to assist teachers in planning across any tier of support and should not be considered exclusive or inclusive of other instructional strategies that may support student learning with the B.E.S.T. Mathematics Standards. For more information about tiered instruction, please see the Effective Tiered Instruction for Mathematics: ALL Means ALL document.

Instructional Tasks

demonstrate the depth of the benchmark and the connection to the related benchmarks

This section will include example instructional tasks, which may be open-ended and are intended to demonstrate the depth of the benchmark. Some instructional tasks include integration of the Mathematical Thinking and Reasoning Standards (MTRs) and related benchmark(s). Enrichment tasks may be included to make connections to benchmarks in later grade levels or courses. Tasks may require extended time, additional materials and collaboration.

Instructional Items

demonstrate the focus of the benchmark

This section will include example instructional items which may be used as evidence to demonstrate the students' understanding of the benchmark. Items may highlight one or more parts of the benchmark.

*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.



Mathematical Thinking and Reasoning Standards MTRs: Because Math Matters

Florida students are expected to engage with mathematics through the Mathematical Thinking and Reasoning Standards (MTRs) by utilizing their language as a self-monitoring tool in the classroom, promoting deeper learning and understanding of mathematics. The MTRs are standards which should be used as a lens when planning for student learning and instruction of the B.E.S.T. Standards for Mathematics.

Structural Framework and Intentional Design of the Mathematical Thinking and Reasoning Standards

The Mathematical Thinking and Reasoning Standards (MTRs) are built on the following.

- The MTRs have the same coding scheme as the standards and benchmarks; however, they are written at the standard level because there are no benchmarks.
- In order to fulfill Florida's unique coding scheme, the 5th place (benchmark) will always be a "1" for the MTRs.
- The B.E.S.T. Standards for Mathematics should be taught through the lens of the MTRs.
- At least one of the MTRs should be authentically and appropriately embedded throughout every lesson based on the expectation of the benchmark(s).
- The bulleted language of the MTRs were written for students to use as self-monitoring tools during daily instruction.
- The clarifications of the MTRs were written for teachers to use as a guide to inform their instructional practices.
- The MTRs ensure that students stay engaged, persevere in tasks, share their thinking, balance conceptual understanding and procedures, assess their solutions, make connections to previous learning and extended knowledge, and apply mathematical concepts to real-world applications.
- The MTRs should not stand alone as a separate focus for instruction, but should be combined purposefully.
- The MTRs will be addressed at multiple points throughout the year, with the intention of gaining mastery of mathematical skills by the end of the year and building upon these skills as they continue in their K-12 education.



MA.K12.MTR.1.1 Actively participate in effortful learning both individually and collectively.

Mathematicians who participate in effortful learning both individually and with others:

- Analyze the problem in a way that makes sense given the task.
- Ask questions that will help with solving the task.
- Build perseverance by modifying methods as needed while solving a challenging task.
- Stay engaged and maintain a positive mindset when working to solve tasks.
- Help and support each other when attempting a new method or approach.

Clarifications:

Teachers who encourage students to participate actively in effortful learning both individually and with others:

- Cultivate a community of growth mindset learners.
- Foster perseverance in students by choosing tasks that are challenging.
- Develop students' ability to analyze and problem solve.
- Recognize students' effort when solving challenging problems.

MA.K12.MTR.2.1 Demonstrate understanding by representing problems in multiple ways.

Mathematicians who demonstrate understanding by representing problems in multiple ways:

- Build understanding through modeling and using manipulatives.
- Represent solutions to problems in multiple ways using objects, drawings, tables, graphs and equations.
- Progress from modeling problems with objects and drawings to using algorithms and equations.
- Express connections between concepts and representations.
- Choose a representation based on the given context or purpose.

Clarifications:

Teachers who encourage students to demonstrate understanding by representing problems in multiple ways:

- Help students make connections between concepts and representations.
- Provide opportunities for students to use manipulatives when investigating concepts.
- Guide students from concrete to pictorial to abstract representations as understanding progresses.
- Show students that various representations can have different purposes and can be useful in different situations.



MA.K12.MTR.3.1 Complete tasks with mathematical fluency.

Mathematicians who complete tasks with mathematical fluency:

- Select efficient and appropriate methods for solving problems within the given context.
- Maintain flexibility and accuracy while performing procedures and mental calculations.
- Complete tasks accurately and with confidence.
- Adapt procedures to apply them to a new context.
- Use feedback to improve efficiency when performing calculations.

Clarifications:

Teachers who encourage students to complete tasks with mathematical fluency:

- Provide students with the flexibility to solve problems by selecting a procedure that allows them to solve efficiently and accurately.
- Offer multiple opportunities for students to practice efficient and generalizable methods.
- Provide opportunities for students to reflect on the method they used and determine if a more efficient method could have been used.

MA.K12.MTR.4.1 Engage in discussions that reflect on the mathematical thinking of self and others.

Mathematicians who engage in discussions that reflect on the mathematical thinking of self and others:

- Communicate mathematical ideas, vocabulary and methods effectively.
- Analyze the mathematical thinking of others.
- Compare the efficiency of a method to those expressed by others.
- Recognize errors and suggest how to correctly solve the task.
- Justify results by explaining methods and processes.
- Construct possible arguments based on evidence.

Clarifications:

Teachers who encourage students to engage in discussions that reflect on the mathematical thinking of self and others:

- Establish a culture in which students ask questions of the teacher and their peers, and error is an opportunity for learning.
- Create opportunities for students to discuss their thinking with peers.
- Select, sequence and present student work to advance and deepen understanding of correct and increasingly efficient methods.
- Develop students' ability to justify methods and compare their responses to the responses of their peers.



MA.K12.MTR.5.1 Use patterns and structure to help understand and connect mathematical concepts.

Mathematicians who use patterns and structure to help understand and connect mathematical concepts:

- Focus on relevant details within a problem.
- Create plans and procedures to logically order events, steps or ideas to solve problems.
- Decompose a complex problem into manageable parts.
- Relate previously learned concepts to new concepts.
- Look for similarities among problems.
- Connect solutions of problems to more complicated large-scale situations.

Clarifications:

Teachers who encourage students to use patterns and structure to help understand and connect mathematical concepts:

- Help students recognize the patterns in the world around them and connect these patterns to mathematical concepts.
- Support students to develop generalizations based on the similarities found among problems.
- Provide opportunities for students to create plans and procedures to solve problems.
- Develop students' ability to construct relationships between their current understanding and more sophisticated ways of thinking.

MA.K12.MTR.6.1 Assess the reasonableness of solutions.

Mathematicians who assess the reasonableness of solutions:

- Estimate to discover possible solutions.
- Use benchmark quantities to determine if a solution makes sense.
- Check calculations when solving problems.
- Verify possible solutions by explaining the methods used.
- Evaluate results based on the given context.

Clarifications:

Teachers who encourage students to assess the reasonableness of solutions:

- Have students estimate or predict solutions prior to solving.
- Prompt students to continually ask, "Does this solution make sense? How do you know?"
- Reinforce that students check their work as they progress within and after a task.
- Strengthen students' ability to verify solutions through justifications.



MA.K12.MTR.7.1 Apply mathematics to real-world contexts.

Mathematicians who apply mathematics to real-world contexts:

- Connect mathematical concepts to everyday experiences.
- Use models and methods to understand, represent and solve problems.
- Perform investigations to gather data or determine if a method is appropriate.
- Redesign models and methods to improve accuracy or efficiency.

Clarifications:

Teachers who encourage students to apply mathematics to real-world contexts:

- Provide opportunities for students to create models, both concrete and abstract, and perform investigations.
- Challenge students to question the accuracy of their models and methods.
- Support students as they validate conclusions by comparing them to the given situation.
- Indicate how various concepts can be applied to other disciplines.



Examples of Teacher and Student Moves for the MTRs

Below are examples that demonstrate the embedding of the MTRs within the mathematics classroom. The provided teacher and student moves are examples of how some MTRs could be incorporated into student learning and instruction. The information included in this table is not a comprehensive list, and educators are encouraged to incorporate other teacher and student moves that support the MTRs.

MTR	Student Moves	Teacher Moves
MA.K12.MTR.1.1 Actively participate in effortful learning both individually and collectively.	 Student asks questions to self, others and teacher when necessary. Student stays engaged in the task and helps others during the completion of the task. Student analyzes the task in a way that makes sense to themselves. Student builds perseverance in self by staying engaged and modifying methods as they solve a problem. 	 Teacher builds a classroom community by allowing students to build their own set of "norms." Teacher creates a culture in which students are encouraged to ask questions, including questioning the accuracy within a real-world context. Teacher chooses differentiated, challenging tasks that fit the students' needs to help build perseverance in students. Teacher builds community of learners by encouraging students and recognizing their effort in staying engaged in the task and celebrating errors as an opportunity for learning.
MA.K12.MTR.2.1 Demonstrate understanding by representing problems in multiple ways.	 Student chooses their preferred method of representation. Student represents a problem in more than one way and is able to make connections between the representations. 	 Teacher plans ahead to allow students to choose their tools. While sharing student work, teacher purposefully shows various representations to make connections between different strategies or methods. Teacher helps make connections for students between different representations (i.e., table, equation or written description).
MA.K12.MTR.3.1 Complete tasks with mathematical fluency.	• Student uses feedback from teacher and peers to improve efficiency.	• Teacher provides opportunity for students to reflect on the method they used, determining if there is a more efficient way depending on the context.



MTR	Student Moves	Teacher Moves
MA.K12.MTR.4.1 Engage in discussions that reflect on the mathematical thinking of self and others.	 Student effectively justifies their reasoning for their methods. Student can identify errors within their own work and create possible explanations. When working in small groups, student recognizes errors of their peers and offers suggestions. Student communicates mathematical vocabulary efficiently to others. 	 Teacher purposefully groups students together to provide opportunities for discussion. Teacher chooses sequential representation of methods to help students explain their reasoning.
MA.K12.MTR.5.1 Use patterns and structure to help understand and connect mathematical concepts.	 Student determines what information is needed and logically follows a plan to solve problems piece by piece. Student is able to make connections from previous knowledge. 	 Teacher allows for students to engage with information to connect current understanding to new methods. Teacher provides opportunities for students to discuss and develop generalizations about a mathematical concept. Teacher provides opportunities for students to develop their own steps in solving a problem.
MA.K12.MTR.6.1 Assess the reasonableness of solutions.	 Student provides explanation of results. Student continually checks their calculations. Student estimates a solution before performing calculations. 	 Teacher encourages students to check and revise solutions and provide explanations for results. Teacher allows opportunities for students to verify their solutions by providing justifications to self and others.
MA.K12.MTR.7.1 Apply mathematics to real-world contexts.	 Student relates their real-world experience to the context provided by the teacher during instruction. Student performs investigations to determine if a scenario can represent a real-world context. 	• Teacher provides real-world context in mathematical problems to support students in making connections using models and investigations.



Grade 6 Areas of Emphasis

In Grade 6, instructional time will emphasize five areas:

- (1) performing all four operations with integers, positive decimals and positive fractions with procedural fluency;
- (2) exploring and applying concepts of ratios, rates and percent to solve problems;
- (3) creating, interpreting and using expressions and equations;
- (4) extending geometric reasoning to plotting points on the coordinate plane, area and volume of geometric figures; and
- (5) extending understanding of statistical thinking.

The purpose of the areas of emphasis is not to guide specific units of learning and instruction, but rather provide insight on major mathematical topics that will be covered within this mathematics course. In addition to its purpose, the areas of emphasis are built on the following.

- Supports the intentional horizontal progression within the strands and across the strands in this grade level or course.
- Student learning and instruction should not focus on the stated areas of emphasis as individual units.
- Areas of emphasis are addressed within standards and benchmarks throughout the course so that students are making connections throughout the school year.
- Some benchmarks can be organized within more than one area.
- Supports the communication of the major mathematical topics to all stakeholders.
- Benchmarks within the areas of emphasis should not be taught within the order in which they appear. To do so would strip the progression of mathematical ideas and miss the opportunity to enhance horizontal progressions within the grade level or course.

The table below shows how the benchmarks within this mathematics course are embedded within the areas of emphasis.

		Operations with Integers, Positive Decimals and Positive Fractions	Ratios, Rates and Percentages	Expressions and Equations	Area and Volume of Geometric Figures and the Coordinate Plane	Statistical Thinking
S	MA.6.NSO.1.1	Х		Х	Х	Х
Operations	MA.6.NSO.1.2	Х				
rat	MA.6.NSO.1.3	Х				
pe	<u>MA.6.NSO.1.4</u>	Х			Х	
10	MA.6.NSO.2.1	Х	Х	Х	Х	Х
and	MA.6.NSO.2.2	Х	Х	Х	Х	Х
Se	MA.6.NSO.2.3	Х	Х	Х	Х	Х
Sen	MA.6.NSO.3.1	Х		х		
S.	MA.6.NSO.3.2	Х		Х		
Number Sense	MA.6.NSO.3.3	Х		Х	Х	
Iun	MA.6.NSO.3.4	Х		Х		
	MA.6.NSO.3.5	Х	Х	Х	Х	Х



		Operations with Integers, Positive Decimals and Positive Fractions	Ratios, Rates and Percentages	Expressions and Equations	Area and Volume of Geometric Figures and the Coordinate Plane	Statistical Thinking
	<u>MA.6.NSO.4.1</u>	Х		Х		
	MA.6.NSO.4.2	Х		Х		
	<u>MA.6.AR.1.1</u>		Х	Х	Х	Х
	<u>MA.6.AR.1.2</u>			х		
50	<u>MA.6.AR.1.3</u>	Х		Х		
ing	<u>MA.6.AR.1.4</u>	Х		х		
son	<u>MA.6.AR.2.1</u>	Х		х		
Algebraic Reasoning	<u>MA.6.AR.2.2</u>	Х		Х	Х	
c R	<u>MA.6.AR.2.3</u>	Х		Х	Х	
rai	MA.6.AR.2.4	Х	Х	Х	Х	
Geb	<u>MA.6.AR.3.1</u>		Х			
Alg	MA.6.AR.3.2	Х	Х			
1	MA.6.AR.3.3	Х	Х	х		
	<u>MA.6.AR.3.4</u>	Х	Х	Х		Х
	<u>MA.6.AR.3.5</u>	Х	Х	Х		
	<u>MA.6.GR.1.1</u>	Х			Х	
ວ່ວ	MA.6.GR.1.2	Х			Х	
itri ain	MA.6.GR.1.3	Х		Х	Х	
S01	MA.6.GR.2.1	Х		Х	Х	
Geometric Reasoning	<u>MA.6.GR.2.2</u>	Х		Х	Х	
	MA.6.GR.2.3	Х		х	Х	
	<u>MA.6.GR.2.4</u>	Х		Х	Х	
s y	<u>MA.6.DP.1.1</u>					Х
lysi ility	<u>MA.6.DP.1.2</u>	Х				Х
lan Jab	<u>MA.6.DP.1.3</u>	Х	Х			Х
a A 'rot	<u>MA.6.DP.1.4</u>					Х
Data Analysis & Probability	MA.6.DP.1.5	Х				Х
	MA.6.DP.1.6	Х		Х		Х



Number Sense and Operations

MA.6.NSO.1 Extend knowledge of numbers to negative numbers and develop an understanding of absolute value.

MA.6.NSO.1.1

Benchmark

MA.6.NSO.1.1	Extend previous understanding of numbers order and compare rational numbers.	to define rational numbers. Plot,
negative rational nu numbers when given <u><i>Clarification 2:</i></u> Wit	cations: hin this benchmark, the expectation is to plot, or mbers when given in the same form and to plot, or in different forms (fraction, decimal, percentage hin this benchmark, the expectation is to use sym enchmarks/Horizontal Alignment	order and compare positive rational e).
MA.6.ARMA.6.AR	O.4.1, MA.6.NSO.4.2 1.2 3.1, MA.6.AR.3.5 1.1, MA.6.GR.1.2, 1.3	 Integers Number Line Rational Number Whole Number

Vertical Alignment

Previous Benchmarks	Next]	Benchmarks
• MA.5.NSO.1.4	•	MA.7.NSO.1.2
http://flbt5.floridaearlylearning.com/standards.htm	l •	MA.8.NSO.1.1, MA.8.NSO.1.2

Purpose and Instructional Strategies

In grade 4, students plotted, ordered and compared fractions, including mixed numbers and fractions greater than one, with different numerators and different denominators. In grade 5, students plotted, ordered and compared multi-digit numbers with decimals up to the thousandths. In grade 6, students plot, order and compare on both sides of zero on the number line with all forms of rational numbers. Additionally, students will rewrite positive rational numbers in different but equivalent forms, which will extend to all rational numbers, including repeating decimals, in grade 7. In grade 8, students will plot, order and compare rational and irrational numbers.

Instruction builds on the understanding of numbers from elementary grades to include • rational numbers. Students should understand that rational numbers are part of a larger number system, the real numbers, and that numbers from previous learning are all rational numbers. The graphic below explains the types of numbers that make up the rational number system.





- Inequality is a comparison between two values. Students should connect the words to the symbols, for example, the symbol < reads "is less than" and the symbol > reads "is greater than."
- It can be helpful for students to think about placement of rational numbers on a number line using benchmark comparison values.
 - Examples of this could include the following questions: Between what two whole numbers does the rational number fall? Is it more than half or less than half way to the next whole number?
- Within the grade 6 benchmarks, students are only expected to convert between forms of positive rational numbers. When working with negative rational numbers, students are only expected to determine their relationship based on relative location to each other, as can be demonstrated on a number line.
- Having students read the comparison relationships from right to left and from left to right can help students develop flexibility of thinking and fluency with using the inequality symbols.
- When comparing negative rational numbers, it is helpful to reason through the comparisons using real-world scenarios (*MTR.7.1*).
 - For example, if a person owes \$12.47 and another person owes \$6.50, most students can quickly see and understand that -12.47 < -6.50 because the person owes more money would have less money.
- Students should be given opportunities to order rational numbers by notating as a list (as is often done with data sets) and by notating using inequality symbols.
 - For example, when ordering from least to greatest, the set could be written

as
$$-\frac{5}{8}$$
, -0.33, 2, 5.8 or as $-\frac{5}{8} < -0.33 < 2 < 5.8$.

• Instruction includes the use of technology to help define and explore rational numbers.



Common Misconceptions or Errors

- Students may think if a positive number is larger than a second positive number that the relationship will hold true given the negative or opposite of the given numbers.
 - For example, if given 6.75 > 6.71, then a student may think that -6.75 > -6.71. Using a number line (vertical or horizontal) can help students to see the relationship with whole numbers, meaning the greater value is always to the right (horizontal) or above (vertical).

This relationship also holds true with rational numbers. If students accurately plot the points they can determine which value is larger by looking at the position.

• Students may think that rational numbers cannot be compared unless they are in the same form (i.e., only fractions can be compared to fractions). Instruction should showcase how to make comparisons using benchmark values for plotting numbers without converting between forms.

Strategies to Support Tiered Instruction

- Instruction includes using a physical or digital number line where students can plot the values and see that the further to the left they move on the number line, the lesser the number.
- When comparing positive numbers in different forms, students may think they can order them just by looking, or that they cannot be compared since they are in different forms. Reviewing converting between fractions, decimals, and percent will help students in the comparing process.
- Teacher provides explanation of negative numbers (perhaps starting with integers) in terms of currency to help bring real-world connection to the standard. Students should know they would rather have someone owe them \$34 over someone owing them \$21. Similarly, they understand that if they owed someone \$6.25 (-6.25), that is less than owing them \$11.84 (-11.84). Then, using the number lines, students can begin to recognize patterns that will bridge their understanding from conceptual to procedural, as well as apply their understanding in real world situations.
- When plotting rational numbers, students should start by making assumptions and reasonable estimations.
 - For example, if a student is plotting $-4\frac{3}{5}$ on a number line, they need to know that $\frac{3}{5}$ is more than half. So, to graph this value, they should plot a point between -4 and -5, with the point closer to the -5. Then, the student can more precisely adjust the point if necessary if any other value is between -4 and -5.
- Instruction showcases how to make comparisons using benchmark values for plotting numbers without needing to convert between forms.



Instructional Tasks

Instructional Task 1 (MTR.1.1, MTR.4.1, MTR.5.1)

Provide students with an open number line and cards labeled with different rational numbers. Students may work together in groups or individual; if individual be sure to provide opportunities for students to discuss with a partner and as a whole group.

Part A. Arrange the cards on the number line.

Part B. Discuss your rationale for placement of rational numbers in your group or with a partner.

Part C. Compare your work and discuss whether you agree or disagree on rational number placement on the number line.

Instructional Task 2 (MTR.6.1, MTR.7.1)

Sharon was being paid to paint a mural on a wall in the gym. The mural was supposed to be at least 6.2 feet tall and 12.8 feet wide. When she measured her completed mural, the tape measure showed the height as $6\frac{1}{4}$ feet and the width as $12\frac{7}{8}$ feet. Did the dimensions of Sharon's mural meet the given requirements? How do you know?

Instructional Task 3 (MTR.2.1, MTR.4.1)

Cameron wrote on a quiz that $\frac{2}{3}$, $-\frac{6}{8}$ and $\frac{1}{9}$ are all rational numbers because they are written as fractions and that - 6, 12% and 4.333 are not rational numbers because they are not written as fractions. Is Cameron's answer correct? Explain your reasoning using a model to represent the situation.

Instructional Items

Instructional Item 1

Plot and label each of the following numbers on a number line: 3.4, $\frac{2}{3}$, 2.7, 7, $\frac{3}{4}$ and 1.

Instructional Item 2

Write the comparisons of $-\frac{1}{6}$ and $-\frac{1}{3}$ in more than one way using words and inequalities.

Instructional Item 3

Part A. Plot -5 and 5 on a number line.

Part B. Write a comparison that describes the relationship.

*The strategies, tasks and items included in the B1G-M are examples and should not be considered comprehensive.



MA.6.NSO.1.2

Benchmark Given a mathematical or real-world context, represent quantities that have MA.6.NSO.1.2 opposite direction using rational numbers. Compare them on a number line and explain the meaning of zero within its context.

Example: Jasmine is on a cruise and is going on a scuba diving excursion. Her elevations of 10 feet above sea level and 8 feet below sea level can be compared on a number line, where 0 represents sea level.

Benchmark Clarifications:

Clarification 1: Instruction includes vertical and horizontal number lines, context referring to distances, temperatures and finances and using informal verbal comparisons, such as, lower, warmer or more in debt.

Clarification 2: Within this benchmark, the expectation is to compare positive and negative rational numbers when given in the same form.

Connecting Benchmarks/Horizontal Alignment	Terms from the K-12 Glossary
• MA.6.NSO.4.1, MA.6.NSO.4.2	• Integers
• MA.6.AR.1.1, MA.6.AR.1.2	Number Line
• MA.6.GR.1.1, MA.6.GR.1.2,	Rational Number
MA.6.GR.1.3	Whole Number
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Vertical Alignment

Previous Benchmarks

Next Benchmarks MA.7.NSO.2.1

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This is the first introduction to the concept of numbers having opposites. http://flbt5.floridaearlylearning.com/standards.html

Purpose and Instructional Strategies

In elementary grades, students plotted, ordered and compared positive numbers. In grade 6, students plot, order and compare on both sides of zero on the number line with all forms of rational numbers. This benchmark focuses on the comparison of quantities with opposite directions (one positive and one negative) and understanding what the zero represents within the provided context. In grade 7, students will use the concept of opposites when solving problems involving order of operations and absolute value.

- A strong foundation in this skill can help students more efficiently solve problems • involving absolute value, finding the distance between points on a coordinate plane, combining rational numbers as well as assessing the reasonableness of solutions.
- Within this benchmark, it is the expectation that students make informal verbal comparisons of rational numbers using "is greater than" or "is less than" or another comparison within context.
 - For example, when comparing the temperature in Chipley, Florida, which is 34°F, to Minneapolis, Minnesota, which is -4° F, one could say that it is warmer in Florida than Minnesota or that it is colder in Minnesota than Florida.
- Students can describe the relative relationships between quantities and include the distance between the values in their description, as this is a way of connecting and reinforcing the MA.6.GR.1 standard (MTR.2.1, MTR.7.1).



For example, if a shark is 7.5 meters below sea level and a cliff diver is standing on a cliff at a point that is 22 meters from the surface of the water, the shark is 29.5 meters below the cliff diver. The shark's position can also be described as - 7.5 meters from the surface of the water if the surface of the water represents 0.

Common Misconceptions or Errors

- Students may incorrectly assign double negatives when describing relationships that are below zero.
 - For example, they may say the temperature is 3 degrees below zero when they mean it is 3 degrees from zero or it is 3 degrees below zero. In this same context, it is important for students to understand that identifying a value as negative indicates the position as being lower or colder than the neutral position of 0.
- Instruction provides many opportunities for students to share verbal descriptions (in written and oral forms) to better develop this skill (*MTR.4.1, MTR.7.1*).
- Students may experience difficulty when trying to create a number line and determining the meaning of 0 within the context. Instruction showcases drawing a picture of the context first and then connect it to the building of a number line.

Strategies to Support Tiered Instruction

- Instruction includes the use of a physical or digital number line to plot various values and to use their location on the number line to assist in comparing them. Instruction focuses on the generalization that the farther to the left a value is on the number line, the lesser the number.
- Teacher assists students with representing rational values in a real-world context, by first drawing a visual representation of the situation and labeling key features of the picture such as the "neutral" point of the visual (sea level, zero degrees, ground level, etc.), direction (above or below sea level, forward or backwards movement, etc.) and magnitude (the absolute value of the given quantity) of the given situation. Once a visual is drawn, the teacher or students create a corresponding horizontal or vertical number line to match the picture and the key features and then use the number line to write the correct rational number, paying close attention to the location of the point relative to zero.
 - For example, Jasmine is on a cruise and is going on a scuba diving excursion. Her elevations of 10 feet above sea level and 8 feet below sea level can be compared on a number line, where 0 represents sea level.



- Teacher provides opportunities for students to represent verbal descriptions of situations pictorially and on a number line. Students then restate the same situation using different vocabulary and check the reasonableness of the new situations by making connections back to the visual representation, number line, and meaning of zero in the context.
 - For example, Thomas's football team lost 3 yards in their first drive while Derrek's football team gained 5 yards in their first drive. The first drives for each



team can be compared on a number line, where 0 represents the line of scrimmag	e
for each play.	

Pict	ure	Meaning of Zero
Thomas × x o o × x o o × x o o x x o o	Derrek * x/0 * x/00 * x/00 x/00 x/0 x/0 x/0 x/0 x/0 x/0	The start of each first drive.
Numbe	er Line	Additional Description
тылас 2000 -4-3-2-10	Derech + + + + →→ + 2 3 4 5	The first drive of Thomas's football team can be represented by -3 and the first drive of Derrek's team can be represented by 5.

- Instruction includes providing students with opportunities to practice placing rational number cards on a provided number line. While placing the cards, students should share their thinking out loud while the teacher listens for reasonable estimations and assumptions for correct placement.
 - For example, if a student is placing a number card with $-4\frac{3}{5}$ on the number line,
 - the student needs to know that $\frac{3}{5}$ is more than half, so to place the card, the student should be between -4 and -5, with the point closer to the -5. As more cards are added to the number line, the students may adjust the placement of other cards, if necessary, for more accurate estimates.
- Teacher and students co-create a list of common terms from contextual situations that may be used to describe positive or negative values.
 - Examples of this could include:

Positive	Negative
Deposit	Withdrawal
Gain	Loss
Above	Below

Instructional Tasks

Instructional Task 1 (MTR.4.1, MTR.7.1)

On Thursday, Calvin borrowed \$46.68 from his mom to purchase a new video game. After mowing yards on the weekend he paid his mom back using the money he earned. Calvin had \$12.32 left to put in his wallet on Monday. What is the meaning of 0 in this situation? Compare the amounts of money that Calvin had on Thursday and Monday. Explain your reasoning including a number line in your justification.

Instructional Task 2 (MTR.5.1)

Part A. Given the inequality 7.2 > 4.5, describe how the numbers would be positioned relative to each other on a number line.

Part B. What role does 0 play in this context?

Part C. Using this reasoning, describe how any number x and any number y could be positioned relative to each other on a number line and the role played by 0.

Instructional Items



Instructional Item 1

New Orleans, Louisiana has an altitude of about $-6\frac{1}{2}$ feet and Miami, Florida has an altitude of about $6\frac{3}{5}$ feet. Compare the two altitudes on a vertical number line.

*The strategies, tasks and items included in the B1G-M are examples and should not be considered comprehensive.

MA.6.NSO.1.3

MA.6.NSO.1.3

Benchmark	
	Given a mathematical or real-world context, interpret the absolute value of a

number as the distance from zero on a number line. Find the absolute value of rational numbers.

Benchmark Clarifications:

Clarification 1: Instruction includes the connection of absolute value to mirror images about zero and to opposites.

Clarification 2: Instruction includes vertical and horizontal number lines and context referring to distances, temperature and finances.

Connecting Benchmarks/Horizontal Alignment	Terms from the K-12 Glossary
• MA.6.NSO.4.1, MA.6.NSO.4.2	Absolute Value
• MA.6.AR.1.1, MA.6.AR.1.2	• Integers
• MA.6.GR.1.1, MA.6.GR.1.2,	Number Line
MA.6.GR.1.3	Rational Number
_	Whole Number
Vertical Alignment	
Previous Benchmarks	Next Benchmarks
• This is the first introduction to the concept of	• MA.7.NSO.2.1

This is the first introduction to the concept of absolute value. http://flbt5.floridaearlylearning.com/standards.html



Purpose and Instructional Strategies

In elementary grades, students plotted positive numbers on a number line and related addition of positive numbers to distance on a number line. In grade 6, students determine the absolute values, both in the context of the distance from zero and determining the distance between two points on the coordinate plane with the same x- or y-coordinate. In grade 7, students will use the concept of opposites when solving problems involving order of operations and absolute value.

- Instruction includes developing the understanding that absolute value explains the magnitude of a real number without regard to its sign, and is denoted by |x| and reads "the absolute value of x."
- Absolute value in real-life situations can help students understand the concept of absolute value.
 - For example, distance is not depicted as a negative number; absolute value context should be used to describe a distance in the opposite direction. Students can draw pictures or diagrams, including vertical or horizontal number lines, to mathematically demonstrate what is happening in the real-life situation (*MTR.2.1*, *MTR.7.1*).
- Using sentence frames can help students describe relationships and reasoning with absolute value (*MTR.4.1*).
 - For example, when given the statement |x| = 6, students may benefit from a frame such as: The distance from x to 0 is _____, so x can be located at _____ or
- Instruction includes the use of technology to explore, interpret and define absolute value.

Common Misconceptions or Errors

- Students may incorrectly state the absolute value of a negative number has a negative value. Students need to understand the total distance you traveled is not dependent on which direction you travel. To help address this misconception, instruction includes students talking about absolute value as distance and asking students questions such as:
 - If your parent drives a car backwards, does the odometer show how far the car traveled by counting backwards?
 - If you walk from your desk to the door backwards (your back is facing the door), about how far would you walk?
 - You stand in line for a ride at an amusement park. You walk forward 10 feet in line then the line makes a U-turn and you walk 30 feet. A U-turn happens in the line again and you travel an additional 16 feet before boarding the ride. Do you subtract the distance when you travel the opposite direction in line, or do you still add it because you are still traveling over a specific distance?
 - Do you describe how far you traveled with a negative number because a person was walking or driving backwards?

Strategies to Support Tiered Instruction

- Instruction includes providing students with a sentence stem to interpret the meaning of the absolute value. Some students may require additional reading support.
 - For example, if given "If the temperature in Chicago, IL, is -7°, how many degrees below zero is the temperature?" the teacher can provide the sentence stem: "The absolute value of <u>-7</u> is <u>7</u> units from zero, so the temperature is <u>7</u> degrees below zero."



- Instruction includes providing students error analysis problems for which the absolute value of a positive number is incorrectly given as its opposite, rather than its distance from zero. Teacher reinforces the absolute value as the distance from zero and provides opportunities for students to plot the value on a number line and record the number of units the point is from zero. Instruction begins with integers and moves toward rational numbers.
- Teacher co-creates a graphic organizer with the students while providing instruction on the definitions of "absolute value," "opposite value," and "negative number." Instruction includes helping students to develop a definition in their own words, identify key characteristics, examples, and non-examples of each term.
- Teacher provides students with flash cards to practice and reinforce academic vocabulary.
- Instruction includes students talking about absolute value as distance and asking students questions such as:
 - If your parent drives a car backwards, does the odometer show how far the car traveled by counting backwards?
 - If you walk from your desk to the door backwards (your back is facing the door), about how far would you walk?
 - You stand in line for a ride at an amusement park. You walk forward 10 feet in line then the line makes a U-turn and you walk 30 feet. A U-turn happens in the line again and you travel an additional 16 feet before boarding the ride. Do you subtract the distance when you travel the opposite direction in line, or do you still add it because you are still traveling over a specific distance?
 - Do you describe how far you traveled with a negative number because a person was walking or driving backwards?

Instructional Tasks

Instructional Task 1 (MTR.4.1, MTR.5.1)

The absolute value of an unknown number is 11.2. Where could the unknown number be located on a number line? Explain how you know.

Instructional Task 2 (MTR.7.1)

The table below shows the change in rainfall for each month from the month's average over the past 5 years. Find the absolute value of each month and determine which month had the greatest change in rainfall.

Month	March	April	May	June	July
Change in Rainfall					
Amount from 5-Year	0.21	-1.64	-0.48	2.01	-2.30
Average (inches)					

Instructional Item 3 (MTR.3.1)

Plot 4, -4 and 0 on the same number line. Compare 4 and -4 in relation to 0. Part A. Plot 4, -4 and 0 on the same number line.

Part B. Compare 4 and -4 in relation to 0.

Instructional Items



Instructional Item 1

What is the value of the expression $\left|-\frac{7}{8}\right|$?

Instructional Item 2

If the temperature in Chicago, IL is -7° , how many degrees below zero is the temperature?

Instructional Item 3

What is the value of the expression -|12.75|?

*The strategies, tasks and items included in the B1G-M are examples and should not be considered comprehensive.

MA.6.NSO.1.4

Benchmark

Solve mathematical and real-world problems involving absolute value, **MA.6.NSO.1.4** including the comparison of absolute value.

Example: Michael has a lemonade stand which costs \$10 to start up. If he makes \$5 the first day, he can determine whether he made a profit so far by comparing |-10| and |5|.

Benchmark Clarifications:

Clarification 1: Absolute value situations include distances, temperatures and finances. *Clarification 2:* Problems involving calculations with absolute value are limited to two or fewer operations.

Clarification 3: Within this benchmark, the expectation is to use integers only.

Connecting Benchmarks/Horizontal Alignment	Terms from the K-12 Glossary
 MA.6.NSO.4.1, MA.6.NSO.4.2 MA.6.GR.1.1, MA.6.GR.1.2, MA.6.GR.1.3 	 Absolute Value Integers Number Line Rational Number
Vertical Alignment	• Whole Number

Previous Benchmarks

Next Benchmarks

MA.7.NSO.2.1

This is the first introduction to the concept of absolute value.

http://flbt5.floridaearlylearning.com/standards.html

Purpose and Instructional Strategies

In elementary grades, students plotted positive numbers on a number line and related addition of positive numbers to distance on a number line. In grade 6, students determine and compare absolute values. In grade 7, students will use the concept of opposites when solving problems involving order of operations and absolute value.

• All values within this benchmark are limited to integers since students do not perform operations on negative rational numbers until grade 7.



- Instruction includes making connections in absolute value problems to direction and distance, or speed. This benchmark connects to finding the distance between two points on a coordinate plane with the same *x* or *y*-coordinate.
- Instruction within absolute value contexts are not limited to distances, temperature and finances. Other situations could arise from a predetermined amount, or zero point, and then measuring above or below that amount (*MTR.7.1*).
 - For example, Leah eats on average 1200 calories in a day. On Wednesday, her caloric intake was 400 calories different than her average. What are her possible caloric intakes on Wednesday?
- Students should progress from solving problems using a concrete number line to solving problems abstractly. Students should represent equations with a visual model to illustrate their thinking. This will allow for students to solidify the abstract concept through a pictorial representation. When students understand both methods and how they connect, students are often able to think more flexibly and reason through challenging problems successfully (*MTR.2.1, MTR.5.1*).
- Instruction includes the use of technology, including calculators.

Common Misconceptions or Errors

- Students may incorrectly state the absolute value of a negative number has a negative value. Instruction includes opportunities for students to talk about absolute value as distance in real-world scenarios (*MTR.7.1*).
 - For example, the odometer on my car reads 92,500 miles when I leave my house to drive 89 miles to Grandma's house. When I get to Grandma's house, the odometer reads 92,589 miles. When I turn around and drive home, which is the opposite direction, will my odometer count backwards and read 92,500 again when I get home, or will it read 92,678 miles?
- Students may incorrectly assume distance is only referring to physical traveling between locations, such as walking, biking or driving. However, if we plot two values on a number line, this can also represent distance because we are determining how far away two points or values are from each other (*MTR.3.1*).



Strategies to Support Tiered Instruction

- Teacher provides instruction to reinforce the concept of absolute value being the distance of a number from zero.
 - For example, students plot integer values that represents temperature on a number line and then record the number of units from zero.
- Teacher provides instruction for utilizing the absolute value symbols within the order of operations and refers to them as groups symbols.
 - For example, when evaluating -|6|, first apply the absolute value of 6, then apply the factor of -1 to result in a solution of -6, so that

$$-|6| = (-1)(|6|)$$

= (-1)(6)
= -6.

• Instruction for comparing absolute values of integers includes the use of pictorial representations or number lines to model the comparison and the use of key features of the model to discuss the problem, using contextual language when provided.

Instructional Tasks

Instructional Task 1 (MTR.2.1, MTR.7.1)

On March 1, Mr. Lopez weighed 187 pounds. This was 12 pounds different than he weighed on January 1. On January 1, Mr. Lopez weighed 25 pounds different than the preceding October 1. What might Mr. Lopez have weighed on October 1? Explain why this question could have multiple answers.

Instructional Items

Instructional Item 1

The Philippine Trench is located 10,540 meters below sea level and the Tonga Trench is located 10,882 meters below sea level. Which trench has the higher altitude and by how many meters?

Instructional Item 2

What is the value of the expression 7 - |-3|?

*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.



MA.6.NSO.2 Add, subtract, multiply and divide positive rational numbers.

MA.6.NSO.2.1

Benchmark				
	N F 1 1 1	 • .•	1, 1, 1, 1,	

MA.6.NSO.2.1 Multiply and divide positive multi-digit numbers with decimals to the thousandths, including using a standard algorithm with procedural fluency.

Benchmark Clarifications:

Clarification 1: Multi-digit decimals are limited to no more than 5 total digits.

Connecting Benchmarks/Horizontal Alignment	Terms from the K-12 Glossary
• MA.6.NSO.3.3	Area Model
• MA.6.AR.1.1	Commutative Property
• MA.6.AR.2.4	of Multiplication
• MA.6.AR.3	 Expression
• MA.6.GR.2	 Dividend
• MA.6.DP.1.2, MA.6.DP.1.3,	• Divisor
MA.6.DP.1.4	

Next Benchmarks

Vertical Alignment

Previous Benchmarks

 MA.5.NSO.2.1, MA.5.NSO.2.2, MA.5.NSO.2.4,
 MA.5.NSO.2.5 http://flbt5.floridaearlylearning.com/standards.html

Purpose and Instructional Strategies

In grade 5, students multiplied and divided multi-digit whole numbers and represented remainders as fractions. They also estimated and determined the product and quotient of multi-digit numbers with decimals to the hundredths and multiplied and divided the product and quotient of multi-digit numbers with decimals to the hundredths by one-tenth and one-hundredth with procedural reliability. In grade 6, students multiply and divide positive rational numbers with procedural fluency, including dividing numerators by denominators to rewrite fractions as decimals. In grade 7, students will become fluent in all operations with positive and negative rational numbers.

- Instruction includes representing multiplication in various ways.
 - \circ 3.102 × 1.1 = 3.4122
 - \circ (3.102)(1.1) = 3.4122
 - \circ 3.102(1.1) = 3.4122
 - \circ 3.102 · 1.1 = 3.4122
- Students should continue demonstrating their understanding from grade 5 that division can be represented as a fraction.
- A standard algorithm is a systematic method that students can use accurately, reliably and efficiently (no matter how many digits) depending on the content of the problem. It is not the intention to require students to use a standard algorithm all of the time. However,



students are expected to become fluent with a standard algorithm by certain grade levels as stated within the benchmarks.

- Instruction includes a variety of methods and strategies to multiply and divide multi-digit numbers with decimals.
 - o Area Models

$3.102 \times 1.1 = 3.4122$					
	3	.1	0.00	.002	
	0.3	.01	0.000	.0002	

• Partial Products

3.102
<u>× 1.1</u>
0.3102
+ 3.1020
3.4122

• Multiplying as if the factors are whole numbers and applying the decimal places to the final product based on the number of decimals represented in the factors (*MTR.3.1*).

3.102 <u>× 1.1</u>	$\xrightarrow{3102} \\ \times 11 \\ 3102 $	4 decimal places in factors 3.4122
	<u>+ 31020</u>	
	34122	

• Students should develop fluency with and without the use of a calculator when performing operations with positive decimals.

Common Misconceptions or Errors

- Students may incorrectly apply rules for adding or subtracting decimals to multiplication of decimals, believing place values must be aligned.
- Students may confuse the lining up of place values when multiplying or dividing vertically by omitting or forgetting to include zeros as place holders in the partial products or quotients.

Strategies to Support Tiered Instruction

- Instruction includes the use of estimation to ensure the proper placement of the decimal point in the final product or quotient of decimals.
 - For example, if finding the product of 12.3 and 4.8, students should estimate the product to be close to 60, by using 12 and 5 as friendly numbers, then apply the decimal to the actual product of 123 and 48, which is 5904. Based on the estimate, the decimal should be placed after 59 to produce 59.04.
- Teacher encourages and allows for students who have a firm understanding of multiplying and dividing fractions to convert the provided decimal values to their equivalent fractional form before performing the desired operation and converting the solution back to decimal form.
- Teacher provides graph paper to utilize while applying an algorithm for multiplying or dividing to keep numbers lined up and help students focus on place value.



• Instruction includes providing opportunities to reinforce place values with the use of base ten blocks or hundredths grids.

Instructional Tasks

Instructional Task 1 (MTR.6.1)

Carlos spent \$20.76 on chips when his friends came over. Each bag of chips cost \$3.46 and each bag has 3 servings. What is the maximum number of friends that Carlos can have over if each person can have a single serving of chips?

Instructional Task 2 (MTR.7.1)

Samantha has 6.75 bags of candy. A full bag of candy contains 13.125 ounces of candy. How many ounces of candy does Samantha have?

Instructional Task 3 (MTR.4.1, MTR.5.1)

Part A. Complete the table below using a calculator.

Expression	Solution	Expression	Solution
559(5)		5.59(5)	
325(25)		3.25(2.5)	
19(93)		19(9.3)	

Part B. Talk with a partner about what you notice from the table in Part A.

Part C. How are the expressions without decimals related to the expressions with decimals? Is there a relationship between the decimal placements in the expressions and the solutions?

Part D. If 2368(421) = 996,928, what would you expect 2.368(4.21) be equal to?

Instructional Items

Instructional Item 1

Determine the product of 23.5 and 2.3.

Instructional Item 2

The expression $13.31 \div 0.125$ is equivalent to what number?

Instructional Item 3

Determine the quotient of 201.3 and 1.83.

Instructional Item 4

The expression 4.321×2.3 is equivalent to what number?

*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.



MA.6.NSO.2.2

BenchmarkMA.6.NSO.2.2Extend previous understanding of multiplication and division to compute
products and quotients of positive fractions by positive fractions, including
mixed numbers, with procedural fluency.

Benchmark Clarifications:

Clarification 1: Instruction focuses on making connections between visual models, and the relationship between multiplication and division, reciprocals and algorithms.

Connecting Benchmarks/Horizontal Alignment	Terms from the K-12 Glossary
• MA.6.NSO.3.3	Area Model
• MA.6.AR.1.1	Commutative Property
• MA,6.AR.3	• Dividend
• MA.6.GR.2	Divisor
• MA.6.DP.1.2, MA.6.DP.1.3,	 Expression
MA.6.DP.1.4	

Vertical Alignment Previous Benchmarks

Next Benchmarks

•

MA.7.NSO.2.2

 MA.5.FR.2.2, MA.5.FR.2.4 <u>http://flbt5.floridaearlylearning.com/standards.html</u>

Purpose and Instructional Strategies

In grade 5, students multiplied fractions by fractions with procedural reliability and explored how to divide a unit fraction by a whole number and a whole number by a unit fraction. In grade 6, students become procedurally fluent with multiplication and division of positive fractions. The expectation is to utilize skills from the procedural reliability stage to become fluent with an efficient and accurate procedure, including a standard algorithm. In grade 7, students will become fluent in all operations with positive and negative rational numbers.

• Instruction includes making connections to the distributive property when multiplying fractions.

• For example, when multiplying $1\frac{1}{2}$ by $\frac{3}{4}$, it can be written as $\left(1+\frac{1}{2}\right)\frac{3}{4}$ to determine $\frac{9}{8}$ as the product.

- Instruction includes making connections to inverse operations when multiplying or dividing fractions.
 - For example, when determining $\frac{3}{4} \div \frac{5}{8}$, students can write the equation $x\left(\frac{5}{8}\right) = \frac{3}{4}$ and then solve for x.
- Instruction focuses on appropriate academic vocabulary, such as reciprocal. Avoid focusing on tricks such as "keep-change-flip." Using academic language and procedures allow for students to connect to future mathematics (*MTR.5.1*).
 - For example, $\frac{3}{4} \div \frac{5}{8}$ can be read as "How many five-eighths are in three-fourths?"



• Instruction includes using concrete and pictorial models, writing a numerical sentence that relates to the model and discovering the pattern or rules for multiplying and dividing fractions by fractions (*MTR.2.1, MTR.3.1, MTR.5.1*).



- Instruction includes providing opportunities for students to analyze their own and others' calculation methods and discuss multiple strategies or ways of understanding with others (*MTR.4.1*).
- Students should develop fluency with and without the use of a calculator when performing operations with positive fractions.

Common Misconceptions or Errors

- Students may forget that common denominators are not necessary for multiplying or dividing fractions.
- Students may have incorrectly assumed that multiplication results in a product that is larger than the two factors. Instruction continues with students assessing the reasonableness of their answers by determining if the product will be greater or less than the factors within the given context.
- Students may have incorrectly assumed that division results in a quotient that is smaller than the dividend. Instruction continues with students assessing the reasonableness of their answers by determining if the quotient will be greater or less than the dividend within the given context.



Strategies to Support Tiered Instruction

- Teacher encourages and allows for students who have a firm understanding of multiplying and dividing decimals to convert the provided fractional values to their equivalent decimal form before performing the desired operation and converting the solution back to fractional form.
- Instruction includes the use of fraction tiles, fraction towers, or similar manipulatives to make connections between physical representations and algebraic methods.
- Instruction includes the co-creation of a graphic organizer utilizing the mnemonic device Same, Inverse Operation, Reciprocal (S.I.R.) for dividing fractions, which encourages the use of correct mathematical terminology, and including examples of applying the mnemonic device when dividing fractions, whole numbers, and mixed numbers.
- Teacher provides students with flash cards to practice and reinforce academic vocabulary.
- Instead of multiplying by the reciprocal to divide fractions, an alternative method could include rewriting the fractions with a common denominator and then dividing the numerators and the denominators.
 - For example, $\frac{5}{6} \div \frac{3}{2}$ is equivalent to $\frac{5}{6} \div \frac{9}{6}$ which is equivalent to $\frac{5/9}{1}$ which is equivalent to $\frac{5}{9}$.
- Instruction provides opportunities to assess the reasonableness of answers by determining if the product will be greater or less than the factors within the given context.
- Instruction provides opportunities to assess the reasonableness of answers by determining if the quotient will be greater or less than the dividend within the given context.

Instructional Tasks

Instructional Task 1 (MTR.2.1, MTR.4.1)

Jasmine wants to build a $2\frac{5}{6}$ meters long garden path paved with square stones that measure $\frac{1}{4}$ meter on each side. There will be no spaces between the stones.

Part A. Create a model that could be used to answer the following question: How many stones are needed for the path?

Part B. How many stones are needed for the path?

Instructional Task 2 (MTR.3.1, MTR.6.1)

A container at a juicing plant holds $6\frac{2}{3}$ tons of oranges. The plant can juice $1\frac{1}{2}$ tons of oranges per day. At this rate, how long will it take to empty the container?

Instructional Task 3 (MTR.2.1)

Explain using visual models why $\frac{4}{5} \times \frac{2}{3} = \frac{8}{15}$.



Instructional Items

Instructional Item 1

What is the value of the expression $\frac{3}{5} \div \frac{5}{8}$?

Instructional Item 2

What is the value of the expression $8\frac{1}{10} \div \frac{5}{8}$?

*The strategies, tasks and items included in the B1G-M are examples and should not be considered comprehensive.

MA.6.NSO.2.3

Benchmark

MA.6.NSO.2.3 Solve multi-step real-world problems involving any of the four operations with positive multi-digit decimals or positive fractions, including mixed numbers.

Benchmark Clarifications:

Clarification 1: Within this benchmark, it is not the expectation to include both decimals and fractions within a single problem.

Connecting Benchmarks/Horizontal Alignment	Terms from the K-12 Glossary
• MA.6.AR.1.1	Area Model
• MA.6.AR.2.4	• Commutative property of
• MA.6.AR.3.2, MA.6.AR.3.3,	Multiplication
MA.6.AR.3.4, MA.6.AR.3.5	• Dividend
• MA.6.GR.2	Divisor
• MA.6.DP.1.2, MA.6.DP.1.3,	Expression
MA.6.DP.1.4, MA.6.DP.1.6	
Vertical Alignment	

Next Benchmarks

• MA.7.NSO.2.3

Vertical Alignment Previous Benchmarks

- MA.5.AR.1.1, MA.5.AR.1.2, MA.5.AR.1.3
- MA.5.M.2.1
- MA.5.GR.2.1

http://flbt5.floridaearlylearning.com/standards.html

Purpose and Instructional Strategies

In grade 5, students solved multi-step real-world problems involving the four operations with whole numbers as well as addition, subtraction and multiplication for solving real-world problems with fractions and for solving problems with decimals involving money, area and perimeter. In grade 6, students solve multi-step real-world problems with positive fractions and decimals. In grade 7, students will solve real-world problems involving any of the four operations with positive and negative rational numbers.

• This benchmark is the culmination of MA.6.NSO.2. It is built on the skills found in MA.6.NSO.2.1 and MA.6.NSO.2.2, so instruction provides practice of these skills within the real-world contexts (*MTR.5.1*, *MTR.7.1*).



- Instruction includes engaging in questions such as:
 - What do you know from the problem?
 - What is the problem asking you to find?
 - Are you putting groups together? Taking groups apart? Or both?
 - Are the groups you are working with the same sizes or different sizes?
 - Can you create a visual model to help you understand or see patterns in your problem?
- With the completion of operations with positive rational numbers in grade 6, students should have experience using technology with decimals and fractions as they occur in the real world (*MTR.7.1*). This experience will help to prepare students working with all rational numbers in grade 7 and with irrational numbers in grade 8.

Common Misconceptions or Errors

- Students may incorrectly oversimplify a problem by mechanically circling the numbers, underlining the question, and boxing in key words and then jumping to an answer, or procedure, without taking the time to comprehend the context or situation (*MTR.2.1*, *MTR.4.1*, *MTR.5.1*, *MTR.7.1*).
- Students may incorrectly apply rules for adding or subtracting decimals to multiplication of decimals, believing place values must be aligned.
- Students may confuse the lining up of place values when multiplying or dividing vertically by omitting or forgetting to include zeros as place holders in the partial products or quotients.
- Students may forget that common denominators are not necessary for multiplying or dividing fractions.
- Students may have incorrectly assumed that multiplication results in a product that is larger than the two factors. Instruction continues with students assessing the reasonableness of their answers by determining if the product will be greater or less than the factors within the given context.
- Students may have incorrectly assumed that division results in a quotient that is smaller than the dividend. Instruction continues with students assessing the reasonableness of their answers by determining if the quotient will be greater or less than the dividend within the given context.

Strategies to Support Tiered Instruction

- Instruction includes using visual models to illustrate and make meaning of situations represented in word problems.
- Instruction includes the use of estimation to ensure the proper placement of the decimal point in the final product or quotient of decimals.
 - For example, if finding the product of 12.3 and 4.8, students should estimate the product to be close to 60, by using 12 and 5 as friendly numbers, then apply the decimal to the actual product of 123 and 48, which is 5904. Based on the estimate, the decimal should be placed after 59 to produce 59.04.
- Teacher provides opportunities for students who have a firm understanding of multiplying and dividing fractions to convert the provided decimal values to their equivalent fractional form before performing the desired operation and converting the solution back to decimal form.



- Teacher provides opportunities for students who have a firm understanding of multiplying and dividing decimals to convert the provided fractional values to their equivalent decimal form before performing the desired operation and converting the solution back to fractional form.
- Teacher provides opportunities for students to comprehend the context or situation by engaging in questions such as:
 - What do you know from the problem?
 - Can you create a visual model to help you understand or see patterns in your problem?
- Teacher provides graph paper to utilize while applying an algorithm for multiplying or dividing to keep numbers lined up and help students focus on place value.
- Instruction includes providing opportunities to reinforce place values with the use of base ten blocks or hundredths grids.
- Instruction includes the co-creation of a graphic organizer utilizing the mnemonic device S.I.R. (Same, Inverse Operation, Reciprocal) for dividing fractions, which encourages the use of correct mathematical terminology, and including examples of applying the mnemonic device when dividing fractions, whole numbers, and mixed numbers.
- Teacher provides students with flash cards to practice and reinforce academic vocabulary.
- Instead of multiplying by the reciprocal to divide fractions, an alternative method could include rewriting the fractions with a common denominator and then dividing the numerators and the denominators.
 - For example, $\frac{5}{6} \div \frac{3}{2}$ is equivalent to $\frac{5}{6} \div \frac{9}{6}$ which is equivalent to $\frac{5/9}{1}$ which is equivalent to $\frac{5}{9}$.
- Instruction includes the use of a three-read strategy. Students read the problem three different times, each with a different purpose.
 - First, read the problem with the purpose of answering the question: What is the problem, context, or story about?
 - Second, read the problem with the purpose of answering the question: What are we trying to find out?
 - Third, read the problem with the purpose of answering the question: What information is important in the problem?
- Instruction provides opportunities to assess the reasonableness of answers by determining if the product will be greater or less than the factors within the given context.
- Instruction provides opportunities to assess the reasonableness of answers by determining if the quotient will be greater or less than the dividend within the given context.



Instructional Tasks

Instructional Task 1 (MTR.3.1, MTR.6.1)

Janie is at the gas station. She has \$53.25 and buys a sandwich that costs \$7.68 and a drink for \$0.97.

Part A. After she buys the sandwich and drink, how much money will Janie have left?

Part B. Janie wants to buy 10 gallons of gas with the remaining money. What is the highest price per gallon that she can afford? Use words or numbers to show your work.

Instructional Items

Instructional Item 1

Candy comes in $3\frac{1}{2}$ pound bags. At a class party, the boys in the class ate $2\frac{1}{4}$ bags of candy and the girls in the class ate $1\frac{1}{3}$ bags. How many pounds of candy did the class eat?

Instructional Item 2

Tina's SUV holds 18.5 gallons of gasoline. If she has 4.625 gallons in her car when she stops to fill it up. How much money will she spend to fill up her car if the current price for gas is \$2.57 per gallon?

*The strategies, tasks and items included in the B1G-M are examples and should not be considered comprehensive.

MA.6.NSO.3 Apply properties of operations to rewrite numbers in equivalent forms.

MA.6.NSO.3.1

Benchmark	
MA.6.NSO.3.1	Given a mathematical or real-world context, find the greatest common factor and least common multiple of two whole numbers.
Example.	• Middleton Middle School's band has an upcoming winter concert which will have several performances. The bandleader would like to divide the students into concert groups with the same number of flute players, the same number of clarinet players and the same number of violin players in each group. There are a total of 15 students who play the flute, 27 students who play the clarinet and 12 students who play the violin. How many separate groups can be formed?
Example.	Adam works out every 8 days and Susan works out every 12 days. If both Adam and Susan work out today, how many days until they work out on the same day again?

Benchmark Clarifications:

Clarification 1: Within this benchmark, expectations include finding greatest common factor within 1,000 and least common multiple with factors to 25.

Clarification 2: Instruction includes finding the greatest common factor of the numerator and denominator of a fraction to simplify the fraction.

Connecting Benchmarks/Horizontal Alignment	Terms from the K-12 Glossary
• MA.6.NSO.2.2, MA.6.NSO.2.3	Area Model
• MA.6.AR.1.4	Composite Number
FLORIDA DEPARTMENT OF	35 Page



• MA.6.AR.3.2, MA.6.AR.3.3,	Dividend
MA.6.AR.3.4, MA.6.AR.3.5	Divisor
	• Factor
	Greatest Common
	Factor (GCF)
	Least Common Multiple
	(LCM)
	Prime Factorization
	Prime Number
_	Rectangular Array
Vertical Alignment	
Previous Benchmarks	Next Benchmarks

revious benchmarks		text Deneminal KS	
٠	MA.4.AR.3.1	٠	MA.7.NSO.2.2
	http://flbt5.floridaearlylearning.com/standards.html	•	MA.7.AR.1.2

Purpose and Instructional Strategies

In grade 4, students determined factor pairs for whole numbers from 0 to 144 and determined if numbers are prime, composite, or neither. In grade 6, students will determine the least common multiple and greatest common factor of two whole numbers. In future grades, students will use their understanding of factors, factorization and the distributive property to generate equivalent expressions and solve equations.

- Instruction includes a variety of methods and strategies to determine the least common multiple (*MTR.2.1, MTR.3.1, MTR.5.1*).
 - Multiple listing method

6	6, 12, 18, 24,30
15	15,30

Factorization

LCM is represented as $2 \times 3 \times 5$.

6	2 × 3
15	<u>3</u> × 5

- Instruction includes a variety of methods and strategies to determine the greatest common factor (*MTR.2.1*, *MTR.3.1*, *MTR.5.1*).
 - T-charts



The greatest common factor of 96 and 138 is 6.

• Factorization

GCF is represented as 3.


6	2 × 3
15	<u>3</u> × 5

• The greatest common factor can be determined by dividing the numbers multiple times by common factors and then multiplying the common factors that were used as divisors.



The greatest common factor of 75 and 150 can be found by multiplying $5 \times 3 \times 5 = 75$.

$$\frac{75}{150} \div \frac{75}{75} = \frac{1}{2}$$

Instruction includes the use of technology to explore, interpret and define greatest common factors and least common factors.

Common Misconceptions or Errors

- Greatest common factor and least common multiple are often mixed up or confused by students. Stressing the academic vocabulary of what is a factor versus what is a multiple can help students keep the two straight in their minds.
- Students may incorrectly think that the greatest common factor of two numbers cannot be 1. However, if given two prime numbers, the greatest common factor will always be 1.
- Students may incorrectly think that if one of the numbers is prime, the greatest common factor must be 1. However, the greatest common factor is not 1 if one of the numbers is a prime number and that prime number is a factor of the second number.
- Students may incorrectly think the least common multiple has to be larger than both of the given numbers. Provide examples to showcase the least common multiple being the same as one of the given whole numbers.
 - For example, the LCM of 12 and 24 is 24.
- Students may incorrectly think the least common multiple can be found by multiplying the two numbers. Provide examples where this is not the case, such as the LCM of 4 and 6 is 12 not 24.

Strategies to Support Tiered Instruction

- Teacher shares their thinking when determining if a given situation requires finding the greatest common factor or the least common multiple. Steps include reading the given context out loud and thinking out loud about if the context requires the final answer to be greater than or equal to the given numbers (least common multiple) or less than the given numbers (greatest common factor).
- Teacher creates and posts an anchor chart with visual representations of factors and multiples and encourages students to utilize the anchor chart to assist in utilizing correct academic vocabulary when referring to factors and multiples.
 - Example:





- Teacher provides students with flash cards to practice and reinforce academic vocabulary.
- Teacher provides instruction on the definitions of greatest common factor and least common multiple then co-creates a graphic organizer using student created definitions, lists of key characteristics, examples, and non-examples of each term.
 - A non-example for greatest common factor might include finding a least common factor, which would result in 1.
 - A non-example for least common multiple might include attempting to find the greatest common multiple, which cannot be determined because multiples are infinite.
- Teacher provides examples to showcase the least common multiple being the same as the larger of the given whole numbers or the same as the product of the two numbers.
 - For example, the least common multiple of 12 and 24 is 24.
 - \circ For example, the least common multiple of 14 and 5 is 70.
- Teacher provides examples where this is not the case, such as the least common multiple of 4 and 6 is 12 not 6 or 24.
- Instruction includes the use of a graphic organizer to compare the multiples or factors of two numbers to help recognize common multiples and factors.

Instructional Tasks

Instructional Task 1 (MTR.3.1)

Parker reads a book every 12 days and Leah reads a book every 8 days.

Part A. If today is Wednesday and they both started a book today, how many days will it be when they both start a new book on the same day?

Part B. What day of the week will it be when they both start a new book on the same day?

Instructional Items

Instructional Item 1

What is the greatest common factor between 636 and 132?

Instructional Item 2

What is the least common multiple between 17 and 12?

*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.

MA.6.NSO.3.2



MA.6.NSO.3.2 Rewrite the sum of two composite whole numbers having a common factor, as a common factor multiplied by the sum of two whole numbers.

Benchmark Clarifications:

Clarification 1: Instruction includes using the distributive property to generate equivalent expressions.Connecting Benchmarks/Horizontal AlignmentTerms from the K-12

	Glossary
• MA.6.AR.1.4	Area Model
	Composite Number
	• Factor
	Greatest Common
	Factor (GCF)
	Prime Number
_	Rectangular Array
Vertical Alignment	

Previous Benchmarks

Next Benchmarks

• MA.7.AR.1.2

- MA.4.AR.3.1
- MA.5.NSO.2.1, MA.5.NSO.2.2 http://flbt5.floridaearlylearning.com/standards.html

Purpose and Instructional Strategies

In grade 4, students determined factor pairs for whole numbers from 0 to 144 and determined if numbers are prime, composite, or neither. In grade 5, students multiplied and divided using products and divisors greater than 144. In future grades, students will use their understanding of factors, factorization, and the distributive property to generate equivalent expressions and solve equations.

- This benchmark builds upon student understanding of the distributive property and supports the decomposition of numbers in earlier grades and extends to future learning in algebraic reasoning in future grade levels.
- Students should not be using the multiplication symbol "×" when rewriting composite numbers as a common factor multiplied by the sum of two whole numbers. In grade 3, students have seen the multiplication symbol "×" when using the distributive property. Students should move away from this practice in grade 6 to writing the common factor directly outside the parentheses with an understanding that a number directly next to parentheses means you multiply (*MTR.3.1*).
 - For example, 24 + 12 = 6(4 + 2).
- Instruction includes the use of manipulatives, models, drawings and equations to rewrite the sum.
- If two numbers have multiple common factors, there will be multiple equivalent common factors multiplied by the sum of two whole number possibilities (*MTR.2.1, MTR.5.1*).
 - For example the equations below are equivalent:
 - 42 + 96 = 2(21 + 48) 42 + 96 = 3(14 + 32) 42 + 96 = 6(7 + 16)
- Provide opportunities for students to identify the common factor and the factors to sum in the parenthesis as well as given the common factor multiplied by the sum of two whole numbers and determine the two composite whole numbers to be summed.
- For this benchmark, all terms are numerical, not algebraic.
- Students should use their basic multiplication facts to do this benchmark and think



through number relationships and patterns (MTR.5.1).

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Common Misconceptions or Errors

- When working with the distributive property, some students may incorrectly multiply only the common factor by only one of the terms inside the parenthesis. Students need to make sure to multiply the common factor by both terms in the parentheses.
- Students may incorrectly think that they always must factor out the greatest common factor from the addends, but is not necessarily the case. Students must read the task or question carefully to determine if any common factor is allowable or if it must be the greatest common factor.

Strategies to Support Tiered Instruction

- Instruction includes the use of area models to visually represent an application of the distributive property.
 - Teacher provides review of prior knowledge of the distributive property using an area model. For example, the teacher can begin with the expression 5(2 + 3) and the area model below.



Then the teacher can co-construct the area model to demonstrate the distributive property.

$$5(2+3) = 10 + 15$$
2
3
10
15
a on area model to determine

 \circ Teacher models using an area model to determine a common factor. For example, the teacher can begin with the expression 9 + 21 and the area model below.



Then the teacher can co-construct the area model to determine a common factor. 9 + 21 = 3(3 + 7)

	3	7
3	9	21
1:	a atradanta n	with in a small stars an

• Instruction includes providing students with incomplete area models they must complete and use to write equivalent expressions.

Instructional Tasks

Instructional Task 1 (MTR.3.1, MTR.4.1)

Rewrite 121 + 66 in the form a(b + c) where *a* is the greatest common factor of 121 and 66 and *b* and *c* are whole numbers. Does your expression have the same value as 121 + 66? Justify your thinking.

Instructional Items

Instructional Item 1

Rewrite the following numerical expression in an equivalent form using the distributive property: 24 + 36.

*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.



MA.6.NSO.3.3

Benchmark

MA.6.NSO.3.3 Evaluate positive rational numbers and integers with natural number exponents.

Benchmark Clarifications:

Clarification 1:	Within	this bench	mark, e	expectations	include using	g natural r	number exp	ponents up to 5.

Connecting Benchmarks/Horizontal Alignment	Terms from the K-12
	Glossary
• MA.6.NSO.2.1, MA.6.NSO.2.2	• Base (of an exponent)
• MA.6.NSO.4.2	 Expression
• MA.6.AR.1.3	• Exponents
• MA.6.GR.2.3	• Factors
	• Integers
	Rational Number
Vertical Alignment	
Previous Benchmarks N	lext Benchmarks
• MA.5.NSO.2.1, MA.5.NSO.2.4	• MA.7.NSO.1.1
• MA.5.FR.2.2	• MA.7.NSO.2.1
http://flbt5.floridaearlylearning.com/standards.html	

Purpose and Instructional Strategies

In grade 5, students multiplied multi-digit whole numbers and fractions. In the grade 6, students evaluate positive rational numbers and integers with natural number exponents. In grade 7, students will apply the Laws of Exponents with rational number bases and whole-number exponents.

- Instruction focuses on the connection to repeated multiplication.
- Instruction allows student flexibility in their solution (*MTR.2.1*).
 - For example, allow for both fraction and decimal response when the base is a fraction or a decimal.
- Instruction provides opportunities for students to continue to practice and apply multiplying fractions by fractions, decimals by decimals, and integers by integers (*MTR.5.1*).
- Instruction includes the use of technology to explore and evaluate positive rational numbers and integers with natural number exponents.
- The expectation of this benchmark is the application of exponents, not the determining of the value of and expressions with multiple operations.
 - For example, $(-12)^4$ and $\left(\frac{21}{5}\right)^3$ would be appropriate, but $1.258^3 12^2$ or

 $(215^3)(71^2)$ would not be appropriate.

Common Misconceptions or Errors



- Students may multiply the base by the exponent instead of multiplying the base by itself as many times as directed by the exponent. t. Instruction includes students using expanded form to represent the multiplication.
 - For example, 1.258^3 written in expanded form is (1.258)(1.258)(1.258).
- Some students may incorrectly apply or use incorrect notation when exponents are • applied to negative integers. If a negative integer has an exponent, the negative number base must be in parentheses and the exponent is on the outside of the parentheses (MTR.5.1).
 - For example, $(-12)^4 = (-12)(-12)(-12)(-12)$ is not the same as $-12^4 =$ -(12)(12)(12)(12).

Strategies to Support Tiered Instruction

- Instruction includes rewriting exponential expressions in expanded form to represent the multiplication before evaluating.
 - For example:

 - $\left(\frac{1}{4}\right)^3 = \frac{1}{4} \cdot \frac{1}{4} \cdot \frac{1}{4} = \frac{1 \cdot 1 \cdot 1}{4 \cdot 4 \cdot 4} = \frac{1}{64}$ $(-6)^3 = (-6)(-6)(-6) = 36(-6) = -216$
 - $1.258^3 = (1.258)(1.258)(1.258)$
- Teacher creates and posts an anchor chart with visual representations of base of an exponent, exponent, power, and factor then encourages students to utilize the anchor chart to assist in correct academic vocabulary when evaluating exponential expressions.
- Instruction includes the use of exponent tiles to represent and evaluate numerical exponential expressions.
- Teacher provides students with flash cards to practice and reinforce academic vocabulary.

Instructional Tasks

Instructional Task 1 (MTR.4.1)

Robin determines the volume of a cube with side lengths of 3.4 cm to be 10.2 cm^3 . Mickey says the volume is 39.304 cm³. Which person is correct and why?

Instructional Task 2 (MTR.4.1)

Sean told Parker that $-5^3 = (-5)^3$. Parker told Sean that he is incorrect. Is Sean correct or is Parker correct? How do you know?

Instructional Task 3 (MTR.6.1)

Determine if 8^4 is equivalent to 4^8 . Explain your reasoning.

Instructional Items



Instructional Item 1

What is the value of the expression $\left(\frac{1}{3}\right)^3$?

Instructional Item 2 What is the value of the expression 2⁵?

Instructional Item 3 What is the value of the expression 0.1^3 ?

*The strategies, tasks and items included in the B1G-M are examples and should not be considered comprehensive.

MA.6.NSO.3.4

Benchmark

MA.6.NSO.3.4	Express composite whole numbers natural number exponents.	s as a produ	ct of prime factors with
Connecting B	enchmarks/Horizontal Alignment		Terms from the K-12 Glossary
	nections to benchmarks s standard were not found. ment		 Base (of an exponent) Composite Number Exponent Factors (of positive whole numbers) Natural Number Prime Factorization Prime Number Whole Number
Previous Benchma	arks	Next Ben	
• MA.4.AR.3	0.1	• IVI	IA.7.NSO.1.1

• MA.5.NSO.2.1, MA.5.NSO.2.2

http://flbt5.floridaearlylearning.com/standards.html

Purpose and Instructional Strategies

In grade 4, students determined factor pairs for whole numbers from 0 to 144 and determined if numbers are prime, composite, or neither. In grade 5, students multiplied and divided using products and divisors greater than 144. In future grades, students will use their understanding of factors and factorization with simplifying exponents, discovering exponent rules and generate equivalent rational expressions.

- Instruction includes representing multiplication in various ways.
 - $\circ 2^3 \times 3$
 - $\circ 2^3 \cdot 3$



 \circ (2³)(3)

- $\circ 2^{3}(3)$
- If the prime factorization has factors that occur more than once it should be simplified where each factor is a unique term and exponents are used to denote a prime factor occurring more than once (*MTR.2.1*).
- If a composite number has more than three factors, the factor tree can be started in more than one way. Students should identify and compare factor trees to other classmates to see that regardless of which factors they used for the first branch pair on the factor tree it will result in the same prime factorization of the number.
- Instruction includes a variety of methods and strategies to determine the prime factorization (*MTR.2.1, MTR.4.1, MTR.5.1*).
 - Factor tree



• Successively dividing a number by prime numbers



- The benchmark can be taught before 6.NSO.3.3 as a bridge between 6.NSO.3.1 and 6.NSO.3.3 and exponents.
- There is no limitation on the size of the whole number exponent for this benchmark.
- It is important to allow students to connect to the commutative property to understand that the prime factorization can be represented as $2^3 \cdot 6^3$ or $6^3 \cdot 2^3$ (*MTR.2.1, MTR.5.1*).



Common Misconceptions or Errors

- Students may incorrectly think when creating branches on a factor tree, one of the branches of each factor pair has to have a prime number.
- Students may incorrectly think the prime factorization of a number will change if different factors are selected for constructing the prime factorization model.
- Students may incorrectly write the prime factorization from a factor tree because they do not take all of the factors into their solution.
- Students may incorrectly think 2 is a composite number because it is even. Have students list the factor pairs that produce a product of 2 for them to conclude that 2 must be prime because it has exactly 2 factors: 1 and itself.
- Students may incorrectly think most odd numbers, like 91, are prime. It can be helpful to, within problem contexts, incorporate divisibility rules, especially those for 2, 3, 5, 6, 9 and 10, to help students identify factors quickly. If students believe a number is prime, students should try to find a number that can produce the ones digit and try numbers that end with that digit.
 - For example, 91 ends in a 1. If you multiply 7 by 3 you get a number that ends in a 1, and when the division is done, 7 is a factor of 91 with 13 being the second factor.
- Students may confuse finding factors with finding multiples of a number. It is important to use the academic vocabulary of factor and multiple within the contexts of problems and tasks.

Strategies to Support Tiered Instruction

- Teacher identifies the first five prime numbers as 3, 5, 7, 11, 13 and introduces the divisibility rules to utilize when finding prime factors of a given value.
- Instruction includes comparing two different factor trees for the same given number with a focus on recognizing that multiple different factor pairs can be used to produce the same final factorization.
 - For example, 48 can be represented by the factor trees below.



- Instruction includes the use of additional divisibility rules for 2, 3, 5, 7, and 10 to assist with determining factors of a given value.
- Teacher creates and posts an anchor chart with visual representations of factors and multiples and encourages students to utilize the anchor chart to assist in utilizing correct academic vocabulary when referring to factors and multiples.
- Teacher provides students with flash cards to practice and reinforce academic vocabulary.
- Teacher models how to find a number that can produce the ones digit and try numbers that end with that digit.



• For example, 91 ends in a 1. If you multiply 7 by 3 you get a number that ends in a 1, and when the division is done, 7 is a factor of 91 with 13 being the second factor. Teacher has students list the factor pairs that produce a product of 2 for them to conclude that 2 must be prime because it has exactly 2 factors: 1 and itself.

Instructional Tasks

Instructional Task 1 (MTR.2.1, MTR.3.1, MTR.4.1)	
Lizzie and Adam both factored 864. Their answers a	re shown below:
Lizzie	<u>Adam</u>
$864 = 2^5 \cdot 3^3$ 864	$= 2 \cdot 2 \cdot 3 \cdot 3 \cdot 2 \cdot 2 \cdot 3 \cdot 2$
Who factored 864 as a product of primes correctly?	If Lizzie or Adam are incorrect, describe
the error they made. If they are both correct, describe	e which factored form is more efficient
as a solution and justify your reasoning.	
Instructional Items	
Instructional Item 1	
Determine all of the factors of 24. Rewrite 24 as a pr	oduct of its factors using exponents.
Instructional Item 2	
Determine all of the factors of 216. Rewrite 216 as a	product of its factors using exponents
*The strategies, tasks and items included in the B1G-M are example	es and should not be considered comprehensive.

MA.6.NSO.3.5

Benchmark

MA.6.NSO.3.5 Rewrite positive rational numbers in different but equivalent forms including fractions, terminating decimals and percentages.

Example: The number $1\frac{5}{8}$ can be written equivalently as 1.625 or 162.5%.

Benchmark Clarifications:

<u>Clarification 1:</u> Rational numbers include decimal equivalence up to the thousandths place.

Connecting Benchmarks/Horizontal Alignment	Terms from the K-12 Glossary
• MA.6.NSO.1.1	• Dividend
• MA.6.NSO.2.1	• Divisor
• MA.6.AR.3.4	Rational Number



Vertical Alignment

Previous Benchmark

- MA.4.FR.1.2
- MA.5.NSO.1.2
- MA.5.NSO.2.2
- MA.5.FR.1.1
 <u>http://flbt5.floridaearlylearning.com/standards.html</u>
 Purpose and Instructional Structuring

Purpose and Instructional Strategies

In grades 4 and 5, students related the relationship between decimal values and fractions out of ten, one hundred or one thousand. Students also were taught that fractions show a division relationship. This understanding is being extended in grade 6 to re-write positive rational numbers into equivalent forms. This skill is extended in grade 7 to also include negative rational numbers.

- Instruction includes various methods and strategies to rewrite numbers into a percentage.
 - Finding equivalent fractions with denominators of 10, 100 or 1000 to determine the equivalent percentage.
 - Writing fractions and decimals as hundredths; the term percent can be substituted for the word hundredth.
 - Multiplying the decimal by 100.
- Percent means "per 100," so a whole is out of 100, or a whole is 100%. If converting the inverse relationship from a percent to a decimal, students divide the percent by 100 to find the equivalent decimal. Students should be encouraged to look for and discover the pattern that occurs (*MTR.5.1*).
- Instruction includes various methods and strategies to rewrite numbers from fraction to decimal or from decimal to fraction (*MTR.3.1*).
 - Decimal grid models



- Dividing the numerator by the denominator. If the fraction is a fraction greater than one or a mixed number, there will be a whole number in the decimal equivalent and the percent will be greater than 100. Students can convert mixed numbers to fractions greater than one and then divide to help them see the pattern of where the whole number falls in relation to the decimal (*MTR.5.1*).
- Instruction focuses on relating fractions, decimals and percent equivalents to familiar real-world situations, like scores and grades on tests or coupons and sales offered by stores (*MTR.5.1*, *MTR.7.1*).
- Use questioning to help students determine their solution's reasonableness (*MTR.6.1*).
 - For example, is it reasonable for the percent to be more than 100? Is it reasonable for the percent to be less than 1?
- Instruction includes the understanding that percentages are a number and are worth specific amounts in contexts (*MTR*.7.1).
- Students should have practice with and without the use of technology to rewrite positive



Next Benchmarks

- MA.7.NSO.1.2
- MA.7.AR.3.1

rational numbers in different but equivalent forms.

Common Misconceptions or Errors

- Students may incorrectly think that, when dividing, the larger value is divided by the smaller value. This is a common overgeneralization because most of their experience in elementary school is dividing larger values by smaller values.
- Students may misplace the decimal when converting from fraction to decimal form because they forget to place the decimal after the whole number in the dividend if the numbers do not divide evenly or do not place the decimal in the aligned place value of the quotient. It is helpful for some students to use graph paper when dividing with decimals to help students keep place values accurately aligned.
- Students may incorrectly think that the decimal value and the percent are exactly the same, not realizing that the percent is 100 times the decimal value.
- Students may incorrectly convert from fraction to decimal form because of their lack of place value knowledge. Instruction includes students using expanded form of the numbers by adding a decimal and zeros in aligned place values until the decimal terminates. Practice includes multiple opportunities for students to work with fractions that require students to add zeros.
- Students may incorrectly move the decimal direction when converting between decimals and percentages because they do not understand what happens to the decimal when a number is multiplied or divided by a power of 10.

Strategies to Support Tiered Instruction

- Instruction includes the use of estimation when converting fractions to decimal form to ensure the proper placement of the decimal point in the final quotient.
- Instruction includes the use of a 100 frame to review place value for tenths, hundredths, and if needed, thousandths and the connections for decimal and fractional forms.



• For example:

• Instruction includes providing multiple opportunities for students to work with fractions that require students to add zeros.

Instructional Tasks



Instructional Task 1 (MTR.7.1)

Kami told her mother that she answered 17 out of 25 questions correctly on her math test or 68%. Did Kami determine the correct percent score? Explain your reasoning.

Instructional Task 2 (MTR.2.1, MTR.4.1, MTR.5.1)

Complete the table to identify equivalent forms of each number. Explain how you approached your solutions.

Fraction	Decimal	Percent
		79%
$\frac{3}{8}$		
	1.236	
$2\frac{1}{4}$		
	0.625	

Instructional Task 3 (MTR.2.1)

Convert each of the following to an equivalent form to compare their values.

1	.		_3		9	1000/
5	0.4	65%	$2\frac{-}{4}$	5.75	8	123%

Instructional Items

Instructional Item 1

How can $\frac{3}{4}$ be written as a decimal and as a percent?

Instructional Item 2

What is an equivalent fraction and decimal representation of 42%?

Instructional Item 3

Complete the following statement:

 $4\frac{2}{5}$ is equivalent to _____ percent or can be written as the decimal _____.

*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.



MA.6.NSO.4 *Extend understanding of operations with integers.*

MA.6.NSO.4.1

Benchmark	
MA.6.NSO.4.1	Apply and extend previous understandings of operations with whole numbers to add and subtract integers with procedural fluency.
Benchmark Clarifica	tions:
Clarification 1: Instru	uction begins with the use of manipulatives, models and number lines working
towards becoming pr	ocedurally fluent by the end of grade 6.
Clarification 2: Instru	uction focuses on the inverse relationship between the operations of addition and

subtraction. If p and q are integers, then $p - q = p + (-q)$ and $p + q$	
Connecting Benchmarks/Horizontal Alignment	Terms from the K-12
	Glossary
• MA.6.NSO.1	Equal Sign
• MA.6.AR.1.3	Equation
• MA.6.AR.2.2	• Integers
• MA.6.GR.1.2, MA.6.GR.1.3	Number Line
	Whole Number
Vertical Alignment	
Previous Benchmarks Next Be	nchmarks

Previous Benchmarks

• MA.7.NSO.2.2 • MA.3.NSO.2.1

http://flbt5.floridaearlylearning.com/standards.html

Purpose and Instructional Strategies

In elementary grades, students added and subtracted whole numbers using models, including number lines and counters. These skills are extended in grade 6 to compare and perform operations with integers with procedural fluency as well as write and solve single-step equations using integers. In grade 7, students work with all operations with rational numbers in the form of expressions, equations and inequalities.

- It can be beneficial for students to start learning to add and subtract integers using real world contexts such as, the movement of a football on a football field, above and below sea level, temperature; refer to Appendix A for more situations. From the real-world context, develop a conceptual model to represent the situation. From the situation, students can describe the relationship mathematically as an expression.
- Explore opportunities with students to discover patterns or rules instead of being directly instructed and expected to memorize them. It is not expected or recommended that students start by generating equivalent expressions mathematically (MTR.2.1, MTR.5.1, MTR.7.1).
- Use models to help students identify patterns for adding and subtracting integers. Instruction includes opportunities to model adding and subtracting integers using tools such as algebra tiles, two-color counters and number lines. Students should relate the model to the expression (MTR.5.1).
 - Algebra Tiles

+3 + (-5)





• Two-Color Counters



- For example, if a student is evaluating 5 + (-3) using two-colored counters, a student can think, "I start with 5 yellows and 3 reds. A positive and a negative together make a zero-sum pair. So if I have 5 positive yellows and 3 negative reds, 3 of the paired chips will have a sum of zero, and I will have 2 yellow positives remaining, so my answer is 2."
- Number Lines



- For example, if a student is evaluating 2 5 using a number line, a student can think, "I start at positive 2 and move 5 in the negative direction (to the left). I am now at 3." Students can also use the commutative property to change the order to (-5) + 2. The student can see that if they start at -5 and move 2 in the positive direction (right), landing on 3.
- When using algebra tiles or two-color counters, group the positive and negative values to create zero-sum pairs, then the remaining tiles or counters show the resulting value.
- When combining integers on a number line, a negative symbol ("-") denotes the direction that will be traveled. If two negative symbols "-(-)" or subtracting a negative number is present, the operators are showing to switch to the opposite direction of movement twice; the first negative symbol (-) indicates moving to the left on the number line, whereas the second negative symbol (-) indicates moving the opposite direction, or to the right, so it is the same as adding the second addend.
- Instruction includes understanding that subtracting a positive value is the same as adding a negative value-both move the value left or decrease it on the number line. The commutative property can help students to see the relationship. Subtracting a negative value is the same as adding a positive value, moving the value to the right.
- Procedural fluency is developed with the combination of conceptual understanding and practice. Students should be encouraged to think through why a sum or difference would result in a positive or negative value instead of encouraged to memorize a set of rules (*MTR.3.1*).
- The commutative property of addition allows for individuals to rearrange the order of the terms they are adding regardless if they are positive or negative terms (*MTR.3.1*).
 - For example, 6 3 can be rewritten as 6 + (-3) in order to the commutative property to see that this is equivalent to (-3) + 6.



- Use real-world contexts that model opposite relationships, like borrowing/earning money or falling/climbing, to help students conceptually reason through why a solution would be positive or negative (*MTR.6.1*).
- Instruction includes connecting understanding of the magnitudes of numbers to the absolute value of a number.
- Students should develop fluency with and without the use of a calculator when performing operations with integers.
- Instruction includes the use of models to demonstrate that the commutative and associative properties does not apply to subtraction. Demonstrate the correct use of the commutative and associative properties of addition by rewriting a subtraction expression as an addition expression before applying either property.
 - For example, $6-3 \neq 3-6$, but 6-3=6+(-3) and 6-3=(-3)+6.
 - For example, $(3-6) + 5 \neq 3 (6+5)$, but (3-6) + 5 = 3 + (-6) + 5 and (3-6) + 5 = 3 + (-6+5).

Common Misconceptions or Errors

- Some students may misunderstand when adding and subtracting integers, the sign of the "bigger number" is kept.
 - For example, in the expression -8 + 4, the sum will be negative because -8 is the "bigger number." Instead, it can be thought of as there are more negatives than positives being combined, so the result will be negative value.
- Students may confuse zero for being a negative number because it is less than a whole. However, 0 is a neutral number; it is neither positive nor negative.
- Students may incorrectly believe that the number with the larger absolute value will always be the minuend (the first term in a subtraction expression) or that the positive number must always be the minuend. This may stem from an overgeneralization of the common pattern in elementary mathematics that "the larger number always goes first in subtraction."

Strategies to Support Tiered Instruction

- Teacher provides opportunities for students to utilize two-color counters to represent addition and subtraction of integers. Use repeated addition to develop generalizations for multiplying integers and discuss the difference between generalized rules for addition and generalized rules for multiplication.
- Teacher provides opportunities for students to utilize two-color counters when evaluating the sum or difference of integers. Instruction includes having students write the expression, representing the expression with the two-color counters, finding the sum or difference, and then recording the solution.
- Teacher models identifying zero pairs using manipulatives such as two-color counters.



Instructional Tasks

Instructional Task 1 (MTR.7.1)

At 9:00 a.m. the temperature was -5° F. By noon, the temperature had risen 14°F. On a number line, show how to find the temperature at noon. Explain.

Instructional Task 2 (MTR.2.1)

Jonah is a novice when it comes to scuba diving. His first dive was 12 feet deep, and his second dive was 3 feet deeper than the first. Describe the depth of Jonah's second dive. Show your work on a vertical number line.

Instructional Task 3 (MTR.2.1)

At 6:00 p.m., the temperature was 11°C. By midnight, the temperature was -3°C.
Part A. Using a visual model, show how to find the difference between the temperatures.
Part B. Write a numerical expression to represent the temperature change from 6:00 p.m. to midnight. Explain.

Instructional Task 4 (MTR.2.1)

Write -3 - 6 as an equivalent addition problem. How are -3 - 6 and the addition problem you wrote related? Explain using a visual model.

Instructional Items

Instructional Item 1

Evaluate -5 - 8 - (-2).

Instructional Item 2

What is the value of the expression 9 + (-12)?

*The strategies, tasks and items included in the B1G-M are examples and should not be considered comprehensive.

MA.6.NSO.4.2

Benchmark

MA.6.NSO.4.2 Apply and extend previous understandings of operations with whole numbers to multiply and divide integers with procedural fluency.

Benchmark Clarifications:

Clarification 1: Instruction includes the use of models and number lines and the inverse relationship between multiplication and division, working towards becoming procedurally fluent by the end of grade 6.

Clarification 2: Instruction focuses on the understanding that integers can be divided, provided that the divisor is not zero, and every quotient of integers (with non-zero divisor) is a rational number. If p and q are integers where $q \neq 0$, then $-\left(\frac{p}{q}\right) = -\frac{p}{q}$, $-\left(\frac{p}{q}\right) = \frac{p}{-q}$ and $\frac{p}{q} = \frac{-p}{-q}$.



Connecting Benchmarks/Horizontal Alignmen	t Terms from the K-12 Glossary
• MA.6.NSO.1.2, MA.6.NSO.1.3	• Dividend
• MA.6.NSO.3.3	Divisor
• MA.6.AR.2.1, MA.6.AR.2.3	• Expression
	• Factor
	• Integer
_	Number Line
Vertical Alignment	
Previous Benchmarks	Next Benchmarks

 MA.5.NSO.2.1, MA.5.NSO.2.2 <u>http://flbt5.floridaearlylearning.com/standards.html</u>

Next Benchmarks • MA.7.AR.2.1, MA.7.AR.2.2

Purpose and Instructional Strategies

Prior to grade 6, students have multiplied whole numbers and positive rational numbers. This is their first experience multiplying and dividing with negative numbers. In grade 6, students will use these skills to write and solve one step equations. Students will continue to develop these skills in grade 7, with multiplying and dividing rational numbers in all forms and using them to solve equations and inequalities.

- Instruction includes extending the understanding that a negative integer is the same distance from zero, but the opposite direction to multiplying and dividing integers.
 - For example, $-6 \cdot 4$ can be thought of as "the opposite of 6 times 4." Since 6 times 4 is 24, the opposite of 24 is -24.
- Instruction includes using algebra tiles or two-color counters to model multiplication and division of integers. Students flip the tiles over as directed by the negative value being "the opposite of."
 - Algebra Tiles



• Two-Color Counters



- Use guided discussion for students to notice and record patterns. From analyzing the pattern, students should conclude that when two positive or two negative integers are multiplied or divided, the resulting product or quotient is positive. If a negative and a positive number are multiplied or divided, the resulting product or quotient is negative (*MTR.2.1, MTR.5.1*).
- Dividing a negative by a negative can be interpreted as was done when dividing a whole number by a whole number.
 - For example, -8 divided by -4 can be interpreted as "How many groups of -4 are in -8," or as "What is the opposite of the size of the group that you get if you divide a group of -8 into 4 parts?".
- Division should be shown using the ÷ symbol when written horizontally and a fraction bar when written vertically.
- If an integer divided by an integer results in a rational number quotient, the quotient can be written as a fraction or as a decimal (*MTR.3.1*).



- Multiplication and division with integers are inverse relationships resulting in related • equations (MTR.3.1, MTR.5.1).
- Students should develop fluency with and without the use of a calculator when performing operations with integers.
- Instruction includes rewriting negative fractions using the division symbol and grouping symbols.
 - The teacher can refer to the negative sign as "the opposite of" to represent the 0 entire quotient is the opposite of its positive value, which will be negative.
 - For example, $-\frac{50}{10} = -(50 \div 10)$ which is equivalent to -(5), which is equivalent to -5.
 - The teacher can refer to the negative sign as multiplying by -1. 0
 - For example, $-\frac{50}{10} = -1\left(\frac{50}{10}\right)$ which is equivalent to $-1(50 \div 10)$, which is equivalent to -1(5), which is equivalent to -5.
 - The teacher can make connections to the properties of operations (Appendix D). 0
 - For example, $-\frac{50}{10} = -1\left(\frac{50}{10}\right)$ which is equivalent to $-1(50 \div 10)$, which
 - is equivalent to $(-50) \div 10$, which is equivalent to -5. For example, $-\frac{50}{10} = -1\left(\frac{50}{10}\right)$ which is equivalent to $-1(50 \div 10)$, which is equivalent to $50 \div (-10)$, which is equivalent to -5.

Common Misconceptions or Errors

- Students may incorrectly apply rules to multiplication and division of integers without experiencing models to provide concrete understanding. Using algebra tiles or twocolored counters, have students flip over the tiles every time they encounter a negative. This allows students to see a pattern and see negatives as "the opposite of" (MTR.2.1, MTR.5.1).
- Students may incorrectly believe the sign of the product or quotient is determined by the integer that is further from zero because they are confusing the pattern or rules for adding and subtracting integers with multiplying and dividing integers.
- Students may incorrectly conclude if an expression begins with a positive integer, the • value of the expression is positive or if it begins with a negative integer, the value of the expression is negative.
- Students may incorrectly assume if division is written as a negative fraction, both the • numerator and denominator are negative values. This can be addressed by modeling with algebra tiles or colored counters.
- Students may confuse zero for being a negative number because it is less than a whole number. However, 0 is a neutral number; it is neither positive nor negative.
- Students may say that negative value divided by itself is zero because they subtract instead of divide. Students should remember than any number divided by itself is equal to 1.
- Students may make the common mistake of dividing the numbers but not remembering to pay attention to the negative sign. It may help students to write or highlight their negative signs in color to make them stand out visually.

Strategies to Support Tiered Instruction



- Teacher provides opportunities for students to utilize two-color counters to represent multiplication as repeated addition to develop generalizations for multiplying integers and discuss the difference between generalized rules for addition and generalized rules for multiplication.
- Teacher provides opportunities for students to utilize two-color counters when evaluating the product or quotient of integers. Instruction includes having students write the expression, representing the expression with the two-color counters, finding the product or quotient, and then recording the solution.
- Teacher provides instruction on the connections between dividends and divisors and numerators and denominators.
- Teacher provides algebra tiles or two-colored counters, to have students flip over the tiles every time they encounter a negative. This allows students to see a pattern and see negatives as "the opposite of."
- Teacher models with algebra tiles or colored counters.
- Teacher models how to write or highlight their negative signs in color to make them stand out visually.

Instructional Tasks

Instructional Task 1 (MTR.4.1)

Camden is trying to understand why the product of a positive number and a negative number should be negative. How would you explain to Camden why 5(-4) is a negative number?

Instructional Task 2 (MTR.6.1)

Shannon noticed that -2[5 + (-3)] can be rewritten using the Distributive Property as:

$$-2 \cdot 5 + (-2) \cdot (-3)$$

= -10 + _____
= -4

She was not sure what to put in the blank.

Part A. What number must go in the blank so the answer is -4?

Part B. What does this tell Shannon about the result of multiplying two negative numbers?

Instructional Task 3 (MTR.7.1)

Describe a real-world problem that can be solved by dividing -12 by 3. Then, find the quotient and explain what it means in the context of your problem.



Instructional Items

Instructional Item 1

Model one method for evaluating -4×5 .

Instructional Item 2

What is the value of the expression – $72 \div 8$?

Instructional Item 3

Select all of the values that are equivalent.

a.
$$\frac{1}{-4}$$

b. $-\frac{20}{5}$
c. 4
d. $-\left(\frac{-5}{-20}\right)$
e. $-\frac{1}{4}$
f. $\frac{-5}{-20}$

*The strategies, tasks and items included in the B1G-M are examples and should not be considered comprehensive.



Algebraic Reasoning

MA.6.AR.1 Apply previous understanding of arithmetic expressions to algebraic expressions.

MA.6.AR.1.1

Benchmark		
MA.6.AR.1.1	Given a mathematical or real-world conte algebraic expressions and translate algebr descriptions.	· · ·
_	The algebraic expression $7.2x - 20$ can be use company who makes \$7.20 per product sold w Benchmarks/Horizontal Alignment	• •
 MA.6.N MA.6.N MA.6.N MA.6.A MA.6.A 	ISO.1.2, MA.6.NSO.1.3, ISO.2.1, MA.6.NSO.2.2, ISO.2.3 R.2.2, MA.6.AR.2.3 R.3.5 R.2.2, MA.6.GR.2.3	 Associative Property Absolute Value Coefficient Commutative Property of Addition Commutative Property of Multiplication Expression
Previous Bench		hmarks
	R.2.1, MA.5.AR.2.4 • MA	A.7.AR.2.2

Students are focusing on appropriate mathematical language when writing or reading expressions. In earlier grade levels, students have had experience with unknown whole numbers within equations. Grade 6 extends this knowledge by focusing on using verbal and written descriptions using constants, variables and operating with algebraic expressions. In grade 7, students use this knowledge when solving equations involving mathematical and real-world contexts.

- Within this benchmark, instruction includes connections to the properties of operations, including the associative property, commutative property and distributive property. Students need to understand subtraction and division do not comply with the commutative property, whereas addition and multiplication do. Students should have multiple experiences writing expressions (*MTR.2.1, MTR.5.1*).
- Instruction focuses on different ways to represent operations when translating written descriptions into algebraic expressions. For translating multiplication descriptions, students should understand that multiplication can be represented by putting a coefficient in front of a variable.
 - For instance, if students were translating "six times a number n," they can write the algebraic expression as 6n.
- For translating division descriptions, students should understand that division can be represented by using a fraction bar or fractions as coefficients in front of the variables (*MTR.2.1*).



- For example, if students were translating "a third of a number *n*," they can write the algebraic expression as $\frac{1}{3}n$ or $\frac{n}{3}$.
- Students are expected to identify the parts of an algebraic expression, including variables, coefficients and constants, and the names of operations (sum, difference, product and quotient).
- Variables are not limited to x; instruction includes using a variety of lowercase letters for their variables; however, o, i, and l should be avoided as they too closely resemble zero and one.

Common Misconceptions or Errors

- Students may incorrectly assume that there is not a coefficient in front of a variable if there is not a number explicitly written to indicate a coefficient (*MTR.2.1*).
 - \circ x is the same as 1x
- Students may incorrectly think that terms that are being combined using addition and subtraction have to be written in a specific order and not realize that the term being subtracted can come first in the form of a negative number (*MTR.2.1*).
 - \circ 2x 3 is the same as -3 + 2x
- Students may incorrectly oversimplify a problem by circling the numbers, underlining the question, boxing in key words, and try to eliminate information that is important to the context. This process can cause students to not be able to comprehend the context or the situation (*MTR.2.1, MTR.4.1, MTR.5.1, MTR.7.1*).

Teachers and students should engage in questions such as:

- What do you know from the problem?
- What is the problem asking you to find?
- Are you putting groups together? Taking groups apart? Or both?
- Are the groups you are working with the same sizes or different sizes?
- Can you create a visual model to help you understand or see patterns in your problem?

Strategies to Support Tiered Instruction

- Instruction includes the use of pictorial representations, tape diagrams, or algebra tiles to represent the written situation before writing an expression.
- Instruction includes identifying unknowns, constants, negative values, and mathematical operations in a written description or algebraic expression.
- Instruction includes co-creating a graphic organizer that includes words used in written descriptions for each of the operations. The graphic organizer should continue to grow as new contexts are encountered.
- Teacher provides opportunities for students to comprehend the context or situation by engaging in questions such as:
 - What do you know from the problem?
 - What is the problem asking you to find?
 - Are you putting groups together? Taking groups apart? Or both?
 - Are the groups you are working with the same sizes or different sizes?
 - Can you create a visual model to help you understand or see patterns in your problem?



Instructional Tasks

Instructional Task 1 (MTR.7.1)

The amount of money Jazmine has left after going to the mall could be described by the algebraic expression 75 - 12.75s - 9.50d, where s is the number of shirts purchased and d is the number of dresses purchased.

Part A. Describe what each of the terms represent within the context.

Part B. What are possible numbers of shirts and dresses Jazmine purchased.

Instructional Task 2 (MTR.2.1)

Some of the students at Kahlo Middle School like to ride their bikes to and from school. They always ride unless it rains. Let d represent the distance, in miles, from a student's home to the school. Write two different expressions that represent how far a student travels by bike in a four-week period if there is one rainy day each week.

Instructional Items

Instructional Item 1

Rewrite the algebraic expression as a written description: $10 - \frac{6}{2}$.

Instructional Item 2

Write an expression to represent the phrase "9 plus the quotient of w and 4."

Instructional Item 2

Write an expression to represent the phrase "7 fewer than the product of 3 and y."

*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.

MA.6.AR.1.2

Benchmark			
MA.6.AR.1.2		-	into an algebraic inequality in the epresent the inequality on a number
Example:	83 out of 100 correct questions of	on the semester here students r	tza if the class has an average of at least exam. The inequality $g \ge 83$ can be eccive a pizza and the inequality $g < 83$ dents do not receive a pizza.
-	<u>fications:</u> ariables may be on the left or right Benchmarks/Horizontal Alig		nequality symbol. Terms from the K-12 Glossary
 MA.6.N MA.6.A MA.6.I 			Number Line
Vertical Ali	gnment		
Previous Bench	marks	Next Bencl	nmarks
• MA.5.N	SO.1.4	• MA	A.7.AR.2.1
• MA.5.A	R.2.1, MA.5.AR.2.4		
FLORIDA DEPART			60 Page

Purpose and Instructional Strategies

In grade 5, students plotted, ordered and compared multi-digit decimal numbers up to the thousandths using the greater than, less than, or equal to symbols. Students translated written real-world and mathematical situations into numerical expressions. In grade 6, students plot, order and compare on both sides of zero on the number line with all forms of rational numbers. The algebraic inequalities include "is less than or equal to" (\leq) and "is greater than or equal to" (\geq). In grade 7, students will write and solve one-step inequalities in one variable and represent the solutions both algebraically and graphically.

- Instruction emphasizes the understanding of defining an algebraic inequality both numerically and graphically. Students should explore how "is greater than or equal to" and "is strictly greater than" are similar and different as well as "is less than or equal to" and "is strictly less than." Students should use appropriate language when describing the algebraic inequality.
- The expectation of this benchmark includes translating from an algebraic inequality into a real-world written description.
- As students identify and write the inequality relationships it is important to ask students about other values on the number line (*MTR.6.1, MTR.7.1*).
 - For example, when representing the inequality x > 1 on the number line, students should compare numbers to 1 in order to determine whether to shade to the left or to the right of 1.
- Instruction includes inequalities where the variable is on the left and right side of the inequality symbol. This will create flexibility in their thinking to be able to apply in future applications of inequalities. Students should form equivalent statements to demonstrate their understanding of how inequalities are related. Students should use context to determine which situation is most appropriate for forming the inequality (*MTR.2.1*).
 - For example, a > 8 can be written as 8 < a.
- Students should understand the solution set and its graphical representation on a number line. This includes showcasing inclusive (closed circle) or non-inclusive (open circle) as well as shading to represent the solution set.
- A number line is a useful tool for modeling inequality situations.
 - For example, students can model on a vertical number line having to be at least 40 inches tall to ride a roller coaster.
- Instruction includes the understanding how inequality relationships can be represented in real-world contexts from the beginning. It can be talked about in terms of character lives in a video game, or amount of money to purchase apps or popular items. Allow students opportunities to identify their own inequality relationships as written descriptions and share with classmates to have them create the algebraic inequality and represent it on the number line (*MTR.1.1, MTR.4.1, MTR.5.1, MTR.7.1*).

Common Misconceptions or Errors

- Students may incorrectly think that the variable must always be written on the left-hand side of the inequality symbol. It is important that students be able to read and understand the context regardless of the side of the inequality that the variable is placed.
- Students may incorrectly shade the solution set of an inequality on a number line. Using



verbal descriptions acknowledging the relationship between the number and the variable can support students in identifying the solution set. Students should test numbers on each side of the value to determine if they are true statements.

- For example, if the relationship is x > 3, have students replace the x with -5 and 5 to see which one creates a true statement.
- Students may not understand the difference between inclusive and non-inclusive solutions sets on a number line. Students can benefit from reasoning within a real-world context.

Strategies to Support Tiered Instruction

- Teacher provides inequalities with variables on the left or right side of the symbol and has students write two verbal comparisons for each statement.
 - For example, x > 15 can be read as "x is greater than 15" or as "15 is less than x."
 - For example, $k \le 6$ can be read as "k is less than or equal to 6" or as "6 is greater than or equal to y."
- Instruction includes the use of substitution to test various numbers to determine which set of numbers will make true statements and then to draw a ray in the appropriate direction. The same strategy holds true for reasoning with inclusive and non-inclusive solution sets and the difference in the solid or open point at the indicated value.
- Teacher provides students with flash cards to practice and reinforce academic vocabulary.
- Instruction includes creating a list of common terms from contextual situations that may be used to describe situations requiring an inequality symbol and add to as an interactive anchor chart as additional situations arise.

(>)	(<)	(≥)	(\leq)
is greater than	is less than	is greater than	is less than or
_		or equal to	equal to
		at least	at most
			no more than

- Examples include the table below.
- Teacher uses verbal descriptions to acknowledge the relationship between the number and the variable to support students in identifying the solution set. Students should test numbers on each side of the value to determine if they are true statements.
 - For example, if the relationship is x > 3, have students replace the x with -5 and 5 to see which one creates a true statement.

Instructional Tasks

Instructional Task 1 (MTR.4.1)

The graph below describes the altitudes, measured in feet, at which civilian aircraft must provide everyone with supplemental oxygen, according to the U.S. Federal Aviation Regulation.



10,000

20,000

Determine an inequality to represent the situation. How can this be written in another way?



Instructional Task 2 (MTR.4.1)

According to historical records, the highest price for regular gas in Florida over the last ten years was just under \$4.06. Tammy states that this is an inclusive relationship. Christine says it is a non-inclusive relationship. Who is correct and why?

Instructional Items

Instructional Item 1

Graph x > 3 on a number line.

Instructional Item 2

According to Interstate Highway Standards, U.S. and state highway traffic lanes must be at least 12 feet wide. Write an inequality to represent the widths that traffic lanes can be.

Instructional Item 3

Trini is allowed to play video games no more than 4 hours over the weekend. Graph the inequality on a number line.

Instructional Item 4

A farmer is going to plant more than 50 acres in corn this year. If *a* represents the number of acres planted in corn, write an inequality to describe all possible values of *a*.

Instructional Item 5

High altitude parachute jumps are usually made from an altitude that is no more than 35,000 feet to avoid frostbite from extreme cold. If *h* represents the height of a jumper, write an inequality to describe all possible values of *h*.

*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.

MA.6.AR.1.3

Benchmark

MA.6.AR.1.3 Evaluate algebraic expressions using substitution and order of operations.

Example: Evaluate the expression $2a^2 - b^5$, where a = -1 and b = 15.

Benchmark Clarifications:

Clarification 1: Within this benchmark, the expectation is to perform all operations with integers. *Clarification 2:* Refer to Properties of Operations, Equality and Inequality (Appendix D).

Connecting Benchmarks/Horizontal Alignment	Terms from the K-12 Glossary
 • MA.6.NSO.3.3	• Base
• MA.6.NSO.4.1, MA.6.NSO.4.2	Coefficient
• MA.6.AR.2.1	• Exponent
	Expression

Vertical Alignment Previous Benchmarks

Next Benchmarks



- MA.5.AR.2.1, MA.5.AR.2.2, MA.5.AR.2.3
- MA.7.NSO.1.1
- MA.7.NSO.2.1
- MA.7.AR.1.1, MA.7.AR.1.2

Purpose and Instructional Strategies

In grade 5, students translated written real-world and mathematical descriptions into numerical expressions, evaluated multi-step numerical expressions used order of operations involving combinations of the four arithmetic operations and parentheses with whole numbers, decimals and fractions. They also determined and explained whether an equation involving any of the four operations is true or false. In grade 6, students will use substitution to evaluate algebraic expressions, including exponents and integer coefficients. The values being substituted will also be integers. This benchmark extends to grade 7 where students will evaluate more complex numerical expressions with rational coefficients, apply laws of exponents and generate equivalent linear expressions.

- Substitution is the process in which a symbol or variable is replaced by a given value. In prior grades students have found missing terms in equations and then substituted the value back in to check it they are correct.
 - For example, students may have seen something such as 2 + ? = 10 and decided that 8 is the value that should replace the ?.

This prior experience can be used to connect prior student understanding with new learning. In grade 6, instead of seeing a symbol like a question mark or a box for a missing value, we use letters called variables.

- An algebraic expression is built from integer constants, variables and operations whereas an equation is the statement of two equivalent expressions. This benchmark is specifically addressing substitution.
- Depending on the given expression, students may see opportunities to start generating equivalent expressions before substituting the value of the variable(s). This is a way students can demonstrate flexible thinking and the understanding of patterns and structure in mathematical concepts (*MTR.5.1*).

Common Misconceptions or Errors

- Students may incorrectly generate equivalent expressions using the order of operations.
- If more than one variable is present in a given expression, students may incorrectly substitute one value in for all given variables or apply the wrong value to each of the variables. To address this misconception, students can use colors (pens, pencils, markers) to keep track of which variable and location correspond to each given value.
- If students try to generate an equivalent expression before substituting integer values, they may try to combine unlike terms (constants with variables or unlike variable terms).

Strategies to Support Tiered Instruction

• Instruction includes building a foundation for the meaning of substitution by introducing algebraic expressions in a single variable with an exponent of 1 and representing the expression with algebra tiles. Then the variable tile can be replaced with the appropriate number of unit tiles to represent the provided value and the expression can be evaluated. The algebraic expression should be represented simultaneously to draw connections between the concrete and abstract representations. Use this foundation to build towards



using algebraic strategies to evaluate expressions that cannot be represented with algebra tiles.

- Algebra Tiles
 Algebraic Representation

 3b + 5 3(-4) + 5

 3(-4) + 5 -12 + 5

 -7 -7
- For example, when evaluating 3b + 5 when b = -4, students can represent this as shown below.

- Teacher provides opportunities for students to use different colored pencils to represent different variables and use the coordinating color to replace the variable with its assigned value before utilizing the order of operations to evaluate.
 - For example, if evaluating the expression $-5a^2 + c$, where a = -3 and c =
 - -12, the teacher can color coordinate as shown below.

 $-5a^{2} + c; a = -3 \text{ and } c = -12$ $-5(-3)^{2} + (-12)$ -5(9) + (-12) -45 + (-12)-57

• Teacher models how students can use colors (pens, pencils, markers) to keep track of which variable and location correspond to each given value.

Instructional Tasks

Instructional Task 1 (MTR.5.1)

To compute the perimeter of a rectangle you add the length, l, and width, w, and double this sum.

Part A. Write an expression for the perimeter of a rectangle.

Part B. Use the expression to find the perimeter of a rectangle with length of 15 feet and width of 8 feet.



Instructional Task 2 (MTR.6.1)

To determine the distance traveled by a car you multiply the speed the car traveled by the amount of time the car was traveling at that speed. The scenario can be represented as st, where s is speed, and t is time. What is the distance traveled by a car that travels at an average speed of 75 miles per hour for 20 minutes?

Instructional Items

Instructional Item 1 If x = 3, find 3x + 8.

Instructional Item 2

If
$$p = 8$$
, find $\frac{1}{4}p - 3$.

Instructional Item 3

Evaluate the expression $-5a^2 + c$, where a = -3 and c = -12.

*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.



MA.6.AR.1.4

Benchmark		
MA.6.AR.1.4	Apply the properties of operations to gene with integer coefficients.	erate equivalent algebraic expressions
Example:	The expression $5(3x + 1)$ can be rewritten equation	uivalently as $15x + 5$.
Example:	If the expression $2x + 3x$ represents the profit selling the same number of cupcakes, sold for The expression $5x$ can express the total profit.	
Clarification 2: R	<u>Fications:</u> roperties include associative, commutative and refer to Properties of Operations, Equality and I Benchmarks/Horizontal Alignment	
• MA.6.N		Coefficient
• MA.0.1	NSO.3.2	Distributive PropertyExpressionInteger
Vertical Ali	gnment	e e e e e e e e e e e e e e e e e e e
Previous Bench	imarks Next Benc	hmarks
• MA.5.A	R.2.2 • MA	A.7.AR.1.1
	• MA	A.7.AR.1.2
Dumose an	d Instructional Strataging	

Purpose and Instructional Strategies

In grade 5, students evaluated multi-step numerical expressions using order of operations including parentheses, whole numbers, decimals and fractions. In grade 6, variable terms are introduced to create algebraic expressions with whole number coefficients. In grade 7, rational number coefficients will be used in variable expressions.

- Instruction focuses on students using the properties of operations to generate equivalent algebraic expressions.
- Within this benchmark, all variables will have an exponent value of 1. Laws of exponents are introduced in grade 7.
- Students should understand if values are equivalent, they are worth the same amount.
 - For example, a 1 dollar bill, 4 quarters, 10 dimes, 20 nickels, 2 half-dollars or 100 pennies have equal values and can be represented as 1b = 4q, 1b = 10d, 1b = 20n, 1b = 2h or 1b = 100p, respectively.
- Instruction includes generating equivalent expressions and comparing with other students' solutions. Discussion focuses around looking for similarities and relationships between students' approaches (*MTR.4.1*).
- Instruction includes the use algebra tiles or other concrete representations to provide visual representation of the properties of operations.





- Students should be encouraged to generate equivalent expressions in ways that are mathematically accurate and make sense to the individual. Students should be able to justify their process using properties of operations.
- Instruction includes having expressions with more than one variable as well as nested grouping symbols.
 - Expression with more than one variable
 - -4x + 3x 2y
 - Nested grouping symbols

$$-2[3(x-3)]$$

Common Misconceptions or Errors

- Students may incorrectly think there is only one right answer or equivalent value to be found. Although the most simplified version of an expression is an equivalent expression, it may not be the only equivalent expression.
- Students may incorrectly perform operations involving nested grouping symbols. Students can be taught or reminded that each grouping symbol is treated similarly to parentheses.

Strategies to Support Tiered Instruction

- Instruction includes providing students with algebra tiles and two different expressions. Students should represent the provided expressions with the algebra tiles and determine if the two expressions are equivalent or not by comparing the number of each tile.
- Teacher provides opportunities for students to use algebra tiles to represent various given expressions, manipulate the tiles to show the expression a different way and then write the corresponding expression.
- Instruction includes building a foundation for the properties of operations by modeling the associative, commutative, and distributives properties with algebra tiles for numeric and algebraic expressions and allowing the students to manipulate the algebra tiles as well.
- Instruction includes providing students with two different expressions already represented with algebra tiles and then allowing the students to manipulate the algebra tiles to determine if they are equivalent. Students should be allowed to justify their reasoning for why the expressions are equivalent, or not.
- Teacher reminds students that each grouping symbol is treated similarly to parentheses.



Instructional Tasks

Instructional Task 1 (MTR.2.1, MTR.5.1)

Look at the following expressions.

2(5+(3)(2)+x)2[(5+3)(2+x)]2(5+3(2+x))

Part A. Simplify the expressions shown above.

Part B. Can any grouping symbols be removed from the expressions without changing the value of the expression?

Instructional Task 2 (MTR.2.1)

```
How can you show the two expressions, 2(x + 5) and 2(x) + 2(5), are equivalent? Explain. Instructional Items
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Instructional Item 1

Tamika is selling chocolate candy bars for \$1 and bags of popcorn for \$3 at the school fair. She sells y candy bars and (y - 7) bags of popcorn. The expression 1y + 3(y - 7) represents Tamika's total sales. Rewrite the expression in a different but equivalent form.

*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.

MA.6.AR.2 Develop an understanding for solving equations and inequalities. Write and solve one-step equations in one variable.

MA.6.AR.2.1

Benchmark

MA.6.AR.2.1 Given an equation or inequality and a specified set of integer values, determine which values make the equation or inequality true or false.

Example: Determine which of the following values make the inequality x + 1 < 2 true: -4, -2, 0, 1.

Benchmark Clarifications:

Clarification 1: Problems include the variable in multiple terms or on either side of the equal sign or inequality symbol.

Connecting Benchmarks/Horizontal Alignment	Terms from the K-12 Glossary
• MA.6.NSO.4.1, MA.6.NSO.4.2	Coefficient
• MA.6.AR.1.2, MA.6.AR.1.3	• Distributive Property
	• Equation
	• Integer

Vertical Alignment

Previous BenchmarksMA.5.AR.2.2, MA.5.AR.2.3

Next Benchmarks • MA.7.AR.2.1, MA.7.AR.2.2

- MA.S.AK.2.2, MA.S.AK.2.5 Purpose and Instructional Strategies
- FLORIDA DEPARTMENT OF EDUCATION Fide.org

In grade 5, students evaluated numerical expressions as well as simplified numerical expressions on both sides of an equation to determine if the equation was true or false. In grade 6, the skills are extended to evaluating expressions where students must substitute the given value of a variable. Students are also expected to use substitution with multiple variables within algebraic equations and inequalities to determine which of the given values make the mathematical statement true and which make it false. The substituted values in grade 6 are limited to integers. This skill extends into grade 7 where students learn to solve two-step equations and one-step inequalities to determine their rational number solutions.

- Instruction focuses on the understanding that solving an equation or inequality is a process of answering the question:
 - Which values from a specified set, if any, make the equation or inequality true?
- Instruction emphasizes the understanding of defining an algebraic inequality. Students should have practice with inequalities in the form of x > a, x < a, x ≥ a and x ≤ a. Students should explore how "is greater than or equal to" and "is strictly greater than" are similar and different as well as "is less than or equal to" and "is strictly less than." Students should use academic language when describing the algebraic inequality (*MTR.4.1*).
- Students should understand a variable can represent an unknown number or, depending on the context, any value in a specified set.
- Instruction includes using set notation to list numbers but not writing solutions in set notation as well as equations where the same variable is in more than one term or on both sides of the equation or inequality. Set notation does not require descending or ascending order.
 - Set notation: $\{-3, 0, 4, 11\}$ or $\{5, -3, 2, 0, 13\}$.
- For this benchmark, students are not expected to perform operations with negative rational numbers.

Common Misconceptions or Errors

- Some students may incorrectly believe only one value can make an inequality true. Inequalities describe a relationship between expressions that more than one value can satisfy.
- If more than one operation is present, students may incorrectly think there is always only one way to accurately evaluate it when there may be more than one accurate method.
 - For example, if students are asked to determine the truth value of x = 8 given the equation 2x 3(x 4) = 4, students could accurately solve using order of operations and properties of operations in more than one way.



Strategies to Support Tiered Instruction

- Instruction includes the use of pictorial representations, tape diagrams, or algebra tiles to represent the equation or inequality then replacing the variables with the possible solutions to test for the equation or inequality to be true.
 - For example, the following representations can be used to determine which of the values, 4 5 or 5, make the equation 4x + 5 = 25 true.

4 <i>x</i>	╋	5	=	25:	

x	x	x	x	1	1	1	1	1
	25							
$4x + 5 \neq 25$, wh	en x = 4							
4	4	4	4	1	1	1	1	1
		21						
4x + 5 = 25, wh	en x = 5							
5	5	5	5	1	1	1	1	1
		25						
$4x + 5 \neq 25$, when $x = 6$								
6	6	6	6	1	1	1	1	1
		29						

• Teacher provides instruction with a simple inequality statement and its graph, and then has students use substitution and the number line to test for possible solutions. Gradually remove the support of the number line and transition students to using only substitution to test for possible values to make the given inequalities true.

Instructional Tasks

Instructional Task 1 (MTR.4.1)

Explain what it means for a number to be a solution to an equation. Explain what it means for a number to be a solution to an inequality.

Instructional Task 2 (MTR.3.1, MTR.4.1, MTR.5.1)

Provide students with a set of integer values.

- Part A. Choose one of the integer values and create an equation that would make a true statement with your selected value.
- Part B. Compare your equation with someone who choose the same value and a different value. What do you notice?
- Part C. Choose two of the integer values and create an inequality that would make a true statement with your selected values. Create another inequality that would make a true statement with one of your selected values but not the other.
- Part D. Compare your inequality with someone who chose the same values and someone who chose different values. What do you notice?

Enrichment Task 1 (MTR.5.1, MTR.6.1)



Which of the following values are solutions to the inequality $6a + 2 \le a - 23$?

a. -5 a. $\frac{21}{5}$

c. –25 d. 5

- e. 4.2
- f. $-\frac{25}{7}$

Instructional Items

Instructional Item 1

Which of the following values makes the equation 3x + 8 = 14 true?

a. -2

b. 2

c. 3

d. 6

Instructional Item 2

Which of the following values make the inequality 4x + 5 > 25 true?

- a. -3 b. 4 c. 5
- d. 6 e. 12

*The strategies, tasks and items included in the B1G-M are examples and should not be considered comprehensive.


MA.6.AR.2.2

MA.0.AK.2.2			
Benchmark			
MA.6.AR.2.2	Write and solve one-step equation real-world context using additions are integers.		
Example:	The equations $-35 + x = 17, 17$ = question "How many units to the r		
-		-	umber lines and inverse operations. and $p + x = q$, where x, p and q
are any integer.	-		
	roblems include equations where th Benchmarks/Horizontal Align		e on either side of the equal sign. erms from the K-12 Glossary
• MA.6.N	JSO.4.1	•	Additive Inverse Property
• MA.6.A	AR.1.1	•	Addition Property of Equality
		•	Associative Property
		•	• Commutative Property of Addition
		•	Equation
		•	Identity Property of Addition
		•	Integer
		•	Number Line
Vertical Ali	gnment		
Previous Bench	marks	Next Benchma	rks
• MA.5.A	R.1.1, MA.5.AR.2.1	• MA.7.A	R.2.2
	$D \rightarrow M \wedge 5 \wedge D \rightarrow 2$		

• MA.5.AR.2.2, MA.5.AR.2.3, MA.5.AR.2.4

Purpose and Instructional Strategies

In grade 5, students wrote and evaluated numerical expressions with positive rational numbers. Students also wrote equations to determine an unknown whole number. In grade 6, students extend their understanding to solve one-step equations which include integers. In grade 7, students write and solve one-step inequalities and two-step equations involving rational numbers.

- When students write equations to solve real-world and mathematical problems, they draw on meanings of operations that they are familiar with from previous grades' work.
- Problem types include cases where students only create an equation, only solve an equation and problems where they create an equation and use it to solve the task. Equations include variables on the left or right side of the equal symbol.
- Use models or manipulatives, such as algebra tiles, bar diagrams, number lines and balances to conceptualize equations (*MTR.2.1*).
 - Algebra Tiles





Balances \cap



Students should understand the equal sign represents the fulcrum in the center of the balance and the scale is supposed to stay balanced even when you manipulate the expression on the pan of the balance (MTR.2.1).

- Instruction includes students identifying the properties of operations and properties of equality being used at each step toward finding the solution. Explaining informally the validation of their steps will provide an introduction to algebraic proofs in future mathematics (MTR.5.1).
- Students should be encouraged to show flexibility in their thinking when writing • equations.

Common Misconceptions or Errors

- Students may incorrectly apply an operation to a single side of an equation. •
- Students may incorrectly use the addition and subtraction properties of equality on the same side of the equal sign while solving an equation. To address this misconception, use manipulatives such as balances, algebra tiles, or bar diagrams to show the balance between the two sides of an equation (MTR.2.1).

- Instruction includes identifying unknowns, constants, negative values, and mathematical operations in the provided context.
- Teacher provides opportunities for students to comprehend the context or situation by engaging in questions such as:
 - What do you know from the problem?
 - What is the problem asking you to find?
 - Are you putting groups together? Taking groups apart? Or both?
 - Are the groups you are working with the same sizes or different sizes?
 - Can you create a visual model to help you understand or see patterns in your problem?
- Teacher provides opportunities for students to use algebra tiles to co-solve provided equations with the teacher without the need of writing the equation first.



- Teacher provides opportunities for students to co-write an algebraic equation with the teacher without requiring students to solve the equation.
- Teacher models the use of manipulatives such as balances, algebra tiles, or bar diagrams to show the balance between the two sides of an equation.

Instructional Tasks

Instructional Task 1 (MTR.2.1, MTR.4.1)

Melvin wants to go to the school musical. The school auditorium has 1250 seats arranged in three sections. The left section has 375 seats, and the right section has 375 seats. Write an equation to find the number of seats in the center section and explain why you wrote the equation the way you did.

Instructional Items

Instructional Item 1 Given z + 15 = 3, what is the value of z?

Instructional Item 2

Given 6 = x - 13, what is the value of x?

Instructional Item 3

Alex has some money in his wallet. His grandmother gives him \$10 for a gift in his birthday card. He now has \$28 in his wallet. Write an equation to represent the problem. How much money did he originally have in his wallet?

Instructional Item 4

The width of the rectangular table top is 4 feet shorter than its length. If the length of the table top is 6 feet, write and solve an equation to determine the width of the table top. *The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.



MA.6.AR.2.3

_		
Benchmark		
MA.6.AR.2.3	Write and solve one-step equations in real-world context using multiplicatio solutions are integers.	one variable within a mathematical or n and division, where all terms and
<i>Clarification 2:</i> In <i>Clarification 3:</i> Pr		
• MA.6.G MA.6.G	R.1.1 R.3.4, MA.6.AR.3.5 R.2.1, MA.6.GR.2.3, R.2.4	 Associative Property Commutative Property of Multiplication Division Property of Equality Equation Identity Property of Multiplication Integer Multiplicative Inverse (reciprocal) Multiplication Property of Equality Number Line Substitution Property of Equality
Vertical Alig		enchmarks
 MA.5.AF MA.5.AF MA.5.AF 	R.2.1, MA.5.AR.2.3,	MA.7.AR.2.2

Purpose and Instructional Strategies

In grade 5, students wrote and evaluated numerical expressions with positive rational numbers. Students also wrote equations to determine an unknown whole number. In grade 6, students extend their understanding to solve one-step equations which include integers. In grade 7, students write and solve one-step inequalities and two-step equations involving rational numbers.

- When students write equations to solve real-world and mathematical problems, they draw on meanings of operations that they are familiar with from previous grades' work.
- Problem types include cases where students only create an equation, only solve an equation and problems where they create an equation and use it to solve the task. Equations include variables on the left or right side of the equal symbol.
- For multiplication, instruction includes the use of coefficients, parentheses and the raised dot symbol (·).
- Use models or manipulatives, such as algebra tiles, bar diagrams and balances to conceptualize equations (*MTR.2.1*).
 - Algebra Tiles





• Bar Diagrams

2x = -26			
x	x		
—:	26		

• Balance



- Instruction includes many contexts involving negative integers, including connections to ratio, rate and percentage problems in MA.6.AR.3.4 and MA.6.AR.3.5.
- Instruction can include students identifying the properties of operations and properties of equality being used at each step toward finding the solution. Explaining informally the validation of their steps will provide an introduction to algebraic proofs in future mathematics (*MTR.5.1*).
- Students should be encouraged to show flexibility in their thinking when writing equations.

Common Misconceptions or Errors

- Students may incorrectly apply an operation to a single side of an equation.
- Students may incorrectly use the multiplication and division properties of equality on the same side of the equal sign while solving an equation. To address this misconception, use manipulatives such as, algebra tiles, number lines or bar diagrams to show the balance between the two sides of an equation (*MTR.2.1*).

- Instruction includes identifying unknowns, constants, negative values, and mathematical operations in the provided context.
- Teacher provides opportunities for students to comprehend the context or situation by engaging in questions such as:
 - What do you know from the problem?
 - What is the problem asking you to find?
 - Are you putting groups together? Taking groups apart? Or both?
 - Are the groups you are working with the same sizes or different sizes?
 - Can you create a visual model to help you understand or see patterns in your problem?



- Teacher provides opportunities for students to use algebra tiles to co-solve provided • equations with the teacher without the need of writing the equation first.
- Teacher provides opportunities for students to co-write an algebraic equation with the teacher without requiring students to solve the equation.
- Teacher models the use of manipulatives such as, algebra tiles, number lines or bar diagrams to show the balance between the two sides of an equation.

Instructional Tasks

Instructional Task 1(MTR.4.1, MTR.7.1)

A solar panel generates 200 watts of power each hour. A warehouse wants to generate 34,000 watts of power each hour.

- Part A. Write an equation to find how many solar panels the warehouse will need on its roof to generate 34,000 watts of power each hour.
- Part B. Explain why you wrote the equation the way you did. Could you write the equation in another way?
- Part C. Find the solution to your equation.
- Part D. What does the solution to your equation mean?

Instructional Items

Instructional Item 1

An outlet mall has 4 identical lots that can hold a total of 1,388 cars. The equation 4c =1388 describes the number of cars that can fit into each lot. How many cars can fit into each lot?

Instructional Item 2

Given $\frac{x}{7} = 56$, what is the value of x? *The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.



MA.6.AR.2.4

Benchmark

MA.6.AR.2.4 Determine the unknown decimal or fraction in an equation involving any of the four operations, relating three numbers, with the unknown in any position.

Example: Given the equation $\frac{9}{8} = x - \frac{1}{8}$, x can be determined to be $\frac{10}{8}$ because $\frac{10}{8}$ is $\frac{1}{8}$ more than $\frac{9}{8}$.

Benchmark Clarifications:

Clarification 1: Instruction focuses on using algebraic reasoning, drawings, and mental math to determine unknowns.

Clarification 2: Problems include the unknown and different operations on either side of the equal sign. All terms and solutions are limited to positive rational numbers.

Connecting Benchmarks/Horizontal Alignment	Terms from the K-12 Glossary
• MA.6.NSO.2.1, MA.6.NSO.2.2,	• Dividend
MA.6.NSO.2.3	Divisor
• MA.6.GR.1.2, MA.6.GR.1.3	• Equation
	• Equal Sign
	Number Line
Vertical Alignment	

Next Benchmarks

• MA.7.AR.2.2

Previous Benchmarks

- MA.5.NSO.2.5
- MA.5.FR.2.1
- MA.5.AR.2.3

Purpose and Instructional Strategies

In grade 5, students multiplied and divided decimals by one tenth and one hundredth, added and subtracted fractions with unlike denominators, and determined if equations were true. In grade 6, students increase their computation with fractions and decimals as well as solve equations with integers. In grade 7, students solve multi-step equations with rational numbers.

- Thinking through the lens of fact families can help students think flexibly about number relationships to determine the unknown value (*MTR.5.1*).
- This benchmark allows for fractions in equations to include unlike denominators.
- The benchmark expects students to reason and use mental math to build their number sense. Students should not follow a specific set of steps to solve.
- Variables are not limited to x; instruction includes using a variety of lowercase letters for their variables; however, o, i and l should be avoided as they too closely resemble zero and one.

Common Misconceptions or Errors

• Students may not see the connection to mental mathematics within the benchmark and instead try to apply rules and procedures when finding an unknown quantity.

- Instruction includes the use of fact family prompts of whole numbers to help guide students reasoning with positive rational numbers.
 - For example, the connection can be made between determining the unknown in the equation $3 \times \square = 15$ and in the equation $\frac{1}{3} \times \square = \frac{1}{15}$.



Teacher provides opportunities for students to identify the relationship between the • provided numbers and then co-solve the equation to determine the unknown.

Instructional Tasks

Instructional Task 1 (MTR.4.1)

Given the equation $0.5 = \frac{c}{0.15}$, describe a process or create a visual to explain how you can determine the value of *c*.

Instructional Task 2 (MTR.4.1)

If $\frac{2}{9} + g = \frac{8}{9}$, what value of g makes the equation true? Support your response with evidence.

Instructional Task 3 (MTR.7.1)

A solar panel can generate $\frac{8}{25}$ of a kilowatt of power. The average store needs to generate about 30 kilowatts of power.

Part A. Write an equation to determine how many solar panels a store needs on its roof. Part B. How many solar panels does a store need?

Instructional Items

Instructional Item 1

Determine the value of *m* in the equation 0.15m = 0.60.

Instructional Item 2

Given the equation $p - \frac{3}{5} = \frac{7}{10}$, what value of *p* could be a solution to the equation? **The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.*



MA.6.AR.3 Understand ratio and unit rate concepts and use them to solve problems.

MA.6.AR.3.1

Benchmark

MA.6.AR.3.1 Given a real-world context, write and interpret ratios to show the relative sizes of two quantities using appropriate notation: $\frac{a}{b}$, *a* to *b*, or *a*: *b* where $b \neq 0$.

Benchmark Clarifications:

Clarification 1: Instruction focuses on the understanding that a ratio can be described as a comparison of two quantities in either the same or different units.

Clarification 2: Instruction includes using manipulatives, drawings, models and words to interpret part-to-part ratios and part-to-whole ratios.

Clarification 3: The values of *a* and *b* are limited to whole numbers.

Connecting Benchmarks/Horizontal Alignment	Terms from the K-12 Glossary
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- MA.6.NSO.2.1, MA.6.NSO.2.2
- MA.6.NSO.3.5

Vertical Alignment

Previous Benchmarks

- MA.4.FR.1.3
- MA.5.FR.1.1

Purpose and Instructional Strategies

In grade 4, students identified and generated equivalent fractions, and in grade 5, students represented the division of two whole numbers as a fraction. This was a foundation for ratio relationships relating parts to wholes. In grade 6, students work with ratios that can compare parts to whole or parts to parts. In grade 7, students use ratio comparisons in multi-step problems that may also involve percentages.

- A ratio describes a multiplicative comparison that relates quantities within a given situation. Instruction emphasizes the understanding of the concept of a ratio and its similarities to a fraction and division.
- When working with ratios in context, the context should drive the form of the ratio.
 - For example, there are 42 students on a school bus. 12 students are girls and the rest are boys. What is the ratio of girls to boys on the school bus? *It is not necessary to simplify this ratio since the unsimplified ratio, 12 to 30, is more descriptive of the actual number of students on the bus.*
- Allow student flexibility in accepting both simplified and non-simplified responses. This provides an opportunity for students to have discussions about why they have different responses and to connect various forms of a ratio to equivalent fractions (*MTR.4.1*).
- Instruction includes the use of manipulatives and models to represent ratios. Manipulatives and models include snap cubes, marbles, bar models, number lines or ratio tables to help visually represent the relationship. Students can also act out the ratio relationship in the classroom to help with visualization (*MTR.2.1*).
 - Bar Models The ratio of toy cars to toy airplanes in Andrew's collection is 3:5.



Next Benchmarks • MA.7.AR.3.1



• Number Lines *The ratio of toy cars to toy airplanes in Andrew's collection is 3:5.*



- Ratio Tables
 - The ratio of toy cars to toy airplanes in Andrew's collection is 3:5.



- Students should be able to write ratio relationships in all three forms: fraction, using "to", or with a colon (:) between two numbers. They are not expected to write it in all three forms for every problem.
- Instruction includes writing the ratio and interpreting its meaning in the provided realworld context (*MTR.5.1*, *MTR.7.1*).
- Ratios can compare quantities of any kind, including counts of people or objects, measurements of length, weight and time.
- Problem types include providing real-world context with written descriptions, charts and tables.
- In some cases, the context of a problem determines a specific ratio, as well as the order in which a ratio is written.
 - For example, there are 2 blue marbles and 5 red marbles. Write the ratio of red marbles to blue marbles.
 - Acceptable responses: 5:2, 5 to 2 or $\frac{5}{2}$.
- In other cases, the context of a problem does not determine the order in which a ratio is written, and it may involve more than one ratio.
 - For example, there are 2 blue marbles and 5 red marbles. Write a ratio relationship.
 - Acceptable responses: 2:5,5:2,2 to 7,7 to 2, $\frac{5}{7}$ or $\frac{7}{5}$.

Common Misconceptions or Errors

- Students may incorrectly reverse the order of a ratio when a question does specify the order. To address this misconception, students can color code or write the order of the description before assigning the numbers to the ratio.
- Students may not recognize simplified forms of ratios. It is not required that students determine the simplified version of a ratio, but when comparing the ratios with other students and seeing different numbers, students should become more adept at seeing both ratios as representing the same relationship. The student should be reminded of the connection to equivalent fractions.



Strategies to Support Tiered Instruction

- Instruction includes using colored pencils to identify the units in each corresponding portion of a ratio and identifying the units before writing the numerical values.
 - For example, Leslie and Sabrina are both running for class president. If for every two votes Leslie receives, Sabrina receives five, describe the relationship between the number of votes Leslie receives to the number of votes Sabrina receives as a ratio.

Leslie's votes to Sabrina's votes

2 to 5, or 2:5, or $\frac{2}{5}$

- Instruction includes the use of two different counters to represent the provided ratio to allow for students to explore equivalent ratios by adding additional sets of counters or by dividing the existing counters into equal groups.
- Teacher reminds students of the connection between ratios and equivalent fractions.

Instructional Tasks

Instructional Task 1 (MTR.4.1, MTR.7.1)

To make the color purple, Jamal's art teacher instructed him to mix equal parts of red paint and blue paint. To make a different shade of purple, the ratio of red paint to blue paint is 2:1. What does the ratio 2:1 mean? Would a ratio of 1:2 make the same color? Why or why not?

Instructional Task 2 (MTR.4.1)

Mr. Keen, a band teacher, wanted to know if certain types of instruments are more appealing to one grade level or another. So, he conducted a survey of his students' preferences. The results are compiled in the chart below.

Instruments	6 th graders	7 th graders	
Strings	15	26	
Woodwind	19	36	
Brass	27	13	
Percussion	39	25	

Part A. What is the ratio of the number of 6th graders preferring woodwind instruments to the number of 7th graders preferring woodwind instruments?

- Part B. What is the ratio of the number of 7th preferring percussion instruments to the total number of 7th surveyed?
- Part C. What does the ratio of 27:40 represent? Does the ratio of 40 to 27 represent the same concept? Why or why not?



Instructional Items

Instructional Item 1

Ana and Robbie both stayed after school for help on their math homework. Ana stayed for 15 minutes and Robbie stayed for 50 minutes. Write a ratio to represent the relationships between the time that Ana stayed for help and the time that Robbie stayed for help.

Instructional Item 2

Leslie and Sabrina are both running for class president. If for every two votes Leslie receives, Sabrina receives five, describe the relationship between the number of votes Leslie receives to the number of votes Sabrina receives as a ratio.

Instructional Item 3

Miss Williams asked her class if they prefer doing their homework before school or after school. If the ratio of students who prefer doing homework before school to students who prefer doing homework after school is $\frac{7}{15}$, what does the ratio $\frac{7}{15}$ represent? Explain. *The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.

MA.6.AR.3.2

Benchmark					
MA.6.AR.3.2	Given a real-world context, determine a ra different units. Calculate and interpret the	1			
Example:	Tamika can read 500 words in 3 minutes. Her response to the unit rate of $\frac{500 \ words}{3 \ minutes}$ which is equivalent to the unit rate of				
Clarification 1: 1 connections betw Clarification 2: 1	Benchmark Clarifications: Clarification 1: Instruction includes using manipulatives, drawings, models and words and making connections between ratios, rates and unit rates. Clarification 2: Problems will not include conversions between customary and metric systems. Connecting Benchmarks/Horizontal Alignment				
• MA.6.N	ISO.2.1, MA.6.NSO.2.2,	• Rate			
MA.6.N	JSO.2.3	• Unit Rate			
Vertical Ali	gnment				
Previous Benchmarks Next Benchmarks					
• MA.5.FF	R.1.1 • MA	.7.AR.4.2			

- MA.5.FR.1.1
- MA.5.AR.1.2, MA.5.AR.1.3



Purpose and Instructional Strategies

In grade 5, students represented the division of two whole numbers as a fraction. In doing this, students started to work with a ratio relationship that relates parts to wholes. In grade 6, students extend this concept to include rates, which are ratios between quantities that are most often in different units. Students use ratio relationships to describe unit rates and percentage relationship and use the division of positive rational numbers to calculate unit rates from rates. In grade 7, students learn that a unit rate is the same as a constant of proportionality in a proportional relationship between two variables.

- Instruction connects rate and unit rate to student understanding of equivalent fractions from elementary school in both numeric and picture or model forms. Students can use the models to represent the situations in different ways (*MTR.5.1*).
- Allow student flexibility in accepting both simplified and non-simplified responses for rates unless unit rate is the specified or expected form.

Common Misconceptions or Errors

- Students may incorrectly identify what is being compared or the order of quantities being compared by the rate.
- Students may have difficulty connecting a unit rate, which is represent by a single number, to a ratio or non-unit rate, which may be represented by two numbers.

Strategies to Support Tiered Instruction

- Instruction includes the use of manipulatives and models to represent the provided rates and then to use multiplicative reasoning to determine the rate of one unit. Manipulatives and models include snap cubes, marbles, bar models, number lines or rate tables to help visually represent the relationship.
- Instruction includes the use of manipulatives to allow for students to explore the meaning of a unit rate. The teacher should provide two different counters to represent a rate equivalent to a whole number unit rate and then co-model the division of the counters into equal groups to determine how many counters of one color are needed to represent a single counter of the other color.
 - For example: At the grocery store, you paid \$9.00 for 3 pounds of apples. What is the unit price paid per pound of apples?



Instructional Tasks

Instructional Task 1 (MTR.6.1, MTR.7.1)

In buying ground beef for hamburgers, there are several packages from which to choose as shown in the table below.

pounds of ground beef	1.5	2	3	3.75
cost	\$5.58	\$7.44	\$11.16	\$13.95

- Part A. Predict how much it would cost for a pound of beef. Explain why your prediction is reasonable.
- Part B. What is the unit cost of the ground beef? Does the unit cost differ by the package size at this store?



Instructional Task 2 (MTR.4.1)

The Jones family is planning on expanding their garden so that they can plant more vegetables. The ratio of the area of the old garden to the area of the new garden is $4\frac{1}{4}:8\frac{3}{4}$. Convert this ratio to a unit rate and explain what it means in this context.

Instructional Task 3 (MTR.2.1, MTR.4.1, MTR.5.1)

Stephen is tracking the number of miles traveled to the number of minutes passed while traveling. He discovered that in 8 minutes he traveled 6 miles.

Part A. In your group, use the chart below to determine the rate and unit rate in miles per minute.

Part B. Which form would be most efficient for this context? Why?

Ratio	Rate	Unit Rate
	Fractional representation	Fractional representation
	Bar Model	Bar Model
	Number line	Number line
	Ratio table	

Instructional Items

Instructional Item 1

At the grocery store, you paid \$9.87 for 3.3 pounds of apples. What is the unit price paid per pound of apples?

Instructional Item 2

Brenda wants to buy one of the three cereals listed below. Determine which box is the best buy. Show and explain how you determined this.

- 16 ounces of Frosted Flurries for \$3.50
- 12.4 ounces of Chocolate O's for \$2.42
- 11.5 ounces of Cinnamon Grahams for \$2.35

*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.



MA.6.AR.3.3

Benchmark

MA.6.AR.3.3 Extend previous understanding of fractions and numerical patterns to generate or complete a two- or three-column table to display equivalent part-to-part ratios and part-to-part-to-whole ratios.

Example: The table below expresses the relationship between the number of ounces of yellow and blue paints used to create a new color. Determine the ratios and complete the table.

Yellow (part)	1.5	3		9
Blue (part)	2	4		
New color (whole)			12	21

Benchmark Clarifications:

Clarification 1: Instruction includes using two-column tables (e.g., a relationship between two variables) and three-column tables (e.g., part-to-part-to-whole relationship) to generate conversion charts and mixture charts.

Connecting Benchmarks/Horizontal Alignm	nent Terms from the K-12 Glossary
• MA.6.NSO.2.1, MA.6.NSO.2.2,	• Rate
MA.6.NSO.2.3	• Unit Rate
• MA.6.AR.2.2, MA.6.AR.2.3	
Vertical Alignment	
Previous Benchmarks	Next Benchmarks

 Previous Benchmarks
 Next Benchmarks

 • MA.5.FR.1.1
 • MA.7.AR.3.2

 • MA.5.FR.2.1, MA.5.FR.2.2
 • MA.7.AR.4.1, MA.7.AR.4.2, MA.7.AR.4.3, MA.7.AR.4.4

Purpose and Instructional Strategies

In elementary grades, students developed understanding of fraction concepts and operations, often in the context of the relationship that relates parts to wholes. In grade 6, students use tables to display parts to parts and parts to whole relationship, as preparation for understanding a constant ratio relationship between two quantities. In grade 7, students will achieve a more formal understanding of the constant of proportionality and proportional relationships, which can be represented by tables, equations and graphs.

- Instruction includes discussion about how the patterns that students see in the tables can help them reason through various situations (*MTR.4.1, MTR.5.1*).
- Instruction includes the use of acting out scenarios, bar models, tables and number lines in order to see relationships and relevance to real-world application (*MTR.2.1*).
 - Bar Model



o Tables





Common Misconceptions or Errors

• Students may be looking for arithmetic or counting patterns within the table and not seeing multiplicative patterns between the ratio values.

- Instruction includes the use of whole number parts to allow for students to explore the various relationships in the tables before introducing positive rational values. Discussions include additive and multiplicative patterns amongst the rows and the columns of the table.
- Instruction includes the use of two different counters to represent the provided ratios with emphasis on the different colors representing the parts and the total number of counters representing the whole. Teacher allows for opportunities for the student to explore equivalent ratios by adding addition sets of counters or by dividing the existing counters into equal groups and recording the equivalent ratios in a two- or three-column table.
 - For example, students can use the counters to help complete the table to express the relationship between the number of students and the number of adults on a recent field trip.

Students (Red Counters)	3	6		
Adults (Yellow Counters)	1		3	
Total People (Total Counters)				16



Instructional Tasks

Instructional Task 1 (MTR.4.1, MTR.7.1)

Jeremy is making punch for a party. The relationship between the cups of syrup and the cups of water he used to create the punch mixture is shown on the table below.

Part A. Complete the table. Explain the process you used to complete the table.

$1\frac{3}{4}$	7	
3	12	
	15	$18\frac{3}{4}$
		20

Part B. If Jeremy needs 30 cups of punch, how many cups of syrup are needed? How many cups of water are needed?

Instructional Task 2 (MTR.3.1)

Given the table below, determine the common ratio between the x- and y-values.

x	у
2	8
5	20

Instructional Items

Instructional Item 1

Shambria is making pies and part of the recipe she uses is described in the table below.

Number of Pies	Cups of Sugar	Pounds of Apples
1	0.5	2.25
5		

Using this recipe, complete what is the amount of sugar and apples needed to bake 5 pies?

Instructional Item 2

The table below describes the same rate at which Drew hiked along the Appalachian Trail each day. Complete the table and determine how many miles he could hike in 2 hours.

time (hours)	5		2
distance (miles)	20	12	

*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.



MA.6.AR.3.4

Benchmarl	ĸ		
MA.6.AR.3.4	Apply ratio relationships t involving percentages usir		atical and real-world problems ip between two quantities.
Example	a protein shake that contain 32	2 grams and the er	nsume more protein every day. If he has ntire shake is 340 grams, what is the ratio between grams of protein
Benchmark Clar	ifications:		
Clarification 1: 1	Instruction includes the compari	son of $\frac{part}{whole}$ to $\frac{pe}{pe}$	$\frac{rrcent}{100}$ in order to determine the percent,
the part or the wl		whole	
Connecting	g Benchmarks/Horizontal A	lignment	Terms from the K-12 Glossary
• MA.6.	NSO.2.1, MA.6.NSO.2.2,		• Rate
MA.6.	NSO.2.3		
• MA.6.	NSO.3.5		
• MA.6.	AR.2.3		
Vertical Al			
Previous Benc	hmarks	Next Bench	ımarks
• MA.5.N	ISO.2.1, MA.5.NSO.2.2	• MA.	.7.AR.3.1
• MA.5.F	R.1.1		
Purpose an	nd Instructional Strategies		
In elementary g	rades, students worked with	creating equivale	ent fractions, as well as operations

In elementary grades, students worked with creating equivalent fractions, as well as operations with whole numbers and fractions. In grade 6, students use ratio relationships to solve problems involving percentages. In grade 7, students will solve multi-step problems and proportional relationships involving percentages.

- Students should understand that percent (%) represents a part to whole relationship.
- Instruction includes the connection to ratio relationships to determine the part, the whole or the percentage (*MTR.5.1*).
 - For example, when determining the how much 40% is of 24, students should compare the ratio $\frac{x}{24}$ to the ratio $\frac{40}{100}$.
- Instruction does not include the use of proportions or cross multiplication to solve problems involving percentages.
- Instruction includes the use of models to represent percentages such as bar models, number lines or ratio tables to help visually represent the relationship (*MTR.2.1*).
 - o Bar Models

$70\% \ of \ 120 = 84$									
10%	10%	10%	10%	10%	10%	10%	10%	10%	10%
12	12	12	12	12	12	12	12	12	12

• Number Lines

70% of 120 = 84





• Ratio Tables

70% of 120 = 84					
percent	100%	50%	10%	70%	
total 120 60 12 84					

Common Misconceptions or Errors

- Students may not understand the difference between an additive relationship and a multiplicative relationship.
- Students may incorrectly set up ratios because of a misunderstanding of the part and the whole addressed in the situation.
- Students may not recognize simplified forms of ratios in order to find equivalent ratios to determine the percentage, the whole or the part.

Strategies to Support Tiered Instruction

- Instruction includes finding an equivalent unit rate (either part or whole) then multiplying to find the desired equivalent ratio.
 - For example: Steve wants to determine how much a 15% tip is if the bill is \$80.00.

Use a visual representation to show 80 represents 100%

		Par	rt		80			
		Per	Percent		100			
Divide the ratio by 80								
		Part		80		1		
		Percent		100		1.25		
Multiply the resulting ratio by 15								
	Part		80		1		12	
	Perce	nt	100		1.25		15	

Using the equivalent ratios, 12 is 15% of 80, so the tip is \$12.00.

Instructional Tasks

Instructional Task 1 (MTR.4.1, MTR.6.1, MTR.7.1)

Carlos predicts that his math homework will take him 60 of the total of 75 minutes he has available for homework tonight.

- Part A. At this rate, how many minutes would Carlos spend on math homework out of a total of 100 available minutes?
- Part B. What percentage of the available homework time does Carlos predict he will spend doing math? Explain how the answer to this question is related to the answer in Part A.

Instructional Items

Instructional Item 1

Find the percent equivalent to $\frac{60}{115}$. Round to the nearest tenth percent.



Instructional Item 2

15% of 80 is what value?

Instructional Item 3

Sami is keeping track of the amount of salt she consumes each day. According to the label on her macaroni and cheese box, one serving contains 470 mg of sodium (salt). If 470 mg is 20% of the recommended daily amount, how many milligrams of sodium are recommended for the whole day?

*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.

MA.6.AR.3.5

Benchmark				
MA.6.AR.3.5	Solve mathematical and real rates, including comparisons within the same measurement	, mixtures, rat		
Benchmark Clarif		aa tama diaanam		
-	astruction includes the use of tabl Benchmarks/Horizontal Alig			ms from the K-12 Glossary
• MA.6.N	ISO.2.1, MA.6.NSO.2.2,		٠	Customary units
MA.6.N	NSO.2.3		٠	Metric units
• MA.6.N	JSO.3.5		•	Rate
• MA.6.A	AR.1.1		•	Unit Rate
• MA.6.A	AR.2.3			
Vertical Ali	gnment			
Previous Bench	marks	Next Bench	ımark	ΣS
• MA.5.FF	R.1.1	• MA.	.7.AR	.3.1, MA.7.AR.3.2,
• MA.5.FF	R.2.1	MA	.7.AR	.3.3
• MA.5.Al	R.1.2, MA.5.AR.1.3			



Purpose and Instructional Strategies

In elementary grades, students developed understanding of fraction concepts and operations, often in the context of the relationship that relates parts to wholes. In grade 6, students solve problems involving ratio relationships. In grade 7, students will solve problems involving proportional relationships. This benchmark is the culmination of the MA.6.AR.3 standard. It combines all of the concepts developed in the previous four benchmarks and applies them to a variety of mathematical and real-world contexts, including conversions of units within a measurement system. In grade 7, students are expected to convert units across different measurement systems.

- Instruction includes a variety of problem types including comparison, mixtures, lengths and conversions. Students should work within the same measurement system, for example, standard measurement to standard measurement or metric system to metric system.
- It is not the expectation of this benchmark to solve problems using proportions; however, problem types will naturally start to build the foundation of proportions and proportional relationships.
- Instruction includes the use of bar models, tables and number lines to help students see relationships and relevance to real-world application (*MTR.2.1*).
 - For example, 3 toy cars cost Mikela \$5 at the local superstore. Mikela needs 18 toy cars. How much will it cost Mikela to buy the cars?
 - Bar Models



- Discussion about why students used certain methods to solve specific problems can help students see the patterns for determining their own processes in the future (*MTR.2.1*, *MTR.5.1*, *MTR.7.1*).
- Instruction includes many opportunities for converting between units in the same measurement system, including conversions of areas and volumes and conversions that are commonly used in the science classroom.

Common Misconceptions or Errors

• Some students may struggle to determine a process for solving in real-world context problems. Instruction highlights strategies for students to build perseverance by modifying methods as needed and analyze the problem in a way that makes sense (*MTR.1.1*).



- Teacher provides opportunities for students to comprehend the context or situation by engaging in questions (writing questions on flash cards to reuse will be useful) such as:
 - What do you know from the problem?
 - What is the problem asking you to find?
 - Can you create a visual model to help you understand or see patterns in your problem?
- Instruction includes using colored pencils to identify the units in each corresponding portion of a ratio and identifying the units before writing the numerical values.
- Instruction includes the use of a three-read strategy. Students read the problem three different times, each with a different purpose.
 - First, read the problem with the purpose of answering the question: What is the problem, context, or story about?
 - Second, read the problem with the purpose of answering the question: What are we trying to find out?
 - Third, read the problem with the purpose of answering the question: What information is important in the problem?
- Instruction highlights strategies for students to build perseverance by modifying methods as needed and analyzing the problem in a way that makes sense.

Instructional Tasks

Instructional Task 1 (MTR.7.1)

On the first day of camp, Sara hiked 20 miles in 5 hours.

- Part A. At this rate, how long would it take Sara to hike 12 miles? Show and explain how you determined this.
- Part B. At this same rate, how many miles could Sara hike in 2 hours? Show and explain how you determined this.

Instructional Task 2 (MTR.7.1)

Chris and Jenny are comparing two similar punch recipes. Each recipe calls for cranberry juice and ginger ale but in different amounts. The tables below show the amounts of cranberry juice and ginger ale for four different quantities of punch.

Chris's	Punch	Jenny's	9 Punch
Cranberry Juice (in cups)	Ginger Ale (in cups)	Cranberry Juice (in cups)	Ginger Ale (in cups)
1	4	2	3
2	8	4	6
3	12	6	9
5	20	10	15

- Part A. Is the ratio of the punch that is cranberry juice the same in each of Chris's recipes given in his table? Explain how you determined your answer.
- Part B. Is the ratio of the punch that is cranberry juice the same in each of Jenny's recipes given in her table? Explain how you determined your answer.
- Part C. Is the ratio of the punch that is cranberry juice the same in Chris's recipes as it is in Jenny's recipes? If not, whose punch has a greater concentration of cranberry juice? Explain how you determined your answer.

Instructional Items



Instructional Item 1

A recent study found that parking lots for offices should have a ratio of 6 spaces for every 1000 square feet of floor space. If a new office building has 19,000 square feet of floor space, how many spaces should there be in the parking lot?

Instructional Item 2

Jessica made 8 out of 24 free throws. Bob made 5 out of 20 free throws. Who has the highest free throw ratio?

*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.



Geometric Reasoning

MA.6.GR.1 Apply previous understanding of the coordinate plane to solve problems.

MA.6.GR.1.1

Benchmark			
MA.6.GR.1.1	Extend previous understanding of the ordered pairs in all four quadrants and as the line of reflection when two orde coordinate.	d on both a	axes. Identify the x - or y -axis
Connecting	Benchmarks/Horizontal Alignment	Te	rms from the K-12 Glossary
• MA.6.N	ISO.1.1, MA.6.NSO.1.2,	•	Axes (of a graph)
MA.6.N	JSO.1.4	•	Coordinate Plane
		•	Coordinate
		•	Origin
		•	Quadrant
Vertical Ali	gnment		
Previous Bench	marks Next B	Benchmar	ks
• MA.5.Gl	R.4.1 •	MA.7.AF	R.4.1, MA.7.AR.4.3

• MA.8.GR.2.3

Purpose and Instructional Strategies

In grade 5, students plotted and labeled ordered pairs of whole numbers in the first quadrant. Students in grade 6 plot ordered pairs of rational numbers in all four quadrants. In grade 7, students will apply their knowledge of the plotting of ordered pairs to the graphing of proportional relationships.

- Instruction includes making connections to opposites on a number line and absolute value, as well as to reflections across the *x* and *y*-axes.
- Instruction includes using academic terminology including calling ordered pairs as coordinates and as a coordinate pair.
- Instruction includes students' plotting ordered pairs on graphs with different scales.
 - For example, students can plot the ordered pair $(\frac{1}{2}, 3)$, where the *x* and *y*-axis have a scale of 2 or a scale of 0.5.



Common Misconceptions or Errors

- Students may switch the location of the *x*-coordinate and the *y*-coordinate in the ordered pair.
- Students may misunderstand that a point on an axis has at least one coordinate of zero.
 - For example, the point on the graph identified as (3,0) may have a student incorrectly identify the location as (3,3) or just 3.
- Students may misunderstand the numbering of the four quadrants (upper right in a counter-clockwise rotation) as well as which coordinate is positive and which coordinate is negative.

- Teacher creates an anchor chart while students create their own graphic organizer to include key features of a coordinate plane. Features include the *x*-axis, *y*-axis, origin, quadrants, and an ordered pair.
- Instruction includes building connections to plotting points on number lines. On one sheet of tracing paper, label a horizontal number line as the *x*-axis and plot the *x*-value. On another sheet of tracing paper, label a vertical number line as the *y*-axis and plot the *y*-value. Overlap the two number lines with a point of intersection at the origin (0,0). Place a third sheet of tracing paper on top of the two number lines, trace and label the *x*-axis to produce a coordinate plane. The location of a new point should then be plotted in the appropriate quadrant to represent the horizontal and vertical locations of the two previously plotted points. This same strategy helps to draw connections to a point laying on an axis if one of the coordinates is zero.
- Teachers may provide instruction on using reasonable estimations when plotting rational coordinates on the coordinate plane.
 - For example, if a student is plotting $-4\frac{3}{5}$ for an x-value and 3 for y-value, they need to know that $\frac{3}{5}$ is more than half, so to graph the x-value, they should plot a point between -4 and -5, with the point closer to the -5. Then the student can more precisely adjust the point if necessary (if any other value is between -4 and -5 they can adjust, but if not, they will see that their estimation will be a valid way to order.)
- When plotting rational coordinates, teacher provides a coordinate plane with an appropriate scaling to match the fractional or decimal units so the points graphed will fall on the intersection of two minor grid lines.
 - For example, if a student is graphing the ordered pair (-0.5, 2.25) the x- and y-axis could have a scale of 0.25.



Instructional Tasks

Instructional Task 1 (MTR.3.1)

Part A. On a graph paper, draw a coordinate grid. Label the axis and plot the ordered pairs below.

•	$A\left(2,\frac{5}{2}\right)$	• $E(0,0)$
	B(-4,5)	● <i>F</i> (2, −8)
	C(-4,-7)	• $G(0, 0.6)$
•	$D\left(\frac{3}{2},-5\right)$	• <i>H</i> (-4,-5)

Part B. Which ordered pair(s) are located on an axis?

Part C. Which points are in quadrant III?

Part D. Which points are a reflection of each other and over which axis are they reflected?

Instructional Task 2 (MTR.4.1)

- Part A. Create a picture with fewer than 20 coordinates in the four quadrants. Write your coordinates on a separate piece of paper.
- Part B. Trade your list of ordered pairs with a partner. Recreate your partner's picture on a new sheet of graph paper.
- Part C. Discuss differences and discuss possible errors you or your partner may have made when recreating each other's pictures.

Instructional Task 3 (MTR.4.1)

If given x > 0 and y > 0, in which quadrant or axis will each ordered pair described below lie? Explain your answer.

- a. (-x, y)
- b. (-*x*, 0)
- c. (x, -y)
- d. (0, y)

Instructional Items

Instructional Item 1

What is the value of the *x*-coordinate of the ordered pair that reflects $\left(5\frac{1}{2}, -8\right)$ over the *y*-axis?

Instructional Item 2

Using the graph below, state the ordered pair that describes the point plotted in Quadrant II?



*The strategies, tasks and items included in the B1G-M are examples and should not be considered comprehensive. MA.6.GR.1.2



Benchmark

MA.6.GR.1.2 Find distances between ordered pairs, limited to the same *x*-coordinate or the same *y*-coordinate, represented on the coordinate plane.

Connecting Benchmarks/Horizontal Ali	gnment Terms from the K-12 Glossary
• MA.6.NSO.1.1, MA.6.NSO.1.2,	• Axes (of a graph)
MA.6.NSO.1.3, MA.6.NSO.1.4	Coordinate
• MA.6.NSO.4.1	Coordinate Plane
• MA.6.AR.2.4	Origin
	Quadrant
Vertical Alignment	-
Previous Benchmarks	Next Benchmarks
• MA.5.GR.4.2	• MA.8.GR.1.2

Purpose and Instructional Strategies

Throughout the elementary grades, students have used the number line to model subtraction as the distance between two points. In grade 6, this connection has been extended to negative integers, and in this benchmark, it extends to the distance between ordered pairs of rational numbers in the four quadrants, if they share a coordinate. This prepares students in a visual way for the subtraction of rational numbers in grade 7. And in grade 8, students will find distances between any two ordered pairs using the Pythagorean Theorem.

- Instruction connects student understanding of MA.6.NSO.1 to the coordinate plane. Strategies include using absolute value to find the distance between two ordered pairs. Even though in grade 6, students are adding and subtracting integers, this benchmark focuses on using absolute value to explore addition and subtraction of rational numbers.
 - For example, the points (4, 9) and (4, -6) are plotted on a coordinate grid.



Students can use the absolute value of the first y-coordinate, 9, and the second y-coordinate, -6, and add these numbers together to determine the distance is 15.

- When using rational numbers, instruction is restricted to numbers within the same form. Students should not be penalized though if they convert from one form to another when performing operations.
 - For example, if students are working with fractions, the ordered pairs will not include decimals. If students are working with decimals, the ordered pairs will not include fractions.
- Students should be given the opportunity to find the distance between the ordered pairs both on and off of a graph.

Common Misconceptions or Errors

- Students may have trouble finding the distance across either of the axes.
 - For example, find the distance between (-4, 3) and (5, 3). It may appear that the "difference" between -4 and 5 is 1. However, the distance from -4 to 0 is 4



units and from 0 to 5 is 5 units. Therefore, the distance between the two points is 9 units.

- Students may misunderstand that a point on an axis has at least one coordinate of zero.
 - For example, the points (0, 8) and (4, 0) are graphed on the coordinate plane.



• Some students may incorrectly believe that the points represent (8,8) and (4,4) or just (8) and (4).

- Instruction includes using two notecards and covering empty portions of the coordinate plane to focus attention on the space between two provided points. Students can then count the number of spaces between the two points, paying attention to scaling.
- If points are not already placed on a coordinate plane, students may plot the points to create a visual representation of the distances created.
- Instruction includes building connections to plotting points on number lines. On one sheet of tracing paper, label a horizontal number line as the *x*-axis and plot the *x*-value. On another sheet of tracing paper, label a vertical number line as the *y*-axis and plot the *y*-value. Overlap the two number lines with a point of intersection at the origin (0,0). Place a third sheet of tracing paper on top of the two number lines, trace and label the *x*-and *y*-axis to produce a coordinate plane. The location of a new point should then be plotted in the appropriate quadrant to represent the horizontal and vertical locations of the two previously plotted points. This same strategy helps to draw connections to a point laying on an axis if one of the coordinates is zero.
- Instruction includes creating connections back to finding distance on a number line. Lay a piece of tracing paper on top of the provided coordinate plane, trace the points, and draw a number line through the two points, paying close attention to the scaling. Once the number line is down, remove the tracing paper and find the distance between the two points on the number line.



Instructional Tasks

Instructional Task 1 (MTR.6.1)

On a coordinate grid, Perry is planning a future town by labeling different buildings. Each unit on the coordinate plane is equivalent to 0.5 miles.

- Town Hall (2,5)
- Fire Station (-4, 5)
- Library (-4, -7)
- Ice Cream Shop (3, -5)
- Central Park (0, 0)
 Grocery Store (2, -8)
- Police Station (0, 6)
- Gas Station (-4, -5)
- Part A. What is the distance, in miles, from the Fire Station to the Library?
- Part B. How far, in miles, would the Mayor, located at Town Hall, have to walk to get to the grocery store?
- Part C. Compare a walk from Central Park to the Police Station and a walk from the Gas Station to the Ice Cream Shop. Which one is further?
- Part D. Using what you have learned can you determine how far Perry would have to ride his bike, in miles, if he is starting at Central Park and going to the Ice Cream Shop and can only travel North, South, East or West.

Instructional Task 2 (MTR.3.1)

André is located at (-5,3), Boris is located at (-1,3) and Carlos is located at (-5,-2). Determine the distance between André and Boris. Then determine the distance between André and Carlos. Show your work.

Instructional Items

Instructional Item 1

The points (0.4, -6) and (1.9, -6) represent the location of two towns on a coordinate grid, where one unit is equal to one mile. What is the distance, in miles, between the two towns?

Instructional Item 2

If the distance between two points is 7 units and one of the points is located at (-6, 3), what could be the coordinates of the other point?

*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.

MA.6.GR.1.3

Benchmark

MA.6.GR.1.3 Solve mathematical and real-world problems by plotting points on a coordinate plane, including finding the perimeter or area of a rectangle.

Benchmark Clarifications:

Clarification 1: Instruction includes finding distances between points, computing dimensions of a rectangle or determining a fourth vertex of a rectangle.

Clarification 2: Problems involving rectangles are limited to cases where the sides are parallel to the axes. **Connecting Benchmarks/Horizontal Alignment Terms from the K-12 Glossary**

- MA.6.NSO.1.1, MA.6.NSO.1.2, MA.6.NSO.1.3, MA.6.NSO.1.4
- Area
- Axes (of a graph)



- MA.6.NSO.4.1 •
- MA.6.AR.2.4

- Coordinate •
- **Coordinate Plane**
- Origin
- Quadrant

Vertical Alignment

Previous Benchmarks

• MA.5.GR.2.1

Next Benchmarks

• MA.7.GR.1.1

Purpose and Instructional Strategies

Students will be able to extend their understanding from grade 5 of finding the perimeter and area of rectangles using models and formulas, to plotting the points on a coordinate plane and determining the perimeter or area in grade 6. Students will also need to find the missing coordinate before determining the perimeter or area (MTR.1.1, MTR.2.1). Students will extend their knowledge to find the areas of other quadrilaterals in grade 7.

- Students will be able to find the area and perimeter of rectangles only if their side lengths are parallel to the axes (MTR.6.1).
- Instruction connects student understanding of MA.6.NSO.1 to the coordinate plane. Strategies include using absolute value to find the distance between two ordered pairs. Even though in grade 6, students are adding and subtracting integers, this benchmark focuses on using absolute value to explore addition and subtraction of rational numbers.
 - For example, the points (4, 9) and (4, -6) are plotted on a coordinate grid.



Students can use the absolute value of the first y-coordinate, 9, and the second ycoordinate, -6, and add these numbers together to determine the distance is 15.

- Instruction includes opportunities to find partial areas and partial perimeters in real world context. When discussing area and perimeter, allow the flexibility for problems and students to use base and height or to use length and width.
 - For example, Nathanial is building a garden in his backyard. His uncle has made a map of the backyard with a grid on it to help them plan out where the garden should go, where each box on the grid is equivalent to one meter. If Nathanial's garden has corners at (0, 9), (8, 9), (0, 2) and (8, 2). The y-axis represents the fence in his backyard. What is the perimeter of wood needed to create a barrier for the garden?

Common Misconceptions or Errors

- Students may switch the location of the *x*-coordinate and the *y*-coordinate in the ordered pair.
- Students may confuse the difference between perimeter (distance around a figure) with area (the total measure of the inside region of a closed two-dimensional figure).



- Instruction includes using two notecards and covering empty portions of the coordinate plane to focus attention on the space between two provided points. Students can then count the number of spaces between the two points, paying attention to scaling.
- If points are not already placed on a coordinate plane, students may plot the points to create a visual representation of the distances created.
- Instruction includes creating connections back to finding distance on a number line in order to determine the perimeter or area of a rectangle.
 - For example, the teacher can model finding the perimeter by laying a piece of tracing paper on top of the provided coordinate plane, trace the points, and draw a number line through the two points of one side of the rectangle, paying close attention to the scaling. Once the number line is down, remove the tracing paper and find the distance between to the two points on the number line. Repeat this for all sides and then add the distances together to determine the perimeter.
 - For example, the teacher can model finding the area by laying a piece of tracing paper on top of the provided coordinate plane, trace the points, and draw a number line through the two points of the length (or base) of the rectangle, paying close attention to the scaling. Once the number line is down, remove the tracing paper and find the distance between to the two points on the number line. Repeat this for the width (or height) and then multiply the length (or base) and width (or height) together to determine the area.
- Instruction includes the use of geometric software to help build upon the concepts of area and perimeter on a coordinate plane.

Instructional Tasks

Instructional Task 1 (MTR.5.1, MTR.6.1)

A square has a perimeter of 36 units. One vertex of the square is located at (3, 5) on the coordinate grid.

Part A. What could be the *x*- and *y*-coordinates of another vertex of the square? Part B. What is the area of the square?

Instructional Task 2 (MTR.3.1, MTR.5.1)

Sandy wants to find the area of a rectangular garden where one side is a side of her house. She graphed the garden on a coordinate plane so that three of the vertices are at:

(-3, -2), (4, -2) and (4, 4).

Part A. Find the coordinates of the fourth vertex so that the garden is a rectangle. Part B. Find the area of the garden, showing your work.

Part C. If Sandy wants to enclose the garden, what is the length of fencing needed? **Instructional Items**

Instructional Item 1

The corners of a rectangular swimming pool are located at (-4, -3), (-4, -8), (6, -3) and (6, -8). What is the perimeter of the swimming pool?

*The strategies, tasks and items included in the B1G-M are examples and should not be considered comprehensive.

MA.6.GR.2 Model and solve problems involving two-dimensional figures and three-dimensional figures.



MA.6.GR.2.1

Benchmark

MA.6.GR.2.1 Derive a formula for the area of a right triangle using a rectangle. Apply a formula to find the area of a triangle.

Benchmark Clarifications:

Clarification 1: Instruction focuses on the relationship between the area of a rectangle and the area of a right triangle.

Clarification 2: Within this benchmark, the expectation is to know from memory a formula for the area of a triangle.

Connecting Benchmarks/Horizontal Ali	ignment	Terms from the K-12 Glossary
• MA.6.NSO.2.1		Algorithm
• MA.6.AR.2.3		• Area
		• Rectangle
		• Triangle
Vertical Alignment		
Previous Benchmarks	Next Bench	nmarks
• MA.5.GR.2.1	• MA	.7.GR.1.2
Purpose and Instructional Strategies		

Students will use their understanding from grade 5 of models and formulas to find the area of a rectangle to derive the formula to find the area of a triangle (*MTR.1.1, MTR.2.1*). Students will extend this knowledge in grade 7 to decompose composite figures into triangles and quadrilaterals in order to find area.

- Instruction includes developing the understanding that two copies of any right triangle will always form a rectangle with the same base and height. Therefore, the triangle has an area of half of the rectangle, $A = \frac{1}{2}(base \times height)$. This understanding can develop from seeing how a triangle is constructed when cutting a rectangular piece of paper diagonally in half.
- Students should be flexible in their understanding of formulas to be able to use show the equivalency of $\frac{1}{2}bh$ and $\frac{bh}{2}$.
- Formulas can be a tool or strategy for geometric reasoning. Students require a solid understanding of two area concepts: (1) the area of a rectangle is *length* × *width* or *base* × *height*, and (2) figures of the same size and shape (congruent) have the same area.
- Instruction includes representing measurements for area as square units, units squared or units².
- Students should understand that any side of the triangle can be a base; however, the height can only be represented as a line segment drawn from a vertex perpendicular to the base. The terms height and altitude can be used interchangeably. Students should see the right-angle symbol, ⊾ to indicate perpendicularity.
- Problem types include having students' measure lengths using a ruler to determine the area.



Common Misconceptions or Errors

- Students may forget that multiplying by $\frac{1}{2}$ and dividing by 2 are the same operation.
- Students may neglect to apply the $\frac{1}{2}$ when finding the area of a triangle.
- Students may incorrectly identify a side measurement as the height of a triangle.

Strategies to Support Tiered Instruction

- Teacher models several problems solving them both ways (using a rectangle and using a formula) and then have the students solve them step by step guiding them to the answer. This will provide students with the opportunity to see that the two operations are identical.
- Teacher reinforces that a right triangle is half of a rectangle, therefore we must cut the area in half.
- Teacher models with geometric software so students can see that a right triangle is half of a rectangle, which is why we multiply by $\frac{1}{2}$.
- Teacher models the use of manipulatives that students can measure to better understand there is a difference between a side length and the height in non-right triangles.

Instructional Tasks

Instructional Task 1 (MTR.2.1, MTR.4.1)

Mrs. Lito asked her students to label a base b and its corresponding height h in the triangle shown.



Three students drew the figures below.



Part A. Which students, if any, have correctly identified a base and its corresponding height? Which ones have not? Explain what is incorrect.

Part B. There are three possible base-height pairs for this triangle. Sketch all three.

Instructional Task 2 (MTR.5.1) Look at the triangles below.





Determine and explain:

- Which triangle has the greatest area?
- Which triangle has the least area?
- Do any of the triangles have the same area?
- Are some areas impossible to compare?

Instructional Items

Instructional Item 1

Find the area of ΔDEF .



*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.



MA.6.GR.2.2

Benchmark		
MA.6.GR.2.2	Solve mathematical and real-world problem quadrilaterals and composite figures by dec rectangles.	
Benchmark Clarif	ications:	
Clarification 1: Problem types include finding area of composite shapes and determining missing		
dimensions.		
Clarification 2: Within this benchmark, the expectation is to know from memory a formula for the area of		
a rectangle and triangle.		
Clarification 3: Dimensions are limited to positive rational numbers.		
Connecting	Benchmarks/Horizontal Alignment	Terms from the K-12 Glossary
• MA.6.N	SO.2.1, MA.6.NSO.2.2,	• Algorithm

Previous Benchmarks	Next Benchmarks
Vertical Alignment	
	• Triangle
	Quadrilateral
• MA.6.AR.1.1	• Rectangle
MA.6.NSO.2.3	• Area
• $MA.0.NSO.2.1, MA.0.NSO.2.2,$	• Algorithm

• MA.5.GR.2.1

• MA.7.GR.1.2

Purpose and Instructional Strategies

Students will use their understanding from grade 5 of finding the perimeter and area of rectangles with fractional or decimal sides to finding the areas of quadrilaterals and composite figures with positive rational number side lengths in grade 6 (*MTR.1.1, MTR.2.1*). Students will extend this knowledge in grade 7 to decompose composite figures into triangles and quadrilaterals in order to find area.

- Instruction includes finding missing dimensions with quadrilaterals and composite figures (*MTR.1.1, MTR.5.1*).
- Instruction includes representing measurements for area as square units, units squared or units².
- When using rational numbers, instruction is restricted to numbers within the same form. Students should not be penalized though if they convert from one form to another when performing operations.
 - For example, if students are working with fractions, the side lengths will not include decimals. If students are working with decimals, the side lengths will not include fractions.
- Students should look for opportunities to either decompose or compose shapes to enhance their geometric reasoning.
 - For example, in the diagram below, students can solve by decomposing or by composing.

Area = $(18 \cdot 7) - \frac{1}{2}(6 \cdot 7) = 105 \text{ cm}^2$ Area = $(12 \cdot 7) + \frac{1}{2}(6 \cdot 7) = 105 \text{ cm}^2$

• Problem types include having students measure lengths using a ruler to determine the



area.

Common Misconceptions or Errors

- Students may invert the perimeter and area formulas.
- Students may incorrectly label all sides of the figure.
- Students may incorrectly identify a side of a triangle as the height.

Strategies to Support Tiered Instruction

- Teacher reviews the definitions of surface area and volume, and co-creates an anchor chart to display in the room explaining each. Providing flash cards or cue cards with the formulas will help students in place of anchor charts when they are outside the classroom area.
- Teacher models the use of different color markers or pencils to match similar sides when decomposing figures. This will help student accurately label the sides of each shape.
- Use manipulatives that students can measure to better understand there is a difference between a side length and the height in non-right triangles.
- Teacher models the use of manipulatives and geometric software to review the concept of perimeter or area.
- Teacher models the use of manipulatives shapes to reinforce the sides of the pieces that make up a decomposed figure.
- Teacher models the use of manipulatives that students can measure to better understand there is a difference between a side length and the height in non-right triangles.

Instructional Tasks

Instructional Task 1 (MTR.1.1, MTR.2.1, MTR.5.1)

The diagram shows the dimensions, in feet, of the local playground. While playing with friends, Shona lost the key to her diary somewhere in the dirt. By composing or decomposing into rectangles, determine the maximum number of square feet that Shona may need to search to find the missing key? If she only searched one rectangular area, what is the least number of square feet Shona searched?



Instructional Items

Instructional Item 1

A pentagon is shown. What is the area, in square inches, of the pentagon? Image not to scale.




Instructional Item 2

Mr. Moretti wants to cover the walkway around his swimming pool with tile. Determine how many square feet of tile he will need to cover the shaded portion of the diagram.



*The strategies, tasks and items included in the B1G-M are examples and should not be considered comprehensive.

MA.6.GR.2.3

Benchmark						
MA.6.GR.2.3	Solve mathematical and real-world problems involving the volume of right rectangular prisms with positive rational number edge lengths using a visual model and a formula.					
Benchmark Clarif						
	oblem types include finding the volu Benchmarks/Horizontal Alignm		sing dimension of a rectangular prism. Terms from the K-12 Glossary			
• MA.6.N	ISO.2.1, MA.6.NSO.2.2,		Algorithm			
MA.6.N	ISO.2.3		• Cube			
• MA.6.N	ISO.3.5		• Rectangular prism			
• MA.6.A	R.1.1					
• MA.6.A	R.2.3					
Vertical Ali	gnment					
Previous Bench	marks N	lext Benchr	narks			
• MA.5.GI	R.3.3	• MA.	7.GR.2.3			

Purpose and Instructional Strategies

Students in grade 5 found the volume of right rectangular prisms with whole-number edges. Students calculated the volume of right rectangular prisms (boxes) using whole-number edges with a unit cube of $1 \times 1 \times 1$. In grade 6, students will use this understanding and apply it to rational-number edge lengths of rectangular prisms. In grade 7, students will find the volume of right circular cylinders.



- Instruction includes exploring volume of the right rectangular prisms using fractional unit cubes.
 - For example, the right rectangular prism has edges of $1\frac{1}{4}$ inches, 1 inch and $1\frac{1}{2}$ inches. The volume can be found by recognizing that the unit cube would be $\frac{1}{4}$ inch of all edges, changing the dimensions to $\frac{5}{4}$ inches, $\frac{4}{4}$ inches and $\frac{6}{4}$ inches. The volume is the number of unit cubes making up the prism (5 × 4 × 6), which is 120 unit cubes each with the volume of $\frac{1}{64} = (\frac{1}{4} \times \frac{1}{4} \times \frac{1}{4})$. This can also be expressed as $(\frac{5}{4} \times \frac{6}{4} \times \frac{4}{4})$ or $(\frac{120}{64})$.
- "Know the formula" does not mean memorization of the formula. To "know" means to have an understanding of why the formula works and how the formula relates to the measure (volume) and the figure.
- Instruction includes measuring volume by filling rectangular prisms with blocks and looking at the relationship between the total volume and the area of the base. Through these experiences, students can derive the volume formula.
- When using rational numbers, instruction should stay within the same form. Students should not be penalized though if they convert from one for to another when performing operations.
 - For example, if students are working with fractions, the side lengths will not include decimals. If students are working with decimals, the side lengths will not include fractions.
- Instruction includes using the formula of V = Bh as well as the formula V = lwh. Students should know when and how to use each formula and be able to apply the formulas to real-world contexts.
 - When given a problem such as "The standard size of a construction brick is $2\frac{1}{4}$

inches by 8 inches by $3\frac{1}{2}$ inches. Find the volume of one brick." There are three measurements given. Therefore, the formula, V = lwh, would be the most appropriate formula.

• When given a problem such as "The floor of a cargo truck is $22\frac{1}{2}$ square feet.

What is the volume of the storage space in cubic feet if the truck is $7\frac{1}{5}$ feet high?", there are two measurements given with one being the area of a base. Therefore, the formula V = Bh would be the most appropriate formula.

- Instruction includes representing measurements for volume as cubic units, units cubed or units³.
- Problem types include having students measure lengths using a ruler to determine the area.

Common Misconceptions or Errors

- Students may invert the formulas for surface area and volume.
- Students incorrectly identify the units for volume. For example, use square inches to represent volume instead of cubic inches.

Strategies to Support Tiered Instruction



- Teacher reviews definitions of surface area and volume, and co-creates an anchor chart to display in the room explaining each. Providing flash cards or cue cards with the formulas will help students in place of anchor charts when they are outside the classroom area.
- Teacher explains the difference between two-dimensional and three-dimensional shapes. When working with two-dimensional shapes, we label in units², but when working with three-dimensional shapes, we label with units³.
- Teacher models the use of manipulatives and geometric software to review the concept of area and perimeter.
- Teacher breaks down formulas for area of a rectangle and volume of a rectangular prism to show when finding area, we are multiplying two sides, which is why we use units², but with the rectangular prism, we are multiplying three sides, so we use units³ to label.

Instructional Tasks

Instructional Task 1 (MTR.4.1, MTR.5.1)

Imagine that the prism pictured below is packed full of smaller identical prisms. The length of each edge of the small prisms is a unit fraction.



Part A. Give the dimensions of the small prisms that can be used to pack the larger prism.

- Part B. How many of the small prisms would it take to completely fill the larger prism? Explain how you found your answer.
- Part C. Explain how the number of the small prisms needed to fill the larger prism is related to the volume of the large prism.

Instructional Items

Instructional Item 1

A right rectangular prism has a length of $4\frac{1}{2}$ feet, a width of $6\frac{1}{2}$ feet and a height of 8 feet. What is the volume of the prism?

Instructional Item 2

Alex has 64 cubes, with dimensions in feet (ft), like the one shown.



He uses all the cubes to fill a box shaped like a larger rectangular prism. There are no gaps between the cubes.

Part A. What is the volume, in cubic feet, of the larger rectangular prism? Part B. What is a possible set of dimensions, in feet, of the larger rectangular prism?



*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.

MA.6.GR.2.4

Benchmark

Given a mathematical or real-world context, find the surface area of right MA.6.GR.2.4 rectangular prisms and right rectangular pyramids using the figure's net.

Benchmark Clarifications:

Clarification 1: Instruction focuses on representing a right rectangular prism and right rectangular pyramid with its net and on the connection between the surface area of a figure and its net.

Clarification 2: Within this benchmark, the expectation is to find the surface area when given a net or when given a three-dimensional figure.

Clarification 3: Problems involving right rectangular pyramids are limited to cases where the heights of triangles are given.

Clarification 4: Dimensions are limited to positive rational numbers.

Connecting Benchmarks/Horizontal Alig	nment Terms from the K-12 Glossary
• MA.6.NSO.2.1, MA.6.NSO.2.2,	• Area
MA.6.NSO.2.3	• Net
• MA.6.NSO.3.5	Rectangular Prism
• MA.6.AR.2.3	Rectangular Pyramid
Vertical Alignment	
Previous Benchmarks	Next Benchmarks
• MA.5.GR.2.1	• MA.7.GR.2.2

Purpose and Instructional Strategies

Students in grade 5 found the area of a rectangle with fractional or decimal sides. In grade 6, students find the surface area of right rectangular prisms and pyramids. In grade 7, students calculate the surface area of right circular cylinders.

- Instruction includes constructing models and nets of three-dimensional figures and • describing them by the number of edges, vertices and faces. Providing these opportunities will allow students to manipulate materials and connect to the symbolic and more abstract aspects of geometry.
- Instruction includes students using formulas and decomposition strategies to find the surface area of figures. Using the dimensions of the individual faces, students should calculate each rectangle or triangle area and add these values together to find the surface area of the figure.
- Instruction includes describing the types of faces needed to create a three-dimensional figure. Students can make and test conjectures by determining what is needed to create a specific three-dimensional figures.
- Students need to practice the language of the problems they are being asked to solve.



- For instance, when being asked how much wrapping paper needed to wrap a box, they know from experience that they are working with surface area. If they are being asked how many boxes will fit in a shipping container, then they are looking at volume.
- When using rational numbers, instruction should stay within the same form. Students should not be penalized though if they convert from one for to another when performing operations.
 - For example, if students are working with fractions, the side lengths will not include decimals. If students are working with decimals, the side lengths will not include fractions.
- Instruction includes representing measurements for surface area as square units, units squared or units².
- Problem types include having students measure lengths using a ruler to determine the surface area.

Common Misconceptions or Errors

- Students may not be able to determine the difference in the two-dimensional figures that compose three-dimensional figures.
- Students may invert the formulas for surface area and volume.

Strategies to Support Tiered Instruction

- Teacher provides nets of the three-dimensional figures and model color coding each similar shape. This will help students properly identify each shape to find the area to calculate surface area.
 - For example, a right rectangular prism can be modeled by the net shown below.



- Teacher reviews definitions of surface area and volume and co-creates an anchor chart to display in the room explaining the differences between them. Teacher models the use of manipulatives and geometric software to review the concept of area and surface area.
- Teacher breaks down formulas for area of a rectangle and volume of a rectangular prism to show when finding area, we are multiplying two sides which is why we use units², but with the rectangular prism, we are multiplying three sides, so we use units³ to label. Providing flash cards or cue cards with the formulas will help students in place of anchor charts when they are outside the classroom area.

Instructional Tasks

Instructional Task 1 (MTR.6.1)

The surface area of a rectangular prism is 115 square inches. The net of the prism is shown. What are the possible dimensions of the prism?





Instructional Items

Instructional Item 1

Carl is shipping a cardboard box that is a rectangular prism. The net of Carl's box is shown. What is the area of cardboard, in square inches, required for Carl's box?



Instructional Item 2

Maxwell is making a replica of the Egyptian pyramids. The figures' dimensions have a square base with a side length of 7.7 cm and a slant height of 6.2 cm. Maxwell wants to cover the model with gold paper. How much paper, in square centimeters, is needed to cover the pyramid?



*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive. Data Analysis & Probability

MA.6.DP.1 *Develop an understanding of statistics and determine measures of center and measures of variability. Summarize statistical distributions graphically and numerically.*

MA.6.DP.1.1

Benchmark	
MA.6.DP.1.1	Recognize and formulate a statistical question that would generate numerical data.

Example: The question "How many minutes did you spend on mathematics homework last night?" can be used to generate numerical data in one variable.

Connecting Benchmarks/Horizontal Alignment

Terms from the K-12 Glossary



• MA.6.AR.1.1

Data Statistical Question

•

Vertical Alignment

Next Benchmarks

Previous BenchmarksMA.5.DP.1.1

• MA.7.DP.1.5

Purpose and Instructional Strategies

In elementary grades, student collect numerical and categorical data to construct tables and graphs. In grade 6, students are formally introduced to statistical information and formulating statistical questions for numerical data. In grades 7 and 8, students will extend this when working with categorical data and then with bivariate data (*MTR.1.1, MTR.4.1*).

- Statistics are numerical data relating to a group of individuals; statistics is also the name for the science of collecting, analyzing and interpreting such data. It is a method for translating a real-world context into a collection of numbers. A statistical question anticipates an answer that varies from one individual to the next and is written to account for the variability in the data. Data are the numbers produced in response to a statistical question. Data are frequently collected from surveys or other sources (i.e., documents).
- Instruction focuses on statistical questions that generate numerical data. Once the data is gathered, it can be organized in a table or displayed in a graph.
- Instruction includes the understanding of a statistical question and a non-statistical question. A statistical question can be answered by collecting information that addresses differences in a population. A statistical question concerns some characteristic of a collection of individuals rather than of one specific individual.
 - For example, the question "How tall am I?" is not a statistical question because there is only about a single individual and there is only one response; however, "How tall are the students in my class?" is a statistical question since it can be answered by gathering information from many students and it is anticipated that this information will vary from one student to the next.
- Survey questions can be used to collect data to gather information for a statistical question.
 - For example, the questions "What are the shoe sizes of the students in your class?" and "What is the average shoe size of the students in your class?" can be construed as statistical questions if your students are to gather the data to try to answer them. They might gather this data by asking the survey question "What is your shoe size?"

Examples	Non Examples
• What is the range of ages of	• How old am I?
students in my school?	• How many pets do my
• How many pets are owned by each	grandparents own?
student in my grade level?	• What is my sister's math test
• What is the average math test scores	score?
of the students in my class?	• What is Martha's favorite type
• How many cupcakes of each type	of cupcake?
were made at the bakery in a week?	• How many letters are in my
• How many letters are in the names	name?
of each person in my class?	• What is my height?



• What is the median height of people	
in my class?	

- For numerical data, statistical questions can result in a narrow or wide range of numerical values. To collect this information, students design a survey question that anticipates variability by providing a variety of possible anticipated responses that have numerical answers, such as 3 hours per week, 4 hours per week and so on. Be sure questions have specific numerical answers.
- Well written statistical questions refer to the following two aspects: population of interest, measurement of interest, and such a question anticipates answers that vary.
- Instruction includes students determining how statistical questions imply that there was data gathered in order to determine a measure of center or measure of variation.
 - For example, the statistical question "How much money does a household in Lake County generally spend on internet in a year?" implies that one must gather numerical data on the cost of internet for households in Lake County to determine how much is generally, or on average, spent.
- Instruction includes the understanding that statistical questions are not limited to data that can gathered by students themselves.
 - For example, the question "What are the ten largest cities in Florida?" can be considered a statistical question because data was collected to determine this.

Common Misconceptions or Errors

- Students may believe that all the questions that they write are statistical questions. Students need to understand that a statistical question must have a range of numerical answers. They will need to have sample questions and practice writing their own.
- Students may think that a survey question is a statistical question, since a survey question can be used to answer a statistical question. A statistical question concerns a population. A survey question is asked of individuals in a population to help answer a statistical question.

Strategies to Support Tiered Instruction

- Teacher provides a list of examples of statistical questions and what qualifies them as statistical to assist students who incorrectly label non-statistical questions.
- Teacher provides simple examples that show how a statistical question concerns an entire population and a survey question concerns an individual within a population. Survey questions can be used to gather data to answer statistical questions.
 - For example, the statistical question "What is the average height at your school?" can be answered by gathering data using the survey question "What is your height?".
- Teacher provides instruction focused on patterns that make statistical questions and how to change non-statistical questions into statistical questions. Teachers work with students on examples to determine if each question is statistical or non-statistical. If the question is non-statistical, teacher models how they can convert it to be a statistical question.
- Teacher provides a list and co-constructs a graphic organizer and determines the pattern from statistical and non-statistical questions. Students will have opportunity to explain why each one is either statistical or non-statistical.
 - For example, "What are the ten largest cities in Florida?" can be considered a statistical question because one must gather data on all of the cities in the state of



Florida. A survey question that can be used to answer this statistical question is "What is the population of your city?"

- For example, "How many movies did you watch last month?" can be considered a survey question which can be used to answer various statistical questions like "What is maximum and minimum number of movies watched last month?" or "What is the average number of movies watched last month by 6th graders?"
- Example of a graphic organizer is shown below.

Question Type	Characteristics	Examples
Statistical	A question that can be answered by collecting data.	What is the average cost of a home in
	Often there will be variability in the data.	this neighborhood?
Data-gathering	Often a question that is on a survey.	Does your father work from home?
Other	A question that is typically not answered by collecting data or used to collect data.	When will you be home?

• Teacher provides sample questions and models how to practice writing their own.



Instructional Tasks

Instructional Task 1 (MTR.7.1)

Write a statistical question that will require data that could be collected from your class to provide information to an advertising agency for teenagers to purchase clothing, shoes, backpacks or school supplies.

- a. Design a table for data collection.
- b. Create a proposal to the advertising agency to recommend an item to advertise based on the data you collected from your statistical question. Include data to support your recommendation.

Instructional Items

Instructional Item 1

Amir collected data from his sixth-grade class at Liberty Middle School. He asked about the amount of time students spent playing video games. Write a statistical question associated with his data.

Instructional Item 2

Which of the questions below are statistical?

- a. Are there typically more manatees in Tarpon Springs or in Blue Springs?
- b. How many Instagram followers does Mr. Youmans have?
- c. How many points did the basketball team score in its last game?
- d. What is the range of photos students in Ms. Alvarez's class have on their phone?
- e. How many minutes a week do 8th graders at Bridgton Middle School spend watching TV?

*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.

MA.6.DP.1.2

Benchmark

MA.6.DP.1.2 Given a numerical data set within a real-world context, find and interpret mean, median, mode and range.

Example: The data set {15, 0, 32, 24, 0, 17, 42, 0, 29, 120, 0, 20}, collected based on minutes spent on homework, has a mode of 0.

Benchmark Clarifications:

Clarification 1: Numerical data is limited to positive rational numbers.



Connecting Benchmarks/Horizontal Align	ment Terms from the K-12 Glossary
• MA.6.NSO.2.3	• Data
• MA.6.NSO.3.5	• Mean
• MA.6.AR.2.2, MA.6.AR.2.3	Median
	• Mode
	• Range
Vertical Alignment	
Previous Benchmarks	Next Benchmarks

• MA.5.DP.1.2

• MA.7.DP.1.1, MA.7.DP.1.2

Purpose and Instructional Strategies

In grade 5, students interpreted numerical data, with whole-number values, represented with tables or line plots by determining the mean, median, mode and range. In grade 6, students find and interpret mean, median, mode and range given numerical data set with positive rational numbers. In grade 7, students continue building their knowledge while using measures of center and measures of variability to compare two populations.

- Instruction includes developing statistical questions that generate numerical data.
- Instruction includes the understanding that data sets can contain many numerical values that can be summarized by one number such as mean, median, mode or range.
- Instruction includes data sets that have more than one mode. Students should understand that a mode may not be descriptive of the data set.
- Instruction includes not only how to calculate the mean, but also what the mean represents (*MTR.4.1*).
- Instruction focuses on statistical thinking that allows for meaningful discussion of interpreting data (*MTR.4.1*). Students should be asked:
 - What do the numbers tell us about the data set?
 - What kinds of variability might need to be considered in interpreting this data?
 - What happens when you do not know all the measures in your data set?
 - Can you find missing data elements?
- Instruction includes student understanding of the difference between measures of center and measures of variability.
- Instruction includes students knowing when a number represents the spread, or variability, of the data, or when the number describes the center of the data.
- The data set can be represented in tables, lists, sets and graphical representations. Graphical representations can be represented both horizontally and vertically, and focus on box plots, histograms, stem-and-leaf plots and line plots.



Common Misconceptions or Errors

- Students may incorrectly believe that "average" only represents the mean of a data set. Average may be any of the following: average as mode, average as something reasonable, average as the mean and average as the median.
- Students may confuse mean and median.
- Students may neglect to order the numbers in the data set from least to greatest when finding the median or range.

Strategies to Support Tiered Instruction

- Teacher discusses with students how the use of the word average in daily life may show a different meaning of the word each time, just as other mathematical words have different meanings in everyday life. This will help students to understand that "average" does not only represent the mean of a data set.
- Teacher provides instruction focused on measures of center, co-creating anchor chart or graphic organizer.
- Teacher provides examples visually that show the clear middle of a data set, but where the average is not the same. This visual will help students understand that the middle of a data set does not mean that amount is the average.
 - For example, the figure below shows a data set with mean of 7 and median of 4.



Instructional Tasks

Instructional Task 1 (MTR.4.1, MTR.5.1)

Salena has 15 students in her class. The mean shoe size is 8.5. She records the shoe sizes below, with one missing:

7.5, 10, 15, 6.5, 7, 9, 9.5, 6, 11, 8.5, 7, 12, 6, 6.5, ____

What shoe size is missing? Explain how she can find the missing shoe size.

Instructional Task 2 (MTR.5.1)

Brandi is in the Girl Scouts and they are selling cookies. There are 11 girls in her troop. The median number of boxes of cookies sold by a girl scout is 26, and the range of the number of boxes sold is 30 boxes.

Part A. What is a possible set of boxes of cookies sold?

Part B. If the mean number of boxes of cookies sold is 22, describe some possible characteristics of the data set.

Instructional Items



Instructional Item 1

Jonathan works for a sporting goods store, and he is asked to report his sales, in dollars, of running shoes for the week. His numbers are given below. {150.25, 122.85, 171.01, 118.48, 108.52, 130.15, 154.36} Part A. What is the mean? Part B. What is the median?

Part C. If you were Jonathan, which measure would you report and why?

*The strategies, tasks and items included in the B1G-M are examples and should not be considered comprehensive.

MA.6.DP.1.3

Benchmark

Given a box plot within a real-world context, determine the minimum, the lower quartile, the median, the upper quartile and the maximum. Use this MA.6.DP.1.3 summary of the data to describe the spread and distribution of the data.

Example: The middle 50% of the population can be determined by finding the interval between the upper quartile and the lower quartile.

Benchmark Clarifications:

Clarification 1: Instruction includes describing range, interquartile range, halves and quarters of the data.

Connecting Benchmarks/Horizontal Alig	gnment Terms from the K-12 Glossary
• MA.6.NSO.2.3	Box Plot
• MA.6.NSO.3.5	• Data
	• Interquartile Range (IQR)
	Median
	• Quartiles
	• Range (of a data set)
Vertical Alignment	
Previous Benchmarks	Next Benchmarks

• MA.5.DP.1.1, MA.5.DP.1.2

• MA.7.DP.1.1, MA.7.DP.1.2



Purpose and Instructional Strategies

In grade 5, students collected and represented fraction and decimal data using tables, line graphs or line plots. They also interpreted whole-number data by determining the mean, median, mode or range. In grade 6, students will be given a box plot in a real-world context to determine quartile values as well as describe the spread and distribution. In grade 7, students will then use the measures of center and variability to make comparisons, interpret results and draw conclusions about two populations (*MTR* 7.1).

- Instruction includes developing statistical questions that generate numerical data.
- Box plots represent only numerical data sets and display the data's spread.
- Instruction focuses more on variation rather than measures of central tendency.
- Vocabulary instruction emphasizes qualitative descriptive words such as symmetrical and skewed.
- Instruction focuses on box plots' benefits and disadvantages in relation to other graphical representations.
- Instruction relates to MA.6.DP.1.5 in which students will create box plots to represent sets of numerical data.
- Instruction includes horizontal and vertical representations of box plots (MTR.2.1).
- Instruction provides opportunities for students to use the following terms interchangeably (*MTR.4.1*).
 - $\circ\;$ lower quartile (LQ), quartile 1 (Q1) and the boundary for the lowest 25% of the data set
 - \circ median and quartile 2 (Q2)
 - upper quartile (UQ), quartile 3 (Q3) and the boundary for the highest 25% of the data set
 - \circ interquartile range (IQR) and the middle 50% of the data set



Common Misconceptions or Errors

- Students may have difficulty remembering what percentage of data is above or below the specific quartile (e.g., 25% below LQ, 50% below/above median, 25% above UQ, etc.)
- Students may have difficulty determining the median of an even set of data.



Strategies to Support Tiered Instruction

- Teacher reviews vocabulary for students who have difficulty understanding what percentage of data is above or below the specific quartile. Students should be given opportunity to relate "quartile" to "quarter." Teachers can ensure students understand that "quartile" means 25% and recognize the median as "middle" of the data.
- If there are an even number of total data point, teacher models how the median is found by finding the mean of the two middle data points. Teacher provides opportunity for students to practice this skill by gradually releasing them until they are proficient and gain understanding.
- Teacher co-constructs vocabulary guide or anchor chart with students who need additional support understanding the vocabulary for measures of center and variation.
 Examples of guides and charts are shown below.

xamples of guid		
Term	Definition	How it is found or calculated
Mean		
Median		
Mode		
Range		
Interquartile		
Range (IQR)		
Quartiles		
lower qu Q_1	artile median	upper quartile Q_3
min whisker		max whisker
L_	b	ox

interquartile range (IQR)



Instructional Tasks

Instructional Task 1 (MTR.5.1)

Use the data from the International Shark Attack File on the number of shark attacks in Florida, which is given in the table below, along with the corresponding box plot to answer the following questions.

Year	2009	2010	2011	2012	2013	2014	2015	2016	2017	2018	2019
Number of Attacks	19	14	11	27	23	28	30	32	31	16	21





Part A. When did the most number of shark attacks occur? When did the lowest number of shark attacks occur? Why do you think this was the case?

Part B. What is the median number of shark attacks?

Part C. What percentage of attacks was below 30?

Instructional Items

Instructional Item 1

The box plot represents the AdvertiseHere company employees' ages. State the lowest age, lower quartile age, median age, upper quartile age and highest age.



*The strategies, tasks and items included in the BIG-M are examples and should not be considered comprehensive.

MA.6.DP.1.4

Benchmark

MA.6.DP.1.4 Given a histogram or line plot within a real-world context, qualitatively describe and interpret the spread and distribution of the data, including any symmetry, skewness, gaps, clusters, outliers and the range.

Benchmark Clarifications:

Clarification 1: Refer to K-12 Mathematics Glossary (Appendix C).

Connecting Benchmarks/Horizontal Alignment	Terms from the K-12 Glossary
• MA.6.NSO.2.3	• Cluster
• MA.6.NSO.3.5	• Data
	Histogram
	Line Plot
	• Outlier
	• Range
Vertical Alignment	



Previous Benchmarks

Next Benchmarks

• MA.5.DP.1.1

• MA.7.DP.1.5

Purpose and Instructional Strategies

In grade 5, students interpreted numerical data from tables and line plots by determining the mean, median, mode and range. In grade 6, students extend their understanding of data interpretation by describing qualitatively the symmetry, skewness, gaps, clusters and outliers of line plots and histograms. Additionally, students will expand from whole-number data sets to rational-number data sets and to include histograms as a graphical representation. In grade 7, students compare two data sets to interpret and draw conclusions about populations.

- Instruction includes developing statistical questions that generate numerical data.
- Instruction includes the understanding that line plots are useful for highlighting clusters, gaps and outliers within a data set and show the shape of the distribution of a data set while displaying the individual data points. Likewise, students should understand that histograms are useful for highlighting clusters and gaps and shows the shape of the distribution of a data set without displaying the individual data points. Additionally, histograms help identify the shape and spread of the data set.
- Problem types include using a histogram's or line plot's symmetry, skewness, gap(s), cluster(s), outlier(s) or range to qualitatively describe the spread/distribution; qualitatively interpret the spread/distribution; or both qualitatively describe and interpret the spread/distribution.
- Instruction relates to MA.6.DP.1.5 in which students create histograms to represent sets of numerical data.
- When describing the distribution, students are not expected to use the term uniform. Instruction focuses on describing data as normal, skewed or bimodal.

Normal	Skewed	Bimodal
NUMBER OF CANS COLLECTED	NUMBER OF CANS COLLECTED	NUMBER OF CANS COLLECTED
0.10 11-20 21-30 31-40 41-50	0-10 11-20 21-30 31-40 41-50	0.10 11.20 21.30 31.40 41.50

• Within this benchmark, the expectation is not to identify skewness as positive, negative, left or right. Students are only expected to describe and interpret skewness within a data set generally. When describing spread of the distribution, students should be able to interpret whether the data set has a narrow range (less spread), wide range (more spread) or contains an outlier (*MTR.4.1*).



Common Misconceptions or Errors

- Students may confuse bar graphs (categorical data) and histograms (numerical data).
- Students have difficulty understanding skewness and how that relates to data and its interpretation.

Strategies to Support Tiered Instruction

- Teacher displays histograms and line plots, side by side and discuss with students to compare and contrast each one will assist in students understanding the difference between the two, and what information can be interpreted from each one.
- Teacher facilitates discussion on symmetry, skewness, gaps, clusters, outliers, and range with students, providing instruction when needed. Teacher provides additional examples for students to reference after instruction.
- Teacher displays a graph or other visual representation to show a real-world example will assist in students seeing data that is skewed.
 - For example, showing a dot plot of the number of Electoral Votes states have will show data that is skewed. Then conversations can be had about what is means that most of the data points are to the left, and which states have the most votes.

	Electoral		Electoral		Electoral
State	Votes	State	Votes	State	Votes
Alabama	9	Kentucky	8	North Dakota	9
Alaska	3	Louisiana	8	Ohio	18
Arizona	11	Maine	4	Oklahoma	7
Arkansas	6	Maryland	10	Oregon	7
California	55	Massachusetts	11	Pennsylvania	20
Colorado	9	Michigan	16	Rhode Island	4
Connecticut	7	Minnesota	10	South Carolina	9
Delaware	3	Mississippi	6	South Dakota	3
District of	3	Missouri	10	Tennessee	11
Columbia					
Florida	29	Montana	3	Texas	38
Georgia	16	Nebraska	5	Utah	6
Hawaii	4	Nevada	6	Vermont	3
Idaho	4	New	4	Virginia	13
		Hampshire			
Illinois	20	New Jersey	14	Washington	12
Indiana	11	New Mexico	5	West Virginia	5
Iowa	6	New York	29	Wisconsin	10
Kansas	6	North Carolina	15	Wyoming	3



Instructional Tasks

Instructional Task 1 (MTR.4.1)

Provide students, either individually or whole group, the histogram below. Have the students do a slow and close look at the graphical representation for 2 minutes. While the students are doing this, have them write down as many noticings and wonderings of the graph as they can. Have students share with a partner their thinking. Then as a class, create a cohesive description and interpretation of the histogram.



Instructional Task 2 (MTR.4.1)

The data set {3.25, 2.25, 0.5, 1.5, 1, 0.75, 4, 1, 2.25, 2, 1.5, 1.5, 0.75, 3, 4, 2} is the result of LaKeesha taking a survey of her class to find out how many hours each student spent on their phone on Tuesday. Describe the distribution by stating its symmetry, its range, any outliers, any clusters and any gaps.

Instructional Items

Instructional Item 1

The line plot below shows the distribution of test scores in Mrs. Duncan's math class.



- Part A. Describe the shape of the distribution. What does the shape of the distribution indicate about how students scored on the math test?
- Part B. Describe the spread by using the range and explain what the shape means in terms of the students' scores on the math test.

*The strategies, tasks and items included in the B1G-M are examples and should not be considered comprehensive.



MA.6.DP.1.5

	Benchmark	
N	IA.6.DP.1.5	Create box plots and histograms to represent sets of numerical data within real- world contexts.

Example: The numerical data set {15, 0, 32, 24, 0, 17, 42, 0, 29, 120, 0, 20}, collected based on minutes spent on homework, can be represented graphically using a box plot.

Benchmark Clarifications:

Clarification 1: Instruction includes collecting data and discussing ways to collect truthful data to construct graphical representations.

Clarification 2: Within this benchmark, it is the expectation to use appropriate titles, labels, scales and units when constructing graphical representations.

Clarification 3: Numerical data is limited to positive rational numbers.

Connecting Benchmarks/Horizontal A	Alignment Terms from the K-12 Glossary
• MA.6.NSO.2.3	Box Plot
• MA.6.NSO.3.5	• Data
	• Histogram
Vertical Alignment	
Previous Benchmarks	Next Benchmarks

MA.5.DP.1.1

• MA.7.DP.1.5

Purpose and Instructional Strategies

In grade 5, students collected and represented numerical data using tables, line graphs or line plots and interpreted this data by determining the mean, median, mode and range. In grade 6, students include box plots and histograms to the types of data displays they are creating. In grade 7, students are asked to choose and create an appropriate graphical representation of both numerical and categorical data, which includes bar graphs and circle graphs (*MTR.1.1, MTR.2.1, MTR.7.1*).

- Instruction includes developing statistical questions that generate numerical data.
- Instruction includes opportunities for students to collect their own data to create a graphical display. This increases student interest in analyzing the data (*MTR.1.1*).
- Scales can be represented using brackets, ranges, inclusive or exclusive endpoints.
 - For example, the numerical data set from the example is {15, 0, 32, 24, 0, 17, 42, 0, 29, 120, 0, 20}. A student has determined to use intervals of 0-20, 20-40, 40-60, 60-80, 80-100, 100-120.
 - Students could use brackets represent inclusive endpoints and parentheses to represent exclusive endpoints. Students can write the intervals as [0-20); [20-40); [40-60); [60-80); [80-100); [100-120].
 - Students can write the intervals as 0-20, 21-40, 41-60, 61-80, 91-100, 101-120 since the data only contains whole numbers.
 - It is important to note that students may create intervals (or bins) that do not necessitate the use of these as it is not an issue with the given data set.
 - \circ Students should discuss how there could be differences in distributions when the



bins of the histograms may vary.

- Given a set of data, allow students to choose to create either a histogram or box plot, ensuring both are being created. Then discuss pros and cons for why one may be preferred over another. Practice this using data sets containing whole numbers as well as with data sets containing positive rational numbers. Students should be provided with different ways to organize the data in order to best create the graphical representation.
- Instruction allows for analysis of the truthfulness or reasonableness of the data set. Students should understand whether the data can be used to showcase real situations.
- Instruction includes the use of online tools to quickly show the difference in distributions when changing the size of the bins in a histogram.

Common Misconceptions or Errors

- Students may choose bin sizes that do not effectively show the distribution of the data.
 - For example, students gathered gas mileage (in miles per gallon) data for 50 cars as shown in the histograms below. Histogram A easily shows the gas mileage for the majority of cars, and a much smaller count being above 40 miles per gallon. Histogram B uses very small bins which leads the consumer to believe that there is more variability in the data than truly exists.





- Students may incorrectly include the same number in 2 bins. For example, if bins are 0-10, 10-20, 20-30, etc., they must decide whether 10 is included in the first bin or if numbers greater than 0, but less than 10 are included in the first bin.
- Students may incorrectly calculate the median given a data set with an even number of values.
- Students may incorrectly believe more data will create a larger box in a box plot.
- Students may neglect to order values from least to greatest when creating a box plot.
- Students may neglect to include titles and labels in the graphical representations.



Strategies to Support Tiered Instruction

- Teacher reviews the difference between histograms and bar graphs, creating an anchor chart with properties of a histogram for students to refer to.
- Teacher reinforces how scales are represented with specific endpoints. The endpoints they chose to use, or as defined in a problem, tell them if the point is included in the bin or not. Include notation of endpoints on anchor chart to display in the classroom.
- If there are an even number of total data points, teacher models how the median is found by finding the mean of the two middle data points. Teachers provide opportunities for students to practice this skill by gradually releasing them until they are proficient and gain understanding.
- Teacher co-constructs vocabulary guide/anchor chart with students who need additional support understanding the vocabulary for measures of center and variation.



• Examples of guides and charts are shown below.



Instructional Tasks

Instructional Task 1 (MTR.3.1, MTR.7.1)

Data from the International Shark Attack File on the number of shark attacks in Florida is given in the table below.

Year	2001	2002	2003	2004	2005	2006	2007	2008	2009	2010	2011	2012	2013
Number of Attacks	34	29	29	12	17	21	31	28	19	14	11	27	23

Shark Attacks in Florida (2001-2013)

Part A. Construct a box plot to summarize this data.

- Part B. Identify and explain what each of the key numbers you used to make the box plot means in the context of the data.
- Part C. Describe the distribution of the number of shark attacks in Florida between 2001 and 2013. Be sure to describe the spread and distribution of the data.

Instructional Task 2 (MTR.4.1, MTR.7.1)

Below are the 25 birth weights, in ounces, of all the Labrador Retriever puppies born at Kingston Kennels in the last six months.

13.5	14	15.25	15.7	16	16.1	16.45	16.9	17.2	17.25
17.4	17.5	17.75	17.75	17.8	18	18	18.5	18.5	18.55
18.6	18.85	18.9	19.2	20					

- Part A. Use a box plot or histogram to summarize these birth weights and explain how you chose which type of graph to use.
- Part B. Describe the distribution of birth weights for puppies born at Kingston Kennels in the last six months. Be sure to describe the spread and distribution of the data.
- Part C. What is a typical birth weight for puppies born at Kingston Kennels in the last six months? Explain why you chose this value.

Instructional Items

Instructional Item 1

Every year a local basketball team plays 82 games. During the past two decades, the number of wins each year was:

42, 54, 51, 72, 67, 61, 43, 38, 53, 57, 41, 68, 54, 52, 47, 60, 46, 53, 73, 65 Make a histogram to summarize the data.

*The strategies, tasks and items included in the B1G-M are examples and should not be considered comprehensive.



MA.6.DP.1.6

Benchmark

MA.6.DP.1.6 Given a real-world scenario, determine and describe how changes in data values impact measures of center and variation.

Benchmark Clarifications:

Clarification 1: Instruction includes choosing the measure of center or measure of variation depending on the scenario.

Clarification 2: The measures of center are limited to mean and median. The measures of variation are limited to range and interquartile range.

Clarification 3: Numerical data is limited to positive rational numbers.

Connecting Benchmarks/Horiz	ntal Alignment Terms from the K-12 Glossary
• MA.6.NSO.2.3	• Data
• MA.6.AR.1.2	Interquartile Range
• MA.6.AR.2.3	• Mean
	Measures of Center
	Measures of Variability
	• Median
_	• Range (of a data set)
Vertical Alignment	
Previous Benchmarks	Next Benchmarks
• MA.5.DP.1.2	• MA.7.DP.1.1
	• MA.7.DP.1.2

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Purpose and Instructional Strategies

In grade 5, students interpreted numerical data by determining the mean, median, mode and range when the data involved whole-number values and was represented with tables or line plots. In grade 6, student understanding is extended to determine the measures of center and variation when the data points are positive rational numbers. Students are also expected to use their understanding of arithmetic to describe how the addition or removal of data values will impact the measures of center and variation within real world-scenarios. In grade 7, students will determine an appropriate measure of center or variation to summarize data and use them to make comparisons when given two numerical or graphical representations of data.

- Instruction includes student understanding that the choice between using the median or the mean as the measure of center or using the interquartile range or range as the measure of variation depends on the purpose.
 - For example, in some cases it is important to include the influence of outliers in the description of a population and the mean might be preferable as the measure of center and the range might be preferable as the measure of variation. If the influence of outliers is meant to be ignored, the median and interquartile range may be more preferable.
- Students should be provided with data sets and asked to find the measures of center and of variability. Students should explore and look for patterns when a data value is removed or a new data value is added that meet the following conditions (*MTR.5.1*):
 - The value is larger than the measure of center.
 - The value is equal to the measure of center.
 - The value is less than the measure of center.
 - \circ The value is greater or less than any value of the original data set.
 - The value is within the range of the original data set.
- Connecting the measures of center and variation to the visual representation on a box plot can help students understand what the value of the median, range and interquartile range represent within a context. If a value is added or removed from a data set, students can create a second box plot based on the new data set to help determine and describe the impact of the change (*MTR.2.1*).

Common Misconceptions or Errors

- Students may incorrectly categorize the data measures (mean, median, range, interquartile range) as measures of center or measures of variability. It can be helpful to frequently refer back to the purpose of a type of measure and how it relates to the center of the data or the variation of the data.
- Students may incorrectly try to determine the change by calculating the mean, median, range or interquartile range for the changed data set instead of calculating for both the initial and the changed sets before comparing.



Strategies to Support Tiered Instruction

- Instruction includes having students calculate the measures of center (mean and median) or the measures of variation (range and interquartile range) for the initial ____ and the changed data sets before comparing the impact of an outlier or an additional data point.
- Instruction includes co-creating a graphic organizer for measures of center (mean and median) and measures of variation (range and interquartile range) and include the generalized impact of outliers on each.

Instructional Tasks

Instructional Task 1 (MTR.5.1, MTR.6.1, MTR.7.1)

Mr. Biggs and his students shared the number of hours they played video games last week and Mr. Biggs recorded it on the table below.

2.5	12	0	28	6.75	21.25	1.2	16
7.33	1.5	4	15	7	2.5	16	0

Part A. Find a measure of center and variability to represent this scenario. Explain why you chose these measures.

- Part B. Mr. Biggs removed the 4 from the data set, since this represented the number of hours he played video games. Describe the impact this removal has on the measures of center and measures of variability of the data set.
- Part C. Mario is a new student in Mr. Biggs's class. If the number of hours Mario played video games caused the measure of center to increase, how long could Mario have played video games last week? Explain your reasoning.

Instructional Items

Instructional Item 1

Christian took his temperature, in degrees Fahrenheit (°F), every day for a week. His temperatures are shown in the table below:

Day	Temperature (°F)
Sunday	98.7
Monday	99.1
Tuesday	98.2
Wednesday	97.9
Thursday	98.1
Friday	98.8
Saturday	99.2
Sunday	

- Part A. If he took his temperature on the Sunday of the next week and it was 103.2°F, which measures of center and variation could be used to summarize the data? Explain your choice.
- Part B. How does the addition of the temperature 103.2°F impact the measures of center and variation?

*The strategies, tasks and items included in the B1G-M are examples and should not be considered comprehensive.

